## PROCEEDINGS OF THE

# 1620 USERS GROUP JOINT CANADIAN-MIDWESTERN REGION 

FEBRUARY 19-21, 1964<br>AT THE O' HARE INN, DES PLAINES, ILLINOIS

FRANK H. MASKIELL
REGIONAL SECRETARY

## MEETING SChEDULE

## 1620 USERS Group

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MEETING SCHEDULE
ATTENDANCE ROSTER
A RELOCATABIE SYMBOLIC PROGRAMMING SYSTEM
KINGSTON FORTRAN II
CARLTON COLLEGE GOMPILER - GARLTON BINARY SmMLATOR
MODIFYING MONITOR I TO INCLUDE OTHER PROGRAMMING SYSTEMS
A NEW GOURSE IN COMPUTER APPREGIATION
EDUCATION PANELISTS
A SURVEY OF THE BEGINNING PROGRAMMING COURSE
DATA PROCESSING TECHNICIAN TRAINING
INTRODDCTION TO MATRICES
A FAMILI OF TEST MATRICES
THE 1620 AS ANALYTICAL AND COMPOSITIONAL AID IN 12 TONE MUSIC
LOGIC THEORBM IETEGTION PROGRAM
AN ADDITIVE PSEUDO-RANDOM NUMBER GENERATOR
A MODEL DIFFUSION-REACTION PROGRAM
AUTOSPOTLPSS NUMERICAL CONTROL
AUTOSPOT II PREPROCESSOR PROGRAM
MANAGEMENT INFORMATION
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February 19-21، , 1964
WEDNESDAY, FEBRUARY 19, 1964

| 8:45 | GEN ERAL SESSION | Convention Hall |  |
| :---: | :---: | :---: | :---: |
|  | 8:45 Announcements | " " | B. Burrows |
|  | 8:55 IBM Announcements | " ${ }^{\prime \prime}$ | J. Jessee |
|  | 9:00 IBM Announcements | " " | G. Rercoco |
|  | 9:10 Programming Syst. Announcements | " " | L. Foster |
|  | 9:30 Index Register Concepts | " " | B. Soclis |
|  | 9:50 Kingstran | " " | D. Jardit |
| 10:30 | Coffee \& Rolls | " " |  |
| 10:45 | SELECTED SPS TOPICS-Elementary | " " |  |
|  | SPS WORKSHOP-ADVANCED | Grecian Room | D. Pratt |
| 12:15 | Lunch | Convention Hall |  |
| 1:30 | EXPLORATORY PROGRAMMING | " " | J. Morrissey |
| 3:00 | Coffee |  |  |
| 3:30 | PANEL OF 1710 USERS | D 4 | J. C. Hill |
|  | SPS WORKSHOP-ADVANCED | Grecian Room | D. Pratt |
| 7:30 | SOUND-OFF SESSION | " " | J.A. N. Lee |
| THURSDAY, FEBRUARY 20, 1964 |  |  |  |
| 7:45 | NEW USERS MEETING (coffee \& rolls) | D 3 | B. Burrows |
| 8:45 | INTRODUCTION TO MONITOR I | Convention Hall | IBM |
|  | PANEL OF 1311 USERS | Grecian Room | B. Burrows |
| 10:15 | Coffee \& Rolls | " " | \& Conven. Hall |
| 10:45 | INTRODUCTION TO MONITOR I | Convention Hall | IBM |
|  | MONITOR I WORKSHOP-ADVANCED | D 4 | IBM |
|  | Magnetic Tape Users Meeting | D 3 | B. Robinson |

FRIDAY, FEBRUARY 21, 1964

10:15

12:15
Lunch
Convention Hall
INTRODUCTION TO MATRICES " "
C. Maudlin, Jr.

MONITOR I WORKSHOP-ADVANCED D 4
IBM

| EDUCATION PAPERS | Grecian Room |  |  |
| :--- | :---: | :---: | :--- |
| 1:30 A New Course in |  |  | C. Davidson |
| "Computer Appreciation" | $"$ | $"$ |  |
| 1:45 A Survey of the Beginning | $"$ | $"$ | C. B. Germain |
| Programming Course | $"$ | $"$ |  |
| 2:00 Data Processing Technicians; " | " |  |  |

2:00 Data Processing Technicians;
W. J. McGraw
an Integrated Training Approach
at Hibbing Area Tech. Inst.
3:00 Coffee
Conven. Hall, Grec.Rm. \& D 4
3:30 Introduction to Regression Conven. Hall
MONITOR I WORKSHOP-ADVANCED D
C. Phillip Cox

IBM
APPLICATION PAPERS Grecian Room
3:30 The IBM 1620 as an A. Tepper

3:30 The IBM 1620 as an
Analytical \& Pre-
Compositional Aide in
12-Tone Music
3:50 A Family of Test Matrices
4:10 A New Random Number Generator
4:30 Logic Theorm Detection Program
A. Tepper
A.C.R. Newberry
H.T. Wheeler
J. Wheatley

MONITOR I \& II Demos
Repeat of 6:30 Program
Repeat of 6:30 Program

Convention Hall
D 2
Repeat
Panel of Commercial Data Processing D 4
PROGRAMMING SYSTEMS PAPERS Convention Hall " "
8:45 Magic I and II

PROGRAMMING SYSTEMS PAPERS Convention Hall
8:45 Magic I and II " "
$"$
9:15 Kingstran
Grecian Room

PANEL ON EDUCATION
R. Thomas
J.A. N. Lee

## IBM

IBM
D. Jardine

4

ENGINEERING \& CONTROL PAPERS D
0:45 AUTOSPOT II Pre-Processor Prog. D
11:00 Autospotless Numerical Control D 4
with the 1620
E. Ray Austin

11:30 Montecarlo Techniques applied to Radio Chemistry

D 4
J.K. Lewis

ROGRAMMING SYSTEMS PAPERS Convention Hall 10:45 Carleton College Compiler
11.00 Carleton Binary Simulator
D. Taranto

1:00 Carleton Binary Simulator
W. Gage

SPS
Other Programming Systems
M. Dorl
A. Purcell

PANEL ON EDUCATION

Lunch

| IGGERGAARD PAUL L ILCORN HERBERT R | GREEN GIANT CCMPANY <br> MISSOURI SCHOCL OF MINES $\varepsilon$ MET | LE SUEUR ROLLA | $\begin{aligned} & \text { MINN } \\ & \text { MD } \end{aligned}$ | DAVIDSCN JAMES L DAVIDSON CHARLES | LCNG ISLAND LTG UNIVERSITY CF WISCONSIN | HICKVILLE MADISON | $\begin{aligned} & \hline \text { NY } \\ & \text { WISC } \end{aligned}$ |
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| MLDMCH F C | CLDSMCBILE DIVISIEN | LANSING | MICH | EAWSCN J | IBM CCRPORATION | CALGARY | ALB |
| MLTENHOFE JOHN | ELECTRO-MOTIVE DIV-GMC | LA ERANGE | ILL | DECK JAMES C | INLAND STEEL COMPANY | EAST CHICAGO | IND |
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| AUSTIN HUBERT | tri-state college | ANGCLA | IND | EILLIMGER DR J L | UNIVERSITY OF ILLINOIS | CHICAGO | ILL |
| BABIENE RCBERT C | USAF - ACIC | ST LCUIS | MO | borl michael | UNIVERSITY OF WISCONSIN | MADISON | WISC |
| bachenber john J | INST CF PAPER CHEM | APPLETON | WIS | DCUGLAS LEE C | ARGCNNE NATL LAB | LAMCNT | ILL |
| BAEVERSTAD HAROLD $L$ | SUNDSTRAND MACHINE TCOL | BELVIDERE | ILL | COULCFFA A | TRANS CANADA PIPE LINES | TORCNTO | ONT |
| BAREUTES ROBERT F | IEM CORPORATICN | YOUNGSTOWN | CHIO | CRESSLER EYRCN | KENT STATE UNIV | KENT | OHIO |
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| STRDESE E I | CCLUMEIA GAS SYSTEM | COLUMBUS 12 | OHIO |  |  |  |  |
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## A Rolocatable Programing Systan

A rolocating assembler for the porpose of this discussion is one which assembles a program in such a form that it may be placed anywhere in memory at load times 1.e. the program does not have to be re-assembled to change its origin. This has bean accomplished in the past by manually placing flags on the digits of the op-code or by using origins greater than the machine size. The suthor finds that these systems have definite disadvantages and has decided on a system in which each operand (either instruction or DSA) carries with it a system assigned relocating tag which determines its relocatability status.

An assembler which produces a relocatable object deck should be of much use in programs amploying subroutines (Fortran, SPS) or in systems of progrems.

The R-SPS system which should be in the library by June of 1964 consists of essentially a 3 pass systcm $t$ Two assembly passes and one compressing pass. The assembly passes may be batched as may the compressing pass.

The main disadvantage of the system is the increased size of the object deck.

The following pages taken from the program write-up further serve to explain the arstem and its use.

|  | Program Abstract |
| :---: | :---: |
| Title: | R-SPS |
| Author: | Michoel Dorl <br> EngIneering Computing Laboratory University of Wisconsin |
| Dote: | 1-1-64 |
| Users Group Code: | 3155 |
| Direct Inguiries to: | Prof. C. H. Davidson <br> Director, <br> Engineering Computing Laboratory <br> University of Wisconsin <br> Madison, Wisconsin 53706 <br> Phone 608-262-3892 |

Description/Purpose
R_SPS provides the capability of relocating ordinary SPS progrems a load time. The assembled decks which it produces are relocatable in the full sense of the word. The system provides the programer with complete control over the relocating feature, elther through manual intervention or through programming. In addition error checking has been expanded ond assembly speed increased.

## Spectifications

```
Storage:
40 K or larger (self-adjusting
```

Equipment:
a) Card system
b) Automatic divide
c) Indirect oddressing

The automatic divide feature is used only to process one seldom used Instruction (MORG). Thus the Automivice restriction could be easily over. come by not using inat instruction.

$$
\text { The program connot be used on o } 20 \mathrm{k} \text { machine. }
$$

Program Language UK_SPS
Language Used In wire-up Engiish
Remorks
Although UW_SPS is not in the programming librery, it is quite similar to R-SPS (see write-up). Copies are avaliable upon request from the author

## Table of Contents

## ENTRY

## Deck Labelling Sheet

## Program write-up

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|  | Program Write-up <br> General Dats |
| :---: | :---: |
| Program Name: | R_SPS |
| Dote: |  |
| Progremmer. | Michael Dorl |
|  | Englineering Computing Laboratory |
|  | University of Wisconsin |
|  | medison, wisconsin |
|  | Phone 608-262-3892 |
|  | User Code 3155 |

Machine Configuration Required
a) Card $1 / 0$
b) 40 k or more
d) Auto-divide

## Program Devetoped On

a) 1620 MOD
c) Indirect addressing
d) 60 k
e) Auto-divide

## Programming System Used in Develooment

R-SPS was assembled using an R-SPS assembled by UW-SPS. Although UW_SPS is not in the program library, it is quite similar to R-SPS. Copies of UW_SPS may be obtained from the author.

The final form of R_SPS is a dumped deck. The dumper is also available from the author.

## Introduction

R-SPS is a Relocatable Symbolic Programming System. It gives the pro-R-SPS is a Relocatable Symbolic programming system. It gives the programmer much more complete and ecsy control over the loading ond relocating
operation than any of the severat other systems available for the 1620 . The jecks which it produces can be re:ocated of load time under complete contro cf the programmer. In addition, assembly thas been speeded up by a random synibol table store and recovery technique so that the assembler is reader oound during pass 1 and punch bound during pass 2 .

In the following discussion it is assumed that the reader is familiar with the use o: IBM SPS and the SPS Reference Monual (IBM 1620/1710 Symbolic frogramming sy:.:Em--C 26-5600).

## Cord Inout Format

Two separate card input formats are provided.

1) UW_SPS format
columns 7-12 for label
columns $14-17$ for instruction
columns 19-77 for operands and comments
2) IBM SPS format
columns ó-11 for label
columns 12-15 for instruction
columns 16-74 for operonds ond corments
The author believes the UW-SPS format to be superior in that all three fields are separated by at least one blank on the card, permitting consistent skipping to the beginning of each new field during keypunching.

Note that the IBM SPS format is modified slightly in that columns 16-74 are available for operands and comments, rather than columns 16-75.

Use of either card format is of the option of the user. The assembler recognizes both types as legal, and they may be intermixed in the same program.

Columns 1-5 are availoble for card identification under both sard formats; however these columns will not appear on the object tisting. since column 6 is used in determining the card format, its use is pronibited for other than lobel field under IBM Format.

Columns 78-80 for UW_SPS Format and columns 75-80 for IBM SPS Format are also available for card identification.

## Statements

Statements are of three types:

1) Processor Instructions, which give the assembler certain commands,
2) Nachine Instructions, which are translated to actual Machine operations,
3) Declarative Instructions, which tell the processor to set aside $\frac{\text { Declarative }}{\text { certain work }}$ areas or set up actual constonts to be used.

## Special Characters

The $\oplus$, *, ond $\$$ ore used for special purposes in R-SPS.

## -3-

The @sign is used to call for a record mark to be incorporated in elther a declarative operation or in the $P$ or $Q$ field of an instruc. tion.

If on@sign is used in a declarative operation it must appear os the last character in the constant. For example,


In the DAC and DACF instruction only terminal signs generate records marks.

In the case where a label is attached to a $D C$ with an sign, the address assigned to the label will be the address of the record mark.
or $Q_{11}$ of on instruction:

$$
\begin{aligned}
& \text { TDM } \quad A=15000 \\
& 3 \quad 15150000000 \%
\end{aligned}
$$

The $Q$ will be translated os a record mark in position $P_{6}$ or $Q_{11}$ respectively; however the when used in this way must appear alone.

The * when usec for address adjustment refers to:

1) the last assigned oddress when used in dectarative or processor instructions.
2) the address of the instruction in which it is used.

The * is treated as a relative oddress.
The $\$$ sign is used to call for a symbolic address under a given head character. For example,
refers to $H I$ neaded by $A$.
Operands used in instructions, for length definition, or for assigned addresses may be of the following form.

$$
\pm A \pm B \pm c \pm 0
$$

Uo to four terms may be included and may be added or subtracted as indiceted. No multiolication is allowed.

The dollar sign may be used to generate a group mork at the end of a numeric constant in the same monner as on o sign.

The rules which determine whether an operand is relocatable (and therefore must be changed ouring lood time) or absolute are given below:

1) The sum or differeace of two absolute quantities is absolute.
2) The sum or difference of an absolute and a relative quantity is relotive.
3) The difference of two relative quantities is absolute.
4) Calling for the sum of two relative quantities is lllegal.

The sign of a relocatable operand is preserved of load time, for only its megnitude is increased by the relocating vector.

## Processor and Declarative Operations

In declarative operations, labels or symbalic oddresses may be assignes as in 13 SPS; however, the relocating of such a label is determined by its assigned address according to the following rules:

1) An integer address is absolute and makes the ossociated labe sbsolute. For example, in

A DS 2, 807
A will be taken as equivalent to an obsolute 80 ? wherever it appears.
2) A symolic oddress gives its relocatability to the label. If $Q$ is an absolute quantity and $Z$ is a relative quantity then in the following statements
$\begin{array}{lll}A & D S & 0 \\ A A & D S & Z\end{array}$
A will be absolute ond AA will be relative.
3) A processor-assigned oddress is relative.

$$
\text { e.g. } A \text { DS } 2
$$

In the Declarative Operations which follow all constant lengths must be sbsolute.

## DC, DAC, DS, DAS, ONB

These pseudo-operations define storage in exactly the same way as described in the IBM 1620/1710 SPS Manual. The sole difference is that if comments are included without assigning on oddress to the constont and if the assigned address field consists of severol blanks, the processor do

Slanks must not appear in the middle of a numeric constant.
(Define Alphabetic Constant Elogged)
This pseudo-operotion performs the some function os does the DAC, except that alphabetic pairs appear with their high order digits flagged.

DSC, DSS, DSB
These pseudo-operations are not avallable in R-SPS.

## DORG

This pseudo-operation is used as described in the IBM 1620/1710 Manual. Although its operand may be either absolute or relative, it is treated os relative.

## DEND

This pseudo-operation is used to define the end of R-SPS progra : optionally to specify the location at which it is to begin. The beginning address may be eilar to it at lood time whenever this relocating vector wlll be added to it of load time. Whenever this to the specified address or to a $\mathbf{m}_{\mathrm{Hal}} \mathrm{t}$; Branch-tomero" pair. This operation does not cause the orithmetic tables to be included in the object progrom.

## MORG (MOdify ORiGin)

This operation is used to set the next assigned address register to the next larger multiple of the operand. The operand which must appear the next larger multiple of the operand. The oper
must also be absolute, non-negative, and non-zero.

This operation is especially useful for starting tables at even multiples of 10,100 , or 1000 . It should be kept in mind that the relocating vector will. influence the value of the last assigned address at load time.

It is for this operation that automatic divide hardware is required.

LOAD (Punch LOADer)
The R-SPS system employs a relocatable loader which must be called for. The statement:

LOAD $x$
causes the loader to be incorporated in the object deck in such a form that its first digit will be $X$. The operand must be absolute, or may
be omitited. If the operand is omitted the beginning digit of the loader
-6.
ust de supplied from the console typewriter at load time. The operation also causes the odd table to loaded

This feature makes it possible to lood part of the program from a loader at position $X$ and load another part from o loader at a different position Y. It should be remembered, however, that incorporation of a second loader destroys all old values of Relocating Vector and the next Load Address. The loader occuples 1220 digits.

The instruction makes it possible to assemble a program in parts while including enly one loader in the final deck.

RVEC (Set Relocating VECtor)
This instruction is used for specifying the value of the relocating vector at assembly time. The operation

## RVEC 10184

causes location 99 to be filled in with 10284 at load time. This instruction has no effect on the lest assigned address register. The 1000

TABL (Punch TABie)
This instruction, which requires no operand, causes the arithmetic toles to be punched out. The add table is loaded along with the loader but the multioly toble is not; thus if any use is made of the multiply table this cormand must be given.

HED (HEaO)
This instruction is used as in I8M SPS. The heading character may be either alphabetic or numeric.

LINK
The pseudo-op

> LINK A,B,C,D,E,F
is used to pass control at load time from the loader to a program which has either been loaded previously by the loader or to a program originally in core.

The $A$ operand, which may be a relocatable symbol, is the address to which control is to pass. The $B, C, D, E$, and $F$ operonds serve as identification fields, ond are ovailable for use by the user's program.
locations 95-99
locations 90-94
locations 85.89
location 84
$\begin{array}{ll}\text { location } & 84 \\ \text { locations } & 26-30\end{array}$
locations 43-47
locations 48-62

Present Relocating Vector
The memory address into which the next digit of an in-
The struction witi be looded The address to which o branch back to the loader.
$A$ zero
The last assigned address register of the end of poss 1 ,

Uoon filling in these areas, o $B$ to 0 is executed thus transferring control to a type six card at zero. (See Output formet).

This card relocetes the $A$ operond if necessary ond transmits control to the address $A$ via a $B T$ A, $A-1$. After the user has modified any of the above constants which are required, control may be passed back to the loader via a 8 to -89 or 88 instruction.

The single digit at location 84 is a switch which controls whether or not the program following the LINK instruction is to be loaded into core or ignored. If location 84 contains a zero the program following on the other hand location 84 is set to a flagged one the progrom follow the LINK statement down to the next LiNk statement will be ignored by the loader (although the cards will be sequence checked).

B _ F It should be noted that the loader does not relocate the operand's - .

END
This instruction, which also requires no operand, is to define the end of an R-SPS program without halting the loading operation. This in end of an R-SPS program without halting the loading operotion. This loaded as one piece.

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Examples of Use of Processor Instructions
A) This example shows now LiNK might be used to type a progrom name on the console typewriter after the first few cards have been loaded.

B) This progrom shows how LINK could be used to read the relocoting vector for a program from the typewriter.

START
$\begin{array}{ll}\text { LOAD } & \text { SVEC } \\ \text { RVTY } & 1000 \\ \text { WATY } & \text { MESSA } \\ \text { RNTY } & 95 \\ \text { BC4 } & *-36 \\ \text { SF } & 95 \\ \text { CM } & 99, \\ \text { BN } & \text { STA }\end{array}$
MESSA
$\begin{array}{ll}\text { B } & -89, \ldots \text { ( } \mathrm{OR} \text { 8B } \\ \text { DAC }\end{array}$
$\vdots$

Mechine Instructions
Any of the symolic operations in the following table may be used and are trensla:ed es shown. In addition numieric op-codes in the operation field ore trensia:ces shown, In addtion numeric op-cades in the operetion for new operations,

$$
\begin{aligned}
& \text { TON - Turn ON } \\
& \text { TOFF - Turn OFF } \\
& \text { BON }- \text { Branch ON } \\
& \text { BOFF }
\end{aligned}
$$

are included. They are used as switches as explained below.
-9-
It is often convenient to remember opast condition by setting s two way switch to elther a zero or flagged one, ond then testing it at some later time with either a BNF or BD instruction. The use of the four ne instructions is equivalent to the following old instructions.

| TON | ADSW | TDM | ADSW,0 |
| :--- | :--- | :--- | :--- |
| TOFF | ADSW | TDM | ADSW,-1 |
| BON | Z,ADSW | BNF | Z,ADW |
| BOFF | $\mathbf{Z , A D S W}$ | BD | $\mathbf{Z , A D S W}$ |

A symbolic label associated with on instruction is a relative quantity.

The flag operand is used as in IBM SPS with one exception. Blanks may be included in the flag operand to set apart its various ports.

$$
\text { e.g. } 0 \begin{array}{lll}
10
\end{array}
$$

However a pair of characters cannot be connected across a blank.

$$
\begin{array}{llll}
\text { e.g. } & 1 & 1 & 0 \\
1 & \text { is lillegal } & \text { is legal : }
\end{array}
$$

table 1
table of allowable mnenonic opcodes and their 1620 equivalents

| $A$ | 21 | x $\mathrm{x} \times \mathrm{x} \times \mathrm{x}$ | xxxxx |
| :---: | :---: | :---: | :---: |
| AM | 11 | xxxxx | xxxxx |
| B | 49 | x $x$ xxx | xxxxx |
| 81 | 46 | x $\times$ xxx | 01900 |
| 88 | 42 | xxxxx | xxxxx |
| $8{ }^{8} 1$ | 46 | x $x$ xxx | 00100 |
| BC2 | 46 | xxxxx | 00200 |
| 3 C 3 | 46 | x $\times$ xxx | 00300 |
| BC4 | 46 | xxxxx | 00400 |
| BD | 43 | x $x$ x $x$ x | x $\mathrm{x} \times \mathrm{x} \times$ |
| BE | 46 | xxxxx | 01200 |
| BH | 46 | xxxxx | 01100 |
| 81 | 46 | XXXXX | xxxxx |
| BL | 47 | Xxxxx | 01300 |
| BLC | 46 | Xxxx | 00900 |
| BME | 46 | Xxxxx | 01600 |
| BMO | 46 | XxxxX | 01700 |
| 8 N | 47 | xxxxx | 01300 |
| bna | 47 | xxxxx | 01900 |
| BNCI | 47 | xxxxx | 00100 |
| BNC2 | 47 | XXXXX | 00200 |
| BNC3 | 47 | xxxxx | 00300 |
| BNC4 | 47 | xxxxx | 00400 |


| bre | 47 | xxxxx | 01200 |
| :---: | :---: | :---: | :---: |
| SNF | 44 | xxxxx | xxxxx |
| 5 SH | 47 | xxxxx | 01100 |
| BNI | 46 | xxxxx | xxxxx |
| 8NL | 46 | xxxxx | 01300 |
| BnLC | 47 | xxxxx | 00900 |
| BNME | 47 | xXXXX | 01600 |
| bnno | 47 | xxxxx | 01700 |
| BNN | 46 | xxxxx | 01300 |
| SNP | 47. | xXxxx | 01100 |
| BNR | 45 | xxxxx | xxxxx |
| BNRD | 47 | XXXXX | 00600 |
| bnv | 47 | xxxxx | 01400 |
| BNWD | 47 | XXXXX | 00700 |
| BNZ | 47 | xxxxx | 01200 |
| BOFF | 43 | XxXXX | xxxxx |
| 80N | 44 | XxXXX | xxxxx |
| BP | 46 | x $x \times x \times 1$ | 01100 |
| BRD | 46 | XXXXX | 00600 |
| BT | 27 | xxxxx | xxxxx |
| STM | 17 | XXXXX | XxXXX |
| BV | 46 | xxxxx | 01400 |
| EWD | 46 | xxxxX | 00700 |
| BZ | 46 | xxxxx | 01200 |
| c | 24 | xxxxx | xxxxx |
| CF | 33 | x $x \times x \times$ | xxXXX |
| CM | 14 | x $x \times x \times$ | XxxxX |
| D | 29 | XxXXX | XXXXX |
| DM | 19 | XxxXX | Xxxxx |
| DN | 35 | x $x$ xxx | xxxxx |
| DNCD | 35 | XxXXX | 00500 |
| DNTY | 35 | XXXXX | 00100 |
| H | 48 | xxxxx | xxxxx |
| K | 34 | x $x \times x \times$ | XXXXX |
| LD | 28 | x $\times$ x $\times x$ | x xXXx |
| LDM | 18 | XXXXX | XXXXX |
| $\mu$ | 23 | x $x$ xxx | XXXXX |
| MF | 71 | XXXXX | XxXXX |
| MM | 13 | x $x \times x \times x$ | XXXXX |
| NOP | 41 | XXXXX | XXXXX |
| RA | 37 | x $x \times x \times 1$ | XxXxX |
| RACD | 37 | xxxxx | 00500 |
| Raty | 37 | xxxxx | 00100 |
| RCTY | 34 | Xxxxx | 00102 |
| RN | 36 | XXXXX | xxxxx |
| RNCD | 36 | xxxxx | 00500 |
| RNTY | 36 | x $x$ xxx | 00100 |

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| s | 22 | xxxxx | xxxxx |
| :---: | :---: | :---: | :---: |
| SF | 32 | XXXXX | XxXXX |
| SM | 12 | XxXXX | xxxxx |
| SPTY | 34 | XXXXX | 00101 |
| TBTY | 34 | XXXXX | 00108 |
| TD | 25 | xxxxx | xxxxx |
| TOM | 15 | x XXXX | xxxxx |
| TF | 26 | x $x \times x \times$ | xxxxx |
| TFM | 16 | x XXXX | xxxxx |
| TNF | 73 | XXXXX | XXXXX |
| TNS | 72 | Xxxxx | xxxxx |
| toff | 15 | x $x$ xxx | 0000J_F_FLAGGED ONE |
| ton | 15 | x $x$ xxx | 00000 |
| TR | 31 | XXXXX | xxxxx |
| WA | 39 | XXXXX | xxxxx |
| WACD | 39 | x $x \times x \times$ | 00400 |
| wnty | 38 | x xxxx | 00100 |
| WN | 38 | xxxxx | xxxxx |
| \%NCD | 38 | XXXXX | 00400 |
| WATY | 39 | xxxxx | 00100 |
| SK | 34 | xxxxx | x07x1 |
| RDGN | 36 | x xxXx | х07×0 |
| WDGN | 38 | xxxxx | x07x0 |
| CDGN | 36 | x $x$ xxx | $\times 0701$ |
| RTGN | 36 | XXXXX | $\times 0704$ |
| WTGN | 38 | XXXXX | $\times 07 \times 4$ |
| CTGN | 36 | XXXXX | $\times 07 \times 5$ |
| RON | 36 | x $x$ x $x$ x | $\times 0702$ |
| WDN | 38 | XXXXX | $\times 07 \times 2$ |
| CDN | 36 | x $x$ XXX | $\times 07 \times 3$ |
| RTN | 36 | XxXXX | $\times 07 \times 6$ |

## Errors

In the course of assembling a program, various error conditions can arise as lllustrated in the following table.

After encountering on error condition the ossembler types out on error After encountering on error condition the assembler types out an error of the offending statement. The machine then halts.

Depending on the setting of console switches one and two, the error is treated as shown below when the start key is depressed:

Switen 2 on $\qquad$ errors are ignored statements in which errors occur are treated as NOP's.

## - 12 -

If the user elects to NCP on instruction in which on error occurs, the listing of the program contains a comment that the error has occurred in place of the mnenonic instruction.

If switches 1 and 2 are off the assembler expects a corrected statement to be entered from the console typewriter. The statement is read into the cleared input-area. Correct processing con not be assured if more than 80 characters are typed.

If an error in typing is made, the user can recover via console switth 4.

## Additional Errors

Three additional error conditions can occur which are not treated as obove.

1) If the program is loaded in a 20 K machine the comment mMACHINE TOO SMALL" will be typed on the console typewriter. It is not possible to proceed.
2) If the symbol table becomes full the comment "SYMBOL TABLE FULL" will be typed. All following symbols will be checked for multipl definition, but they will not be defined. The comment is typed only once.
3) If at the end of pass 2 the contents of the last assigned address counter do not agree with the contents of that counter os of the end of pass 1, the comment "END CONFLICT" is typed. Processing proceeds after this corment.
table 2
ERROR CODES
DORG operand is missing or zero
DEND or END Operand is negetive
DNB length is illegal
Incorrect card format contains a label
D_0
legal first operond
legal lengh specilication for $D S, D C$ DAS, DAC, or DACF
DAC or DACF length specified will not fit on card
D. 3 Illegal oddress specified for DS, DC, DAS, DAC, or DACF

## - 13

More than one arithmetic sign occurs in a DC More than fifty numeric characters supplied or more characters supplied than specified in O DC, DAC or DACF
Field not blank after record mark in $D C$ and not blonk Nore than 10 terms in a DSA
OSA term includes@ or **
F-1 Non-numeric character in flag operand Flag operand sub terms not in oscending order

Illegal identification operond in LINK
Illegal LINK address
Illegal LOAD address
Illegal RVEC operand
Field contains something in addition to ** or character
Too complicated on expression
Alphabetic symbol contains too many characters or numeric constant contains too many digits Unmatchec operefor or operand
Illegal use of alphabetic symbol
Two operators in a row
Illegal charecter in on operand
Multiply relocatable constant
Leading numeric character followed by alphabetic
character in op-code
valid numeric op-code followed by non-biank characters Op-code not in table
Symbol contains special character or teading numeric character
mbol
Previously defined symbal
Symbol undefined with fult symbol table.

## Operating Procedure

The following list of operations must be performed in order to run _SPS:

1) Loed the R-SPS deck. It is not necessary to clear memory.
2) Press start. If you desire operating procedures to be typed out turn switch 4 on and press start agoin. If you wish to bypass this type-out turn switch 4 off and press start.

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3) The console typewriter asks: "IS SOURCE DECK TO BE STORED ON DISK, TYPE YES OR NO". If you have a disk file and wish to store the source deck on the disk for use during pass 2 , type a YES. . If you do not wish to use this option type NO

The machine then corments mswitch 1 ON TO CHANGE disk WOE". This provides for change in the cose of error in the above operotion.
4) Place the source program in the read hopper and start the reader.
The source program will be read in and processed. If any errors are discovered, they may be treated individually as described in the wlll be typed out.
5) If you desire output on pass 2 turn switch 3 of $f$ and press start. If you desire R-SPS to suppress output turn switeh 3 on and press start.
6a) If the source progrom has been stored on disk during pass 1 , processing for pass 2 will proceed using the stored source stotements.

6b) If the source program was not stored on disk during pass 1 it must be read in agoin during poss 2.
7) If the R-SPS program nas been producing an object deck, near the end of pass 2 the program will type "SWITCH 1 ON FOR SYMBOL and start is pressed. Otherwise the pass is finished, ofter start is depressed and a comment is typed.

Steps 3-5 may be repeated for many source programs without reloading the processor.

For those installations without a disk file steps 3 and 60 may be ignored. They may be eliminated fran the processor by placing a yINUS SIGN in column 1 of the last card.

The object deck which Resps produces will not in general be ready to use until it is compressed. (The compressor punches out the loader).
8) Load the compressor.
9) Enter your object deck and press stort.

The compressor will read the object deck ond produce a compressed deck which may be looded into the mechine.

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Steps 8 and 9 may be repeated for mony object decks without reloeding the compressor.

All decks which are processed or loaded must be in correct sequence If an error in sequence is discovered a typewriter comment will be made. Rearrange the deck in correct order and proceed.

## Output Format

There are six types of output cards as specified by the digits 1-6 in cotumn 76 of each card. They are used as specified below:

1) Card type 1 is used to toad up to five instructions per card into memory. Columns $1-60$ hold the instruction while columns $61-70$ nold a pair of rel-tags (digits which determine the re-
locatability of the various $P$ and $Q$ fields) for each instruction on the card. Each pair of rel-tags pertains to one instruction, the first to the $P$ fietd and the second to the $Q$ field. in all such uses of rel-tags a 2 implies o relotive quantity while a 4 stands for an obsolute quantity. Furthermore, the number of instructions is determined by the number of ret-tag pairs.
2) Type 2 cards are used to specify the next digit into which an instruction will be loaded. The value in columns $1-4$ of the card is stepped by the relocating vector and saved in NEXDIG of the loader.
3) Type 3 cards cause the loader to transfer control to the card itself. Instructions located in columns $0-79$ of the card are hen executed and control is returned to the loader by a branch to 89 indirectly. These cards are used to:
a) load or reset the relocating vector,
b). change the next card check number (see patch cards).
4) Cards with a 4 in column 76 are used to load records of absolute numeric information into memory. They consist of a record of information beginning in column 1 of the card, o beginning address A in memory for the record, a memory address B to preserved during the loading operalion, and a singie ret-tag which determines the relocatability of $A$ and $B$. $A$ is in columns $56-60$, 8 in columns 61-65, and the ret-tag in column 55. This card type is similar to the one used exclusively in sps to load information.
5) This card type is used to load DSA's into core. Up to 10 addresses appear in columns $1-50$ of the cord folliowed by one of items is determined by the number of rel-tags.

- 16 -

6) This final card type is used to process the LINK statement. The card loads the following data into locations $0-72$

$$
\begin{array}{ll}
\text { A } & *+30,99, \text {, THESE INSTRUCTIONS ARE } \\
\text { A } & *+23,99, \text { NOP S IF A ABSOLUTE } \\
\text { BT } & \text { A, A-1 } \\
\text { B } & -89, \text { WIDTH } \\
\text { DSA } & \times 1, \times 2, \times 3, \times 4, \times 5
\end{array}
$$

A return address to the loader is filled in locations 85-89 and location 84 is set to a zero before control is transferred to location zero (see LINK statement).

A 4 digit consecutive card number is found in columns 77-80 of all cards.

## Patch Cards

Various errors in the object deck can be corrected by means of patch cards placed in the compressed deck. These patch cards may be of the form of ony of the six card types specified above.

For example to place an

$$
\text { AM } \quad A, 2,10
$$

in location 1000 relative, where $A$ is 14287 relative, the following two cards could be used.

## 01000 <br> 1114387000-2

$\underbrace{1}$ column 1


These two cards would be incorporated into the patched deck before the last card and the whole deck renumbered.

An olternate procedure to renumbering the deck is to incorporate type. 3 card to change the next card check number located in the
igit of the loader. The following 3 cards would then do the trick


KINGSTON PORTRAN II
FOR THE IBM 1620 DATA PROCESSING SYSTEM

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by:
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J.A.N. Lee, ${ }^{3}$ and D.G. Robinson ${ }^{2}$
by :
ple in the early stages of developing this sys useful ideas on compiler and systems construction. To all those who, in any way, contributed to this venture, the authors extend their heartfelt thanks.

We would like to recognize the following people who made particularly useful contributions to the project:
J.W. Holmes ${ }^{1}$ - for his extremely well written arithmetic and function subroutines which appear, with some modification, in this system.
F.H. Maskiell ${ }^{2}$ - for many helpful suggestions, particularly in the coding and testing of the arithmetic and function subroutines.
C.H. Davidson ${ }^{3} 1620$ Users Group representative on the A.S.A. Fortran II subcommittee, for explaining to us the structure of American Standard Fortran II, and for pointing us in the right direction for exteriding the language.

1. Cooper-Bessemer Corp., Mount Vernon, Ohio.
2. McGraw-Edison Corp., Penn. Trans. Div., Canonsburg, Pa.
3. University of Wisconsin, Madison, Wis.

HISTORY

The writing of compilers seems to be one of the more popular pursuits of the members of the 1620 Users Group. At least six different FORTRAN compilers for the testifies to the enthusiasm and ability of 1620 users and to their very real desire to build the best possible mousetrap.

All previous user-written compilers have accepted variations of the FORTRAN I language, with the exception of the University of Wisconsin FORGO, a load-and-go problems which accepted a somewhat restricted FORTRAN II. To our knowledge, KINGSTON FORTRAN II is the first user-written FORTRAN II for the 1620. We hope that this initial effort will encourage others to tackle the problem and improve on our system in the same way that improvement followed improvement in the user-written FORTRAN I compilers.

The initial impetus for KINGSTON FORTRAN II came in about August 1963, from those of us living in Kingston, Ontario, when we started to find out how UTO FORTRAN Operated, with the intention of providing a suitable
FORTRAN for a 40 K 1620 . It soon became apparent that FORTRAN for a 40 K 1620 It soon became apparent that many useful features of FORTRAN II could be incorporated
at little extra work. Messrs. Lee and Field, authors of at little extra work. Messrs. Lee and Field, authors of
UTO FORTRAN, were approached for ideas and suggestions, the UTO FORTRAN, were approached for ideas and suggestions, the preliminary discussion, it was found that it would be no more work to write a whole new system than to make the desired alterations in UTO FORTRAN.

The basic concepts were conceived in three rather long evening sessions during the October 1963 , 1620 Users Group Meeting in Pittsburgh, Pa. By the end organization and general logic of the compiler were organization and general logic of the compiler were
developed and agreed upon. The various sections wer then allocated to the individuals best qualified to handle them. By the first week in January, the main sections of the compiler had been written and tested and it remained to tie the pieces together in a operating system. This was done in Kingston, Ontario, during lat January, when all 5 authors worked for five days on two identical 40 K l620's (Du Pont of Canada and Queen's University).

We hope that Users with 40 K l620's will find the system useful and easy to operate. We have tried to include every useful idea from other people's efforts so that the system would be as speedy and compact as possible

## The work was divided as follows:

\(\left.$$
\begin{array}{ll}\text { J.A. Field } & \begin{array}{l}\text { - Input/Output statements, DO statements, } \\
\text { input/output subroutines, FORMAT } \\
\text { statement. }\end{array}
$$ <br>
D.A. Jardine \& - Arithmetic and function subroutines, <br>

write-ups and operating manuals.\end{array}\right\}\)| E.S. Lee | - Compilation of arithmetic expressions. |
| :--- | :--- |
| J.A.N. Lee | - Compilation of everything not handled <br> by the other authors. |
| D.G. Robinson | -Symbol table organization, including |
| COMMON, DIMENSION, EQUIVALENCE, TYPE. |  |

COMMON, DIMENSION, EQUIVALENCE, TYPE.

## KINGSTON PORTRAN II

This write-up describes a FORTRAN system for the IBM 1620 equipped with automatic division, indirect addressing, additional instructions (TNS, TNF, MF), card input-output and minimum 40 K memory. It is assumed
that a Model E-8 or larger 407 is available for listing.

The language is that of IBM's FORTRAN II with a rew modifications and a number of additions. For the is at least on speaking terms with the FORTRAN II language.

The compiler for this system batch compiles a source program in one pass, at approximately twice the speed of existing compilers for the 1620. The execution speed of the object program is also approximately twice made to speed up all important parts of the system; in addition, more core storage is available for the object program than existing FORTRAN II compilers allow.
SOURCE PROGRAM CARDS
These are as required for IBM FORTRAN II. Any number of continuation cards are possible, but the statement may not contaln more than

## ARITHMETIC PRECISION

Real numbers: 8 digit mantissa, 2 digit exponent.
Notation 1s excess 50; (1.e. 1.0 5110000000)
Integer numbers: 4 digits, modulo 10000

## VARIABLES

These are as in IBM PORTRAN II, 1 to 6
alphabetic or numeric characters, starting with a letter, Which, for integer variables, must be one of I, J, $K$, $L$, $\mathrm{M}, \mathrm{N}$, unless otherwise specified in a TYPE deciaration. SUBSCRIPTS

A variable with, at the most, two subscripts
appended to it can refer to an element of a one- or twodimensional array. Three dimensional subscripting is not permitted. A subscript may be an expression of any
desired complexity, provided only that the result of the evaluation of the expression be an integer quantity. However, a zero or a negative subscript can be used. To use tris effectively, the programer must know how data areas are laid out in memory. See the operating instructions:

Examples of Subscripts:

```
1
3
\(2+\mathrm{MU}\)
\(2+\mathrm{MU}\)
\(\mathrm{MU}+2\)
\(\mathrm{J} * 5+\mathrm{M}\)
J*5
\(5 * 5\)
6*J-K+2-10/L+M
\(4 * J(K+2-L+M)+K(M(N+2)) / 3\)
\(\operatorname{FIXP}(A * B+3.0 * * \operatorname{SIN}(X))+L / 2\)
```

The variable in a subscript may itself be subscripted, and this process of subscripting may be carried on to any esired depth of subscripting. It can, in fact, be carried what hend the point where the average programmer understands

## UUBCRIPTED VARIABLES

Only singly or doubly subscripted arrays may be defined. The size of these must be specified in a DIMENSION statement.

## EXPRESSIONS

These are defined and organized exactly as in IBM
II. FORTRAN II.

## LIBRARY FUNCTIONS

Ten library (closed) functions are included in the KINGSTON FORTRAN II System. These are listed in Table I.
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TABLE 1

| Punction Definition $\quad$ Fu | Function <br> Name (s) | No. of Arguments | Type Function | Of Argument |
| :---: | :---: | :---: | :---: | :---: |
| Sine of the argument | SIN | 1 | Real | Real |
| Cosine of the argument | COS | 1 | Real | Real |
| Exponential $\left(e^{x}\right)$ of the argument | EXP | 1 | Real | Real |
| Square Root of the argument | nt SQRT | 1 | Real | Real |
| Natural logarithm of the argument | LOG | 1 | Real | Real |
| Arctangent of the argument | ATAN | 1 | Real | Real |
| $\begin{aligned} & \text { Arctangent of }\left(\arg _{1} /\right. \\ & \operatorname{argz}) \end{aligned}$ | ARCTAN | 2 | Real | Real |
| Signum of the argument; $=-1$. for $X<0 .,=0$. for $\mathrm{X}, 0 .,=+1$. for $\mathrm{X}>0$. | SIGNUM | 1 | Real | Real |
| Absolute value of Arg 1 with the sign of Arg ? | SIGN | 2 | Real | Real |
| Choosing the larger value of the two arguments | MAX | 2 | Real | Real |
| Choosing the smaller value of the two arguments | MIN | 2 | Real | Real |

Table 2 lists the open or built-in functions. These are compiled in-line every time the function is referred to.

| TABLE 2 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Function Definition | Function Name | No. of Arguments | Function | Of Argument |
| Absolute value of the argument | $\begin{aligned} & \text { ABS } \\ & \text { ABS } \end{aligned}$ | 1 | Real <br> Integer | Real |
|  |  |  |  | Integer |

Table 3.1ists closed functions which are permanently stored in the machine, whether or not they are mentioned by name in a FORTRAN source program.

| Function <br> Definition | Function <br> Name | No. of <br> Arguments | Function | Type of |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Floating an integer | FLOAT | 1 | Real | Integer |

THE ARITHMETIC STATEMENT
The arithmetic statement is the same as in IBM
FORTRAN II except for the extensions in complexity of evaluation of subscripts.

CONTROL STATEMENTS
FORTRANIS The control statement flexibility in standard FORTRAN's leaves something to be desired, particularly where the program is complex and core storage is at a
premium. These conditions, it might be noted, are the normal ones for almost all, problems. KINGSTON FORTRAN II attempts to improve this situation by expanding the capabilities of the ASSIGN and assigned GO TO statement and by extending the ASSIGN concept to the other control
statements. statements.

ASSIGN STATEMENT
ASSIGN i TO n
In IBM FORTRAN II, the ASSIGN statement is used only in conjunction with an assigned GO TO statement. For instance,

$$
\begin{aligned}
& \text { ASSIGN } 3 \text { TO } \mathrm{J} \\
& \text { GO TO } \mathrm{J},(3,5,9,243)
\end{aligned}
$$

will cause a branch to the statement numbered 3 .
The effect of the ASSIGN statement is to "equate" the non-subscripted integer variable $J$ to statement number 3. The subsequent GO TO J, $(3,5,9,243)$ is then interpreted as GO TO 3.

In KINGSTON FORTRAN II, this concept has been changes, the following definitions are used:

Statement Label - A statement label is the name attached to the memory location containing the first instruction compiled from the statement identified by the label. There are two kinds of statement labels:
 from one to four digits long.

Alphabetic Statement Label - A variable which may

by one or more ASSIGN statements has been equated
to a numeric statement label (statement number).
It is most important to realize the difference between a will place in and an arithmetic variable. ASSIGN compiled from statement number 3. J $=3$ will cause the number 0003 to be placed in $J$. The sequence of statements

## ASSIGN 3 TO J

GO TO J
will cause a branch to statement numbered 3 . However,

$$
J=3
$$

GO TO J
will result in disaster. Moreover,

## ASSIGN 3 TO J

$$
\mathfrak{J}=\boldsymbol{J}+1
$$

GO TO J
will not transfer control to the statement numbered 4 Arithmetic on assigned variables is not permitted; assigned variables are not in any way the same as arithmetic variables except that they may be subscripted and stored in an array They may a

It is possible in KINGSTON FORTRAN II, to equate two alphabetic statement labels by an ASSIGN statement. If the first statement label in the ASSIGN statement is alphabetic, it must be enclosed in parentheses.

The following examples illustrate the ASSIGN statement:
ASSIGN 3 TO N (St. label N is equated to St. label 3)
ASSIGN ( N ) TO J (St. label J is equated to St. label $N$ )
ASSIGN 3 TO $I(K)$ (same as the line above. $K$ must have been defined before this statement and I must be dimensioned).

ASSIGN (I (K)) TO L(3+M/4-M**3)
same as above. The alphabetic statement labels can be subscripted as desired).

Since the primary definition of a statement identifier is its occurrence as a statement number, it is necessary that any iven state ASSIGN statement number. Failure to observe this rule will cause trouble. For example,
$3 \quad A=B$
ASSIGN (J) TO K(I)
is not correct, because $J$ has not been associated with any statement identifier when the ASSIGN statement is executed. However,

$$
\begin{aligned}
3 \quad & \mathrm{~A}=\mathrm{B} \\
& \overline{\mathrm{ASSIGN}} 3 \text { TO } \mathrm{J} \\
& - \\
& \text { ASSIGN } \\
& \text { (J) TO } \mathrm{K}(\mathrm{~L})
\end{aligned}
$$

is correct.
Alphabetic statement labels may be used in the following control statements.

> GO TO (both unconditional and assigned) IF (SENSE SWITCH 1) IF (arithmetic expression) Computed GO TO
phabetic statement labels may not be used in a DO statement

## GO TO STATEMENT

GO TO n unconditional GO TO
GO TO $n,\left(n_{1}, n_{2}, \ldots n_{m}\right)$ assigned GO TO
where $n$ is a statement label. If $n$ is alphabetic, then it must previously have been defined in an ASSIGN statement. The assigned GO TO statement is treated exactly like th optional and will be accepted but ignored by the compiler.

## Computed GO TO Statement

$$
\text { GO TO }\left(n_{1}, n_{2}, n_{3} \cdots-n_{m}\right), 1
$$

where $n_{1}, n_{2}--n_{m}$ are statement labels. If alphabetic they must have been previously defined by ASSIGN statements. 1 is a fixed point (integer) variable or expression. i may be subscripted as desired.

## ARITHMETIC IF STATEMENT

## $\mathrm{IF}(\mathrm{a}) \mathrm{n}_{1}, \mathrm{n}_{2}, \mathrm{n}_{3}$

where a is an integer or real (floating point) expression of any complexity, and $n_{1}, n_{2}, n_{3}$ are statement labels. If alphabetic, $n_{1}, n_{2}, n_{3}$ must have been previously defined in ASSIGN statements.

## IF (SENSE SWITCH) STATEMENT

## IF (SENSE SWITCH i) $\mathrm{n}_{1}, \mathrm{n}_{2}$

where 1 is a one or two digit unsigned integer number or an integer expression, and $n_{1}$, $n_{2}$ are statement labels. If 1 is an integer expression, the low order two digits of the value numbers resulting from this are the numbers of machine indicators, not just console switches.

## THE DO STATEMENT

## DO $n 1=m_{1}, m_{2}, m_{3}$

where $n$ is a statement number, 1 is an unsigned integer
variable which may be subscripted and $m_{1}, m_{2}, m_{3}$ are
variable which may be subscripted and $m_{1}$, mon $m_{3}$ are
complexity, positive or negative, $n$ may not be an
alphabetic' statement label, and i may not be an expres
There are no particular restrictions on mive man particular they $^{\text {may }}$ be positive or negative quantities
If $m_{1}=m_{2}$, the DO will be executed once only. $m_{1}, m_{2}, m_{3}$ should be chosen so that the DO loop terminates. See below sor an example of a never-ending DO-100p.

## Example:

DO $5 \mathrm{~J}=\mathrm{K}+\mathrm{L}-5, \mathrm{M}-\mathrm{I}(\mathrm{JOB}(\mathrm{KK})),-\mathrm{L}$

If $m_{1}, m_{2}, m_{3}$ are expressions, their values are the values of the expressions when the DO statement is encountered at object time, and these values are unaffected by alteration
inside the Do of the values of the variables in the expressions $m_{1}, m_{2}, m_{3}$.

As a result of allowing positive or negative values for $m_{1}, m_{2}, m_{3}$, it is legal to have DO loops which count down. For example,

$$
\text { DO } 3 I=10,1,-1
$$

will cause $I$ to run from 10 to 1 in steps of $(-1)$. The following is also permitted.

$$
\text { DO } 10 \mathrm{~J}=-10,5,2
$$

which will cause $J$ to assume successively the values $-10,-8$, $-6,-4,-2,0,2,4$. If the DO variable assumes zero or negative values, it may be used, with caution, as a subscript knowledge of the layout of data areas in memory as des areas in memory, as described in the operating instructions.

Care should be taken to see that the DO index terminates properly. For instance,

$$
\text { DO } 20 \mathrm{~K}=-10,-1,-2
$$

will increment nearly 5000 times before termination. The same is true of

DO $40 \mathrm{~K}=10,1,2$
Termination in both cases occurs because integer arithmetic is performed modulo 10000

All the restrictions on DO statements currently imposed by IBM FORTRAN II are also in force in KINGSTON FORTRAN, except as already mentioned.

CONTINUE STATEMENT
Same as IBM FORTRAN II.
PAUSE STATEMENT
PAUSE
PAUSE $n$, where $n$ is a fixed point constant, variable or expression.

The typewriter types PAUSE $n$, together with error messages (see operating instructions) and the machine halts. If $n$ is a variable or expression, its current value is typed s no typing. In either case, depression START wili cause resumption of program.

```
STOP STATEMENT
STOP
STOP n, where n is a fixed point constant, variable
                    or expression.
```

The typewriter will type STOP, followed by the
urrent value of $n$. If $n$ is not specified, STOP 0000 will be typed. CALL EXIT is then executed (see operating instructions)

## END STATEMENT

END is an instruction to the compiler that the program is complete. An END statement must be physically the last card of the main line program and of each subprogram which is associated with the job. The END statement results in CALL EXIT except in a sub-program, where it is interpreted as a RETURN statement

## FUNCTION AND SUBPROGRAM STATEMENTS

FUNCTION and SUBPROGRAM statements are the same in KINGSTON FORTRAN as in IBM 1620 FORTRAN II, and the same restrictions apply.

Because the compiler is one-pass, the subprograms are not compiled separately from the main program. See the operating instructions for further details.

## INPUT/OUTPUT STATEMENTS

The INPUT/OUTPUT statements in KINGSTON FORTRAN II are similar to those of IBM FORTRAN II, except that expressions are permitted in certain places in INPUT/OUTPUT 1ists. Indexed ilsts, array names (to handle a whole array) and all other standard FORTRAN II features are allowed. It is not necessary to specify a FORMAT statement number in an I/O statement. If no FORMAT statement number is given, the system. will supply FORMAT ( 5 N ). Sce the description of FORMAT for an explanation of FORMAT (5N).
$-12$

The permitted INPUT/OUTPUT statements are:
READ (card input), ACCEPT TAPE, ACCEPT (input on console typewriter), REREAD (re-reads last input record), PUNCH, typewriter), REREAD (re-reads last input record), PUN printer).

Indexed I/O Lists
As in IBM FORTRAN II, the statement
READ 10, ( $(\mathrm{A}) \mathrm{I}, \mathrm{J}), \mathrm{I}=1,10), \mathrm{J}=1,10$ )
will cause 100 numbers $A(1,1)$ to $A(10,10)$ to be read into array A. Similarly,

$$
\operatorname{READ} 10,((\mathrm{~A}(\mathrm{I}, \mathrm{~J}), \quad \mathrm{I}=\mathrm{K}, \mathrm{~L}), \quad \mathrm{J}=\mathrm{M}, \mathrm{~N})
$$

will cause various elements of $A$ to be read in under the control of the indices $I$ and $J$

In KINGSTON FORTRAN II, the limits on the implied DO's (II=K,L; J=M,N) may be expressions. Furthermore, the names of the input variables may be subscripted to any desired depth. For example:
READ $10,(((A)(\mathrm{I}(\mathrm{Kl}), \mathrm{J}(\mathrm{Ml})), \mathrm{Kl}=\mathrm{K}-\mathrm{JOB} * 2, \mathrm{~L}+5-\mathrm{J} 6), \mathrm{Ml}=\mathrm{M} * 8-\mathrm{MM} 9, \mathrm{~N}-3 * \mathrm{~N} 18$
will be executed as
D0 $\quad 100 \mathrm{Ml}=\mathrm{M} * 8-\mathrm{MM} 9, \mathrm{~N}-3 *$ N18
DO $\quad 100 \mathrm{Kl}=\mathrm{K}-\mathrm{JOB} * 2, \mathrm{~L}+5-\mathrm{J} 6$
100 READ 10, A(I'K1, J(M1))
where $I$ and $J$ are names of one-dimensional arrays which must previously have been defined.

KINGSTON FORTRAN II permits the same kinds of expressions in indexing as are permitted in standard DO statements. The mplied DO in and I/O list may run forward or backward, and may have integer expressions of any desired complexity.

INPUT LISTS
In an input list, the variables may be only simple variables or indexed variables. Input of expressions is meaningless, and not permitted. For example

READ 10, M, Q, $A(I(K+4 * L), M(N-5 * L+4)), B$
is permitted, provided $I, K, L, N$ and $M$ are previously defined. READ 10, $A+B-C(K)$ is not permitted.

## OUTPUT LISTS

Output lists may be fully indexed lists, as
described above. In addition, expressions may appear in the list as output quantities. For example:

PUNCH 20, C*D/(LOGF (X-Y*Z)+10.3), Y, D
will cause

## C*D/LOGF (X-Y*Z)+10.3

to be calculated at the time the punch statement is encountered and its value to be punched, together with the values of $Y$ and D , on a card, according to Format statement 20 . The value of the expression in an output list is lost when it is expression in añ I/O list may be of any desired complexity and may be indexed as required, either by DO statements, or by implied DO statements in the list itself. For exampie:

PUNCH 20, ( ( (C*SQRTF (A (I, J ) )-M(I)), I=1, $L+4,3), J=I+1, K-10,5)$
will cause values of $C * \operatorname{SQRTF}(A(I, J))-M(I)$
to be punched out for values of J from $\mathrm{I}+1$ to $\mathrm{K}-10$ in steps of 5 and values of I from 1 to $\mathrm{L}+4$ in steps of 3 .

## ASSIGNED FORMAT NUMBERS

Format statement numbers may be assigned by ASSIGN statements in the same way any other statement number can. Hence, inpulace of Pormat statement numbers. For statement the following program is permitted:

```
3 FORMAT (5(13,F10.5))
4 FOORMAT (5I5)
    FORMAT (5I7)
    ASSIGN 3 TO J
    ASSIGN 4 TO K(1)
    READ J, (M(I),A(I), I=1,5)
    10 READ K(L), (M4(I), I=1,5)
```

Note that the first statement will be executed according to Format statement 3 , while the second READ statement will be according to Format Statement 5 when $\mathrm{L}=2$.

The subscripted variables in all the above examples must previously have been mentioned in a DIMENSION statement.

## ARRAY NAMES IN I/O LIST

As in IBM FORTRAN II, array names without subscripts may appear in I/O lists. Mention of an array name will statement to be input or output. Two dimensional arrays are handled column-wise -

## $\underset{\text { READ, }}{\operatorname{DIMENSION}} \mathrm{A}(10,10)$

will cause the entire 100 elements of $A$ to be read in, in 5 N notation. The elements of $A$ must be in order $A(1,1), A(2,1)$, $A(3,1), A(4,1), A(5,1), A(6,1)$, etc.

## FORMAT STATEMENTS

Format statements are, in general, equivalent to Format statements allowed in $7090 / 94$ FORTRAN II. $E, F, I$ and A conversion are permitted. Repetition Of 1 equivalent to

```
FORMAT (I2,E12.4,E12.4,E12.4)
```

Parenthetical expression is permitted in order to enable repetition of data fields according to certain Forma specifications within a longer FORMAT statement. The number of repetitions is limited to 99 . Thus,

$$
\text { FORMAT }(2(\text { F10.6,E10.2),I4) }
$$

The level of parenthesizing can be extended to a second level, thus:

> FORMAT $(2(\mathrm{I} 4,2(\mathrm{~F} 6.2, \mathrm{~F} 8.3)))$ is equivalent to
> FORMAT (I4, $\mathrm{F} 6.2, \mathrm{~F} 8.3, \mathrm{~F} 6.2, \mathrm{~F} 8.3, \mathrm{I} 4, \mathrm{~F} 6.2, \mathrm{~F} 8.3, \mathrm{~F} 6.2, \mathrm{~F} 8.3)$

The depth of such nesting of parentheses must not exceed 5 , which appears to be more than would ever be necessary.

## N-Format

Rigid format on input data is not always desirable, and in many cases makes key-punching more difficult.
KINGSTON FORTRAN allows so-called "free form" input, as wel as the more familiar fixed or rigid format. If the FORM statement specifies I, E or F format on input, then the input data record must conform to the normal rules for such (denoting "free form") is used, the data numbers may appear anywhere on the card, and input is controlled by the input list.

N format is used like E, F or I format except that no width or decimal point location digits are required or permitted. For example

> READ 10, I, J, A, C, Z
> 10 FORMAT (5N)
will cause the program to read in a record of 2 integer numbers followed by 3 floating-point numbers. In N format, a number is defined as: any number of leading blanks, followed by a reaningful collection of digits, followed b 1 trailing blank. Note that the blank column immediately following the right-most digit or character of the number is considered part of the number, and serves to delineate the right-hand end of the number.

In the case of $E$ numbers handled with N-format, blanks after the letter $E$ are ignored, and the machine uses the next set of digits as the exponent. For example:

## bl. $2345678 \mathrm{E}-05 \mathrm{~b}$

will be interpreted as . 000012345678 .
The number bl. $2345678 \mathrm{Ebbbbb}-05 \mathrm{~b}$
w11l be interpreted in the same way.
bl. 2345678 Ebbbbl 103
will resuit in an error condition (see operating instructions).

## bl. 2345678 E bb 00005

will be interpreted as 123456.78 . Leading zeros before either the mantissa or exponent are ignored.

An E- type number handled by $N$-format ends with the blank after the exponent digits.

A FORMAT statement may specify $N, E, F, I$ or A format as required, thus allowing both free and rigid format on the same card. Note that, in $N$ format, if a floating point number does not have a decimal point,

Some examples may help:

$$
\text { READ } 10, I, J, A, C, Z
$$

10 FORMAT (5N)
The card might look like:
bbl23bbbbbbl2bbbl6.3bbbbbl. 2E6bl23000bbb etc.
$N$ Format requires only that at least $l$ blank column follow the number. In this case, I, J, A, C, $Z$ would b stored as $123,12,16.3,1.2 \mathrm{E} 06,123000$. resp

READ 11, I, J, A, C, Z
11 FORMAT (I3, I6, N, FlO.3, N)
The Format requires that I, J, C follow rigid format. The card might look like:
bl2bbbl2bbbbbbl20.bbbbl234567bbbl6.8bbb etc.
This would give the following results:

| Variable | Value |
| :---: | :--- |
| I | 12 |
| J | 120 |
| A | 120. |
| Z | 1234.567 |
|  | 16.8 |

Note that the F-specification for C starts on the first column after the blank following 120., (see the position of the arrow) since this blank is considered part of the value of an N-Format number.

An output, $N$ format is equivalent to IPE14.7,1X for floating point numbers, and I5,1X for integer numbers.

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N Format allows repeated format and parenthesizing, and follows the usual rules for them.

If a number is positive, the output under $E, F, I$ or N Format will not contain a leading plus sign. On I Format, no space is left for it, so that it is possible to construct a fully packed output record provided all numbers are positive. N Format generates a space for a + sign and a
space following the number. space following the number.

If a floating point number is output under Iw Format, the integer part of the floating point number is convered to Iw Format. Thus 128342.56 output with Ilo Format would appear as bbbbl28342.

## SCALE FACTORS

To permit more general use of $E$ and $F$ conversion, a scale factor followed by the letter $P$ may precede the
specification. The scale factor is defined such that

Output number $=$ internal number $\times 10^{\text {scale factor }}$ Internal number $=$ input number $\times 10^{\text {-scale }}$ factor
This operates exactly the same as in IBM FORTRAN II for the larger machines. For example
FORMAT (2PF10.4)
used on output will multiply the number by 100 before output On input, it will divide the external number by 100 before storing it in the machine.

On E-Format output, the effect of P-scaling is to shift the decimal point in the mantissa and to adjust the exponent by the amount of the shift.

Thus, if FORMAT(E15.8), used for output, produced the number . $12345678 \mathrm{E}-04$, then FORMAT ( 3 PE15.5) would produce $123.45678 \mathrm{E}-07$ for the same number. Note that for E-Format output. P-scaling does not change the magnitude of the number. It shifts the decimal point, and makes a compensating change in the exponent. For F-Pormat, P-scaling alters the magnitude

## VARIABLE PORMAT

KINGSTON FORIRAN II allows variable Format. That is, Format specifications may be read in at object time. In this way, data may be read in under control of a Format Statement Which itself has been read in, Variable Format statements must be read under A-For

For example:
DIMENSION FMT (15)

$$
\operatorname{READ} 10,(\operatorname{FMT}(I), I=1,14)
$$

10 FORMAT (15A5)
will cause 70 characters of input record (i.e. the Format Statement being read in) to be stored in array FMT. It is then possible to write:

$$
\text { READ FMT, A, } B, X, Z,(A(J), J=1,10)
$$

where the input variables will be read in according to the Format Statement stored in array FMT.

It is also possible to alter array FMT by programming. This should be done with some care, otherwise the Format tatement stored in array FMT may become completely unintelligible.

The name of the variable Format specification must appear in a DIMENSION Statement, even if the Array size is only 1.

The Format read in at object time must take the same form as a source program Format Statement except that the ord Format is omitted, i.e. the variable Format begins with a left parenthesis.

## SPECIFICATION STATEMENTS

## COMMON

Variables, including array names, appearing in COMMON statements will be assigned core storage locations beginning at the high end of memory, and will be stored at object time in descending sequence, 10 digits per variable, or per item of a dimensioned variable, as they are encountered in the COMMON statement. If a variable is a dimensioned variable, the size of the dimensioned array must appear in the COMMON statement, and the variable must not again be dimensioned in a DIMENSION statement. The COMMON Statement must precede EQUIVALENCE or DIMENSION statements program. For example:
COMMON A,B,I,J,X(10,3),Y(5)
(Inclusion of dimensioning information in COMMON statements is allowed in FORTRAN IV).

## DIMENSION

The DIMENSION statement is the same as IBM FORTRAN II except that variables already mentioned in COMMON may not again be dimensioned and that only 2 subscripts are allowed.

$$
\text { DIMENSION } Z(10,5), V(400) \text { is permitted }
$$

DIMENSION $X(10,5,10)$ is not permitted

## EqUIVALENCE

EQUIVALENCE ( $\mathrm{a}, \mathrm{b}, \mathrm{c}, \ldots--$ ), $(\mathrm{d}, \mathrm{e}, \mathrm{f},--),---$
where $a, b, c, d, e, f$, are variable names. KINGSTON FORTRAN imposes some restrictions on EQUIVALENCE statements which are not pesent in IBM FORTRAN II. These are noted below:

1. Single variables may be equivalenced only to single
variables.
2. Arrays may be equivalenced to other arrays, of the same
3. Single variables may not be equivalenced to individual items of arrays, nor may single items of two arrays be equivalenced. In general, no subscripts may appear in
an Equivalence statement.
4. Because the compiler is single pass, it is crucial that
the order in the source deck be:

COMMON (if any), DMMENSION(if any), EQUIVALENCE (if any).

## They must precede the first executable statement of the

 program.5. If arrays are to be equivalenced, the first item only
in the list must have been defined previousiy in a COMMON, or DIMENSION declaration, and the remaining items in the list must not have been so defined. The
Equivalence statement itself defines these remaining items, If single variables are to be equivalenced, and any item in the Equivalence list has been defined in a previous COMON or TYPE statement, it must be first in been defined in a COMMON or TYPE statement. For example,
```
COMMON A,B(10,3),C
IMENSION D(50)
EQUIVALENCE (A,P,G),(D,X)
```

This puts $A$, array $B$, and $C$ in common storage; defines array $D$; defines $F$ and $G$ as single variables in the same
memory iocation as $A$; and defines $X$ as a 50-item vector in the memory location as A; and defines $x$ as a $10 c a t i o n$ as $D$. The following are errors: (in the example above).

| EQUIVALENCE | D,A | (para.1,2) |
| :---: | :---: | :---: |
| EQUIVALENCE | ( $\mathrm{B}(1,1), \mathrm{G})$ | (para. 3) |
| EQUIVALENCE | ( $\mathrm{X}, \mathrm{D}$ ) | (para.5, X not defined |
| EQUIVALENCE | ( $G, A, F)$ | (para.5, G not defined, A defined) |
| IVALENCE | D (50) , X | (para. 3 |

6. To preserve compatibility with other FORTRAN systems which require DIMENSION statements for all array variables in an Equivalence list, KINGSTiON FORTRAN allows extra DIMENSION statements after the Equivalence statements Such DIMENSION statements may be used to mention the equivalenced variables, but since they have already been defined in the Equivalence Statement, the compiler will example:

$$
\begin{aligned}
& \text { DIMENSION X }(10), Y(20) \\
& \text { EQUIVALENCE }(X, A, B),(Y, C, G) \\
& \text { DIMENSION A }(10), \mathrm{B}(10), \mathrm{C}(20), \mathrm{G}(20)
\end{aligned}
$$

is permitted. The variables $A, B, C, G$ in the second DIMENSION statement are ignored by the compiler, because they have already been defined in the preceding EQUIVALENCE statement.
7. It is possible to equivalence items not of the same type or mode: e.g. EQUIVALENCE (A,I) - where A is real and I is integer.

## TYPE

Two TYPE declarations are permitted. These statements
determine the type of variable associated with each variable name appearing in the statement. This TYPE declaration is in effect throughout the program. The two declarations are

$$
\begin{aligned}
& \text { INTEGER } a, \dot{b}, c, \ldots \\
& \text { REAL } a, b, c, \ldots
\end{aligned}
$$

where $a, b, c$, are variable names appearing within the program. Function names may not appear in TYPE declarations.

Rules:-
(1) A variable defined to be of a given type remains of that type throughout the program.
(2) INTEGER indicates that the variables listed are integer, and over-rides the alphabetic naming convention.
(3) REAL indicates that the variables listed are floating point, and over-rides the alphabetic naming convention.

The TYPE declaration must occur before the first executable statement of the program. If any of the variables mentioned in a TYPE declaration are mentioned in a COMMON or DIMENSION statement, the TYPE declaration must follow such mention.

If a TYPE declaration precedes an EQUIVALENCE statement, then it defines a variable in the sense required by the EQUUIVALENCE statement, and all variables equivalenced to the one declared in the TYPE statement will be of the same type.

If a TYPE declaration follows an EQUIVALENCE statement, then only the specific variable names mentioned in the declaration will be affected.

## Examples,

1. INTEGER A

EQUIVALENCE ( $\mathrm{A}, \mathrm{B}, \mathrm{C}$ )
2. ERUIVALENCE (A,B,C)

INTEGER A
3. EQUIVALENCE (A , B,C)

INTEGER A,B,
4. INTEGER A,B,C

ERUIVALENCE ( $\mathrm{A}, \mathrm{B}, \mathrm{C}$ )
Examples 1 and 3 cause $A, B, C$, to be integer variables and occupy the same memory location

Example 2 causes $A$ to be integer, $B, C$ to be real, and $A, B, C$ to occupy the same memory location.

Example 4 is an error in KINGSTON FORTRAN (see para. 5 under EQUIVALENCE).

```
J.A.A. Fleld, }\mp@subsup{}{}{1}\mathrm{ D.A. Jardine,'}\mp@subsup{}{}{2}\mathrm{ E.S. Lee,
```

    J.A.N. Lee, \({ }^{3}\) and D.G. Robinson \({ }^{2}\)
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## KINGSTON PORTRAN II

## OPERATING CONCEPTS

KINGSTON FORTRAN has incorporated in it the ability
to recognize certain control cards both at compile and object time. The control cards recognized by the compiler are, with one exception, instructions to the compiler to execute various options such as symbol table output, compile with or without trace, etc. A list of these and their functions appears later The control cards recognized by the object program are intende and to permit continuous flow of programs through the machine with a minimum of operator intervention. The system will allow stacking of programs in the read hopper and execution of these programs, in the order they are presented to the machine, without requiring button pushing at each program load.

## COMPILER OPERATION

The compiler deck is self-loading and selfidentifying. To load the compiler, push RESET, LOAD. The switch settings are:

$$
\begin{array}{ll}
\text { Par1ty } & \text { - STOP } \\
\text { I/0 } & \text { Program }
\end{array}
$$

Sense Switches - Program used. Position immaterial

Because the 1620 typewriter is prone to write-checks, any errors in its operation are completely ignored. Card I/O read- and write-checks are handled by programming.

The source deck is assembled with the main-line program accompanied by all subprograms in source language. The main-line and subprograms may be in any order. Because of subprogram object loaders, the entire deck is compiled at one time. The job size must be such that the main program and all its subprograms can be accommodated in core at one time. That is, no overlay of subprograms by other subprograma is permitted. This restriction also
exists in IBM 1620 PORTRAN II.

The end of the mainline program and of each subprogram must be indicated by an END statement. Thus a program may contain more than one END statement. A spectal control card is used to indicate the end of the entire job; a job, in this context, means the set of main-line program and all required subprograms.

## Form: Col l-\$, *, or

Col 7 - UNLIST

## ocation in Deck: anywhere

Function: If the typewriter had previously been
typing locations as a result of a
LIST card, the UNLIST card stops it.
Otherwise, the UNLIST card has no
effect.
MAP
Form: $\quad$ Col $1-\$$, *, or $\ddagger$
Col 7 - MAP
Location in deck: anywhere before any END
statement.
Punction: The symbol table for the main program
or subprogram (depending on which END
statement is currently being processed)
is punched on cards when the END
Statement is encountered, provided a
MAP card occurred previously in that card is required for each section of the job for which a symbol table is wanted.
JOB
Form: $\quad \operatorname{Col} 1 \quad-\$, *$, or $\neq$
Col 7-9 - JOB
Col 10-79- any valid information
Location in deck: The JOB card must be the first card of any source deck.
Function: The JOB card informs the compller that what follows is a FORTRAN source program. The compiler will not recognize a source program until a Job card is until it finds one. The JOB card is reproduced (from column 7 onwards) into the object deck so that the object deck is self-identifying when it is loaded.

## END OF JOB

Form: $\quad$ Col $1-\not 又$, *, or $\neq$
COI 7 - EOJ
Location in Deck: The EOJ card must be the last card of any source deck, i.e. must be the last card of the job. It is in fact, the super END card.
Function: The EOJ card informs the compiler that the end of the source deck has been reached. The machine will stop, Pressing start will cause the compile to read cards searching for a JOB card or a LOAD card (q.v.).

LOAD
Form: Col l- $\quad$, *, or $\neq$
COI 7 - LOAD
Location in Deck: following the last EOJ card of the last source deck

Function: Because this is a batch compiler, a control card is needed to inform the compiler that what follows is not a ource deck, but rather a new program to be loaded. When the compller finds a LOAD card, it executes a 1620 load peration on the card immediately following, on the assumption that it program. If it is not, you will be in trouble.
PRESCAN

$$
\text { Form: } \quad \operatorname{col} 1-\ngtr, * \text {, or } \neq
$$

Col 7 - PRESCAN
Location in Deck: anywhere
Function: Inhibits punching of object deck. Error cards are punched if errors are ound. A PRESCAN card may be used in place of a JOB card.

Form: $\quad$ Col $1-\neq$, , or $\neq$
Col 7 - SIZE NNNN9
Location in Deck: Immediately following JOB card, i.e. 2nd card of source deck.

Function: The SIZE card specifies the highest numbered core location which the object program is to occupy. NNNN are any 4 be 1999 if compliing for a 20 K machine on a 40 K machine. It, however, can be any 4 digits whatsoever. If the assignment of this highest memory location is such that the job will not fit, an overlap message will result.

Form: $\quad$ Col $1-\not 又$, , or $\neq$ Col 7 - ORIGIN NNNNN

Location in Deck: Immediately follows SIZE card if one exists. Otherwise it follows the JOB card.

Function: The ORIGIN card specifies the core location in which the first machine language instruction of the compiled program will be placed. NNNNN must be an even number. If not, you choice of SIZE and ORIGIN, the object program can be put almost anywhere in core. In fact, it is possible to specify so little core for the object program that no source program whatsoever will fit in it.
If the origin is not specified by an ORIGIN card, the object program will quite as good as it looks, because, as is common with many computing systems, you may need extra bits and pieces to make things work. See the section on subroutines.

## SUMMARY

To compile a program, load the compiler followed by the source deck. The source deck order is:

JOB card
Main-line program with END card) these may be Subprogram(s) with END card(s) in any orde EOJ card.
If another source deck is to be compiled, make it up in the same way, and stack up in the reader oading program, precede it with a \$LOAD card.

## Symbol Table

If a MAP card occurred in the source deck, a symbol table will have been punched. Because a separate symbol table may be punched for the main program and each object deck and the symbol table. For this reason, the symbol table cards are identified by a particular code on the card. The 407-E8 wiring diagram in this. Write-up will detect which are symbol table cards and print only those, ignoring object program cards. The symbol table is punched 4 symbols per card.

Whether or not a symbol table is punched, the compiler punches 1 blank card following completion of the job. This allows removal of the object deck without using the non-process runout feature on the 1622 . The next deck to be punched will be preceded by the blank card, which must be discarded.

## Error Checking

The KINGSTON FORTRAN compiler has built in provision or checking errors in the source program. Because of the expansions in the language, certain statements which are unacceptable to a normal FORTRAN compiler will, of course, be accepted by the KINGSTON FORTRAN compiler.

All errors will be punched on cards suitable for 407 listing using the panel described in this write-up. The 407 will ignore any object program cards in the deck line number in which it occurred. The errors and their codes are described in Table 1.

## TABLE I

ERRORS AT COMPILE TIME

| Error | Reason |
| :---: | :---: |
| Q1 | Character after Format not ( |
| Q2 | No EOJ card |
| Q3 | Continued Error |
| Q4 | Argument List in Subroutine or Function Declaration not a simple variable. |
| Q5 | Unpaired Parentheses. |
| Q6 | No statement number in Format. |
| Q7 | Unrecognizable. |
| Q8 | Statement exceeds 300 characters. |
| Q9 | Doubly defined St. No. |
| Pl | Incorrect Go To Statement. |
| P2 | Invalid Assign Statement. |
| P3 | Invalid If Statement. |
| P4 | Invalid Computed Go To Statement. |
| P5 | EOJ Card not preceded by an End Card. |
| P6 | Expression in Subr. |
| P7 | Invalid Call. |
| WA | Illegal Operator in Expression is $\$$ or $\odot$. |
| WB | Illegal sequence of operators. |
| WC | Mode Error. |
| WD | OP-VAR-OP Sequence Illegal; Syntax error in Statement. |
| WE | ) not followed by an operator. |
| WF | Invalid operator in subscripting. |
| WH | Number of subscripts does not agree with DIMENSION Statement. |
| WG | Floating Subscript. |
| WJ | Expression Ends in Illegal Character. |
| WS | Invalid expression on left-hand side of Arithmetic Statement. |
| WP | Invalid expression on right-hand side of Arithmetic Statement. |
| WT | One of the tables used in compiling Arithmetic is full; 1.e. Statement is too long. |

Table I (contid)
Error Reason
R1. Incomplete DO or I/O Statement.
R2 Expression in Input List.
R3 Unpaired () in Assigned Format No. Invalid Delimiter in I/O Statement. Invalid Use of () in I/O Statement.
Fl Format too verbose for simple minded compiler or, (before completion of repeating format.
F2 Most likely, invalid format, DO, I/O, or Arithmetic Most likely, invalid format, DO, I/O, or Arithmetic
Statement. If Format, can be: sign that is not of H type; no closing); statement not complete; non permissible character.
F3 More than 5 levels of repeating format Repeated Power Format has more than 49 repeats Field Width is missing in I, A, F, E, Specs A-Width greater than 50
D missing in EW.D or FW.D
Decimal missing in EW.D or FW.D
Non-permissible character.
D greater than W in EW.D or FW.D
Field Width greater t
A-Type has zero field width
ER99 Symbol is more than 6 characters.
ER98 Fixed point number has too many digits.
ER97 Floating point number too big.
ER96 Floating point number too small.
ER95 Symbol table full.
ER94 Symbol which should be a function is not
EBy3 Simple variable in Dimension Statement.
ER92 Dimension IMAX not followed by ) or ,
ER91 Missing ) on Dimension Variable.
ER90 No , between Dimension or Common items
ER89 Unidentified Card.
ER88 First item in Equiv List not in Table.
ER87 Missing or , in Equivalence.
ER86 Number in Equiv Statement.
ER85 Variable Dimensioned Twice.
ER84 Arith. St. Func. Defined Twice.
9.
10.

## OBJECT PROGRAM OPERATION

## 1. Introduction

The permanent subroutines package contains routines which facilitate the handing of multi-part programs and the handiling of multiple data sets for the same program. The routines also have the ability to recognize certain control cards as described below This is not by any means a resident monitor, but it uses some of the simpler concepts involved in monitor systems.

An object program will operate perfectly satisfactorily without referring to the resident supervisor program. If this kind of operation is desired, then the running of the object program is the same as for any other card 1620 FORTRAN. Load the object program, followed by the subroutine deck, followed by the data, and pray.

## 2. Error Messages at Object Time

No method really satisfactory to all people can be devised for handling errors at object time. Some people want every error, however trivial, brought to their attention every time it happens, either by typewriter message or by stopping the machine. Others say monitor and delivering to the programmer a core dump (preferably in binary) together with a cryptic indication as to the possible source of his trouble. Still others assert that no errors should be detected at all, that the machine should run merrily on and that it is up to the programmer to figure out post facto why his answers

The position taken in KINGSTON FORTRAN is that a 40 K 1620 is a littie too expensive to permit unbridled to permit some stopping during the course of debugging a program.

Object time errors are collected in an 18 digit error field located in the permanent subroutines. Digits are inserted in this field to indicate various kinds of errors, and system CALL statements have been included to allow interrogation, typing, and resetting of this error field.

Most errors do not resuit in stopping the machine, and the error is not communicated when it occurs

The error field is also typed out when a PAUSE, STOP or END statement is encountered. The error codes are given in Table 2. If a check digit is zero, the error in question did not occur.

The systems CALL statements for interrogating and using the error field, follow

## CALL EPRT

If the error field contains one or more non-zero digits (1.e. at least one error has occurred) the typewriter types the 18 digit field foilowed by CHECK. If the error field was zero throughout, only the word CHECK is printed. The error field is not reset to zero by atatent of the program.

CALL RESET
The error field is reset to zero. It is not typed out. Control is passed to the next executable statement of the program.

CALL ERRCK (J)
The error field is interrogated. If it is non zero (at least one error has occurred) the integer variable $J$ is set equal to 1 . If no errors have occurred, $J$ is set equal to 2 . The error field is printed out (if non-zero) and reset to zero. Control is

The error field is also typed out by certain supervisor control cards, as described in the next section.

## THE SUPERVISOR

The resident supervisor can recognize 3 kinds of control cards. One of these signals that the following card is the first card of a new job and that a load operation is called for. The other two are used to

## New Program Card

Form : Col $1 \$$
Col 2-80 any alpha numeric information
Location: first card of an object program deck.

Function: . This card informs the object program that a new job is waiting to be loaded If the current object program reads such a card under the misapprehension that it is a data card, the words END OF DATA are typed followed by the word CHECK and the error field (if non-zero). The typewriter then types out the contents of the card, operation to read in the next job.

## End of Block

Form : $\mathrm{Col} 1,2, \$ \$$
Col 3-80-any alphanumeric information
Location: At the end of a block of data
Function: When a card containing $\$ \$$ is read under control of a READ statement, the End of Block Indicator is turned on, and the typewriter types the contents of the Rnd of Block card, followed by the word CHRCK and the error field. (if non-zero) Control is then transferred to the first ent of the program

The End of Block Indicator may be interrogated by calling the End of File or Block subprogram. See below. (The End of Block Indicator is a program switch not a hardware feature).

## End of Pile

## Form: Col $\begin{aligned} & \text { 1,2,3 } \text { Sis8 } \\ & \text { Col } \\ & 4 \text { any alphanumeric information }\end{aligned}$

Location : at the end of a set of blocks of data
Function: When a card containing \$\$\$s is read under control of a READ statement, the End of File Indicator is turned on, and the typewriter types the contents of the End and the error field (if non-zero). Contro is then transferred to the first executable statement of the program.
The End of File Indicator may be interrogated by calling the End of File or Block Subprogram. See below. (The End of le indcator is a program switch, not a hardware feature).

The End of File or Block Subroutine Subprogram (which is built into the system) may be used t interrogate the End of File and End of Block Switches.

$$
\text { CALL EOFB }(J)
$$

The End of File and End of Block indicators are interrogated.
If the End of File Indicator is on, $J$ is set equal to 1 .

If the End of Block Indicator is on, $J$ is set equal to 2. If neither is on, $J$ is set equal to 3 . Both rogation. Control is transferred to the next
executable statement of the program.

## Note on the use of End of File, End of -Block

In a job which is processing data in batches, it is convenient to have some way of telling the computer where the end of a data set is, and also to tell the machine which is the last set of such data.

The end of a set of data is called a "block" in our nomenclature. It may be of variable number of data is the amount of data which is appropriate for the whole job or for a section of it.

Many jobs are set up to process several blocks of data in more or less the same way for each block. It is that the program is informed that no more data exist. The End of File Indicator accomplishes this. In our nomenclature, a "file" is a set of one or more "blocks" of data.

Since reading an End of Block or End of File card returns control to the first executable statement of the program, it, is suggested that this first statement should be

CALL EOFB (J)
followed at a suitable place by a computed GO TO using $J$ as its index.

Two other system subroutine call statements are provided in KINGSTON FORTRAN:

CALL EXIT 66
13.

When this subroutine call is encountered the object
program is stopped and control is passed to the
supervisor. The machine will read cairds until it finds
a new job card. When this is found, the number of cards read before finding the new program card is typed out as BYPASS $N$ where $N$ is the number of cards. The error check field is typed and the new program card is handled in the normal way.

## CALL SKIP

This subroutine call causes interruption of the
 encountered, at which time control is transferred to the first statement of the program. If a new job card is new program will result. In any case, the check field is typed, together with BYPASS $N$ as explained above under CALL EXIT.

CALL SKIP will usually be employed to stop calculation on a block of data because of an abnormal ituation (e.g. failure to converge on an iteration bad data) which has occurred in the block of data. In such a case, CALL SKIP will cause that particular alculation to be abandoned, and a new set of data to be presented to the program.

CALL EXIT and CALL SKIP may also result from certain object time error conditions. See Table 2 .

Certain input-output errors are also detected at object time. If one of these is encountered, the ypewriter will type the words I/O ERROR, followed by igit. A list of these errors is shown in Table III.

Object Time Errors

| Position <br> in Error Field | Digit | Meaning | Action Taken (FAC = Accumulator = Result Field) |
| :---: | :---: | :---: | :---: |
| lst digit | 1 | Floating Point Underflow | FAC $=0000000000$ |
| 2nd | 2 | Floating Point Overfiow | FAC $= \pm 9999999999$ |
| 3 rd | 3 | Floating Point Divide by Zero | FAC $= \pm 9999999999$ |
| 4 th | 4 | Fixed Point Divide by Zero | FAC is unchanged, i.e. $\mathrm{J} / \mathrm{O} \equiv \mathrm{J}$ |
| 5 th | 5 | Square Root of Neg. Number | Square root of absolute value of arg. |
| $a^{6 \operatorname{th}}$ |  | Log of zero or Neg.Number | $\log (0) \equiv-9999999999$; otherwise log of abs. value of arg. |
| 7 th | 7 | Sin or cos, arg. $>10^{8}$ | CALL EXIT |
| 8 th | 8 | $\operatorname{Exp}(\mathrm{x})$ out of range | FAC $= \pm 9999999999$ |
| 9 th | 9 | Input number too small | The number entered memory as 0000000000 |
| 10th | 1 | Input number too big | The number entered memory as $\pm 9999999999$ |
| 11 th 12 13 | $\left.\begin{array}{l}2 \\ 3 \\ 4\end{array}\right)$ |  |  |
| 14 | 5 6 | Unused. Available for user-defined relocatable |  |
| 16 | 7 | subprograms. |  |
| 17 18 | 8 9 |  |  |

TABLE 3
I/O Errors at Object Time

| $\begin{gathered} \text { I/O } \\ \text { Error } \end{gathered}$ | Reason | Result |
| :---: | :---: | :---: |
| 0 | Input record from $T / W$ or paper tape over 120 characters long | CALL EXIT |
| 1 | Non-alphabetic data on A-type output | CALL EXIT |
| 2 | Field Width too small on I, E, F, output | CALL SKIP |
| 3 | Invalid character on input data on I, E, F, or N Format | CALL SKIP |
| 4 | Read in integer with E, F, or N Format and has lost right-hand end digits | CALL SKIP |
| 5 | Input-Output list with no numeric specifications between last openingclosing parenthesis pair in Format statement | CALL EXIT |
| $\wedge^{6}$ | Format requires more than 120 characters in a record | CALL EXIT |
| 07 | Write-check occurred 3 times when attempting to punch output or trace card | CALL EXIT $\stackrel{-}{\square}$ |
| $1 F$ | Error in Variable Format - similar to error Fl at compile time | CALL SKIP |
| 2 F | Ditto - similar to error F2 at compile time | CALL SKIP |
| 3 F | Ditto - similar to error F3 at compile time | CALL SKIP |
| $\begin{array}{ll} \text { READ } & 1 \\ \text { READ } & 3 \\ \text { READ } & 5 \end{array}$ | Read check on T/W   <br> " " " " paper tape  <br> $"$ $"$ $"$ cards | Computer halts. <br> When start is pressed, the machine will attempt to read the record again |

16. 

## MEMORY ALLOCATION AT OBJECT TIME

All constants and variables are stored in 10 digit words. The address of the low order digit ends always in 9 Hence the address, of the high order digit ends in 0 .

```
SIMPLE VARIABLES
Real Variables - }10\mathrm{ digits, low order digit address ends
    in }9
Integer Variables - 4 digits, low order digit address ends in
Real Constants - same as real variables.
Integer Constants - In the rare cases that fixed point
    constants are stored in the object program,
    both the negative and positive value of
    the constant are stored. The positive
    value occupies the low order 4 digits of
    the 10 digit word; the negative value has
    ts low-order digit address ending in
    The other 2 cores are unused.
    e.g. 012 34 4 5 % 7 8 % %
        0567805678
    This illustrates storage of }567
A-Format Words - are stored in a lo digit field, the low
    are stored in a 10 digit field, the low
    digit at the high order address (ending
    in 0) is flagged.
```


## ARRAYS

## Vectors-

Matrices -
two dimensional arrays. Matrices are stored starting with the first element, (1,1), stored at the highest numbered wise at progressively lower numbered addresses: $B(1,1), B(2,1), B(3,1)$ etc. The address of $B$ ) $\mathrm{I}, \mathrm{J}$ ) may be calculated from:
Address of $B(I, J)=$ Address of $B(0,0)-10$ ( J*IMAX +I )
where the address of $B(0,0)$ is called the base of $B$. IMAX is the maximum number of ows in $B$ as specified in the DIMENSION
statement
Note that:
The address of $B(0,0)=$ address of $B(1,1)+10$ (IMAX+1)
Negative or zero subscripts on a matrix will work properly on the second subscript, but not on the first subscript. For instance, if $B$ is dimensioned $\dot{B}(3,3)$, then (, 1 ) and $B(0,2)$ will be in the same undesirable. However, $B(2,0)$ will te stored in the second item before $B(1,1)$
An example of a memory layout may help. Suppose the program has the following COMMON statement:

COMMON X, $\mathrm{A}(4)$, $\mathrm{B}(2,3)$
The layout of memory is:

| Variable | Memory Location (low order digit) |
| :---: | :---: |
| X | 39999 (Base of A) |
| A (1) | 89 (Base ${ }^{\text {OT }}$ ) |
| A (2) | 79 (Base of B) |
| A (3) | 69 (вая |
| A (4) | 59 |
| $\mathrm{B}(1,1)$ | 49 |
| B $(2,1)$ | 39 |
| B $(1,2)$ | 27 |
| B $(2,2)$ | 19 |
| B ( 1,3 ) | 09 |
| B $(2,3)$ | 39899 |

The address of the statement is stored in a 5 digit field, which is referred to indirectly. Two such 5 digit
fields are contained in a 10 digit word, whose low order address ends in 9.

## SUBPROGRAM ADDRESSES

FORTRAN subprograms or arithmetic statement functions require two 5 digit addresses for their entry points. These are stored in a 10 digit word whose low order address ends in 9.

## TEAPORARY ACCOMULATORS

(1) 10-digit accumulators may be required during the evaluation of an arithmetic expression, These are
treated exactly like storage for simple variables.
(2) 5-digit accumulators are used in subscripting calculations 5-digit accumulators are used in subscripting
Two of these are stored per 10 digit word.

No provision is made for reproducing the subroutine deck into the object program. It is the opinion of the writers of KINGSTON FORTRAN II that the 1620 should not be that reason it is required that the subroutine deck be placed behind the object deck when loading. If a condensed program is desired, use a suitable core-dump-and-reload program.

The subroutine deck consists of 3 parts, which are, In order: (a) the relocator, which handles the loading of the relocatable subprogram (as requested by the object which consist of the library function subprograms (sin, cos, exp, etc.), parts of the input-output subroutines and any subroutine subprograms which the user may wish to write; (c) the permanent subroutines containing the programmed floating-point arithmetic routines, the fixed point routines, the supervisor, the trace routine, and a hard cord of the input-output routines.

These three sections are essentially independent. The relocator is a completely separate program which uses information contributed by the object deck (memory size, subprograms desired, where empty space is available for those subprograms, etc.) to select and load into core storage the
relocatable subprograms needed for the job.

In a small machine, like the 1620 , it is essential to conserve memory space. For this reason, the inputto conserve memory space. For this reason, the inputtreated like any other relocatable routines. For instance, if the object program does not use A-specification, the routine to handle this will not be loaded into core. Thus, only the input-output routines needed by the object program will be loaded.

The question arises, how far should this be carried. About 2000 cores of input-output routine are used by all other input-output routines, and these are for exponentiation, floating and integer, and for integer division were made relocatable. All others are part of the permanent package. Some consideration was given to making the trace routine ( 300 cores) relocatable. This was rejected on the grounds that any program which fits this can be assured is to have the trace routine permanently in place.
20.

The permanent subroutines are a self-contained deck Independent of the relocator. This deck is so programmed that after loading, control is transferred to the core location containing the first machine language instruction of the object program

A list of the relocatable subprograms is given in Table II.

RELOCATABLE SUBPROGRAMS
User-defined-relccatable-subprograms (abbreviated UDRS) may be of several types, depending on the coding generated by the compiler when the subprogram name is encountered in a FORTRAN source statement. The generated coding is controlled by the makeup of cards placed at the compiler what subprograms aro available and also supply auxiliary information about them.

Each entry on a trailer card consists of a two digit subprogram number, followed by the subprogram name (six characters maximum) followed by a 3 digit code number enclosed in parentheses. A typical entry has the form:

```
NNXXXXXXX(n}\mp@subsup{n}{1}{}\mp@subsup{\textrm{n}}{2}{}\mp@subsup{\textrm{n}}{3}{}
```

where $N N$ is a two digit number unflagged).
XXXXXXX is a 1 to 6 charaster name
$n_{1} n_{2} n_{3}$ is a 3 digit code which describes the subprogram properties to the compiler

NN is any two digit number between 01 and 66.
XXXXXXX is any name beginning with a letter. It does not have to end in $F$ and its starting letter is independent of the function mode; e.g. integer
functions do not have to begin with $\mathrm{I}, \mathrm{J}, \mathrm{K}, \mathrm{L}$, functions
$n_{1} n_{2} n_{3}$ is made up as follows: $n_{1} n_{2}$ form a two digit number is made up as follows: $\mathrm{n}_{1} \mathrm{n}_{2}$ form a two digit numb
controlling the coding gererated by the complier; controlling the coding gererated by the compile describes this.

SVECT is a location in a subprogram transfer vector located in the permanent subroutines. This vector contains the relocated address of the subprogram, as explained below.
21.

| TABLE I |  |  |  |
| :---: | :---: | :---: | :---: |
| $\begin{aligned} & \text { Digits } \\ & \mathrm{n}_{1} \mathrm{n}_{2} \\ & \hline \end{aligned}$ | ```Coding Generated``` |  | Use and Notes |
| 10 | $\begin{aligned} & \mathrm{TF} \\ & \mathrm{BTM} \end{aligned}$ | B, FFAC, ARG <br> -SVECT,*+12 | Single arg. UDRS which may internally branch and transmit |
| 20 | $\begin{gathered} \begin{array}{c} \mathrm{BT} \\ \mathrm{BT} \\ \vdots \\ \vdots \\ \mathrm{BT} \end{array} \end{gathered}$ | $\begin{aligned} & \text {-SVECT, ARG } \\ & \text {-SVECT, ARG } \\ & \vdots \vdots \\ & \vdots \\ & \text {-SVECT , ARG1 } \end{aligned}$ | Multi-argument, single entry UDRS. If one of the arguments is already in B,FFAC when the UDRS is called, it will not be transmitted by a BT-SVECT,ARG. If one of the arguments is not already in B\$FAC, then $A R G$ is placed in B\$FAC and $\mathrm{ARG}_{\mathrm{k}-\mathrm{t}}$ to $\mathrm{ARG}_{1}$ are transmitted through SVECT. This type of entry is designed for functions like MAX and MIN. |
| 25 | BT | -SVECT, ARG | Single argument UDRS which may not internally branch and transmit |
| 30 | $\begin{gathered} \mathrm{TF} \\ \mathrm{BT} \\ \vdots \\ \mathrm{BT} \\ \mathrm{BT} \end{gathered}$ | BSFAC, ARG ${ }_{k}$ -SVECT,ARG $k$ <br> -SVECT, ARGg <br> -SVECT, $\mathrm{ARG}_{1}$ | Similar to $n_{1} n_{2}=20$ above, where $A R G_{k}$ is forced into BSFAC |
| 35 | $\begin{gathered} \text { BTM } \\ \vdots \\ \text { BTM } \\ \text { BTM } \end{gathered}$ |  | A UDRS which may have any number of arguments (including no arguments at all) and which may branch and transmit internally, and which does not have any of its arguments in B\$FAC when entered. This entry is required if the UDRS is to be used as a subroutine subprogram. |

If $n_{1}$ is flagged, the UDRS is expected to produce a floating point result. If $n_{1}$ is not flagged, the UDRS is expected to produce an integer result
$\mathrm{n}_{3}$ can have 3 possible values:
$\overline{0} \quad$ denotes an even function, i.e. $f(x)=f(-x)$; used only
for single arg. functions
1 denotes an odd function, i.e. $f(x)=-f(-x)$; used only
for single arg. functions.
0 denotes a function which is neither odd nor even.
22.

If in doubt, set $n_{s}=0$, which will never cause trouble. (Certain economies at object time are possible
if the compiler knows whether the function is odd or even).

A UDRS may be used as an arithmetic function or as a subroutine subprogram. If a UDRS is called as the result of the appearance of its name in FORTRAN arithmetic statement or expression, it will be compiled as if it wer a function; that is, it must have a single number for a result, and this result must be left in Bgrac on exit fron the UDRS.

However, if the UDRS is used as a subroutine subprogram 1 ts name must appear in a FORTRAN CALL statement In this case, more than one result can be generated, and these are transmitted back to the calling program by the Cormal parameter list or through COMMON storage. The only permissible $n_{1} n_{2}$ for this case is 35 .

The same subprogram may be given several names. All that is necessary is to construct several entries in the trailer card using the same subprogram number and code igits, but different names. Entries on the trailer car must be packed with no blanks. After the last entry on each card, a single record mark ( $0-2-8$ ) is placed. After are placed.
For example, a trailer card might look like:

## 5BLAP ( 100 ) 05BLAPF ( 1000 ) $10 G U R K$ (200) 18A (15I) 10RUNCH (200

10FLAPF (200)
The code digits have been described above
Subprogram 05 is known by the names BLAP and BLAPF,
subprogram 10 by GURK,RUNCH and FLAPF, and subprogram 18 as A.

As many trailer cards as necessary are constructed and placed after the compiler deck. They should be inserted between the second and thes of the system relocatables; the last card contains two record marks at the end of its entries (see above).

## PROGRAMMING RELOCATABLE SUBPROGRAMS

UDRS are to be coded and assembled using either IBM 1620/1710 SPS II or AFIT SPS. To aid in understanding the process of adding ator behaviour follows.
23.

The relocator will relocate all addresses of 8000 or more. Thus subprograms are preceded with a DORG 80000 instruction. Any address below 80000 will not be relocated relocated; however a constant (defined by DC, DSC, DAC) or a DSA will be relocated only if its location is at or above 80000. Furthermore, the constant assembled from a DSA will have both its value and its location relocated if they lie at or above 80000 and provided also that it occurs before the first executable instruction of the subprogram This will become clearer later.

The compiler constructs entry commands to the subprogram as described previously. Note that the user can force compilation of instructions (in the object program) which culminate with BTM -SVECT,*+12. Since this case, the UDRS has a real 5-digit return address by branching indirectly to this 5 digit address. This allows the user to employ BT and BTM instructions In his own subprogram. This feature permits direct access relocatable subprograms. It is also possible for a UDRS to call other relocatables, even though the FORTRAN source program does not require them directly.

Linkage to the relocated subprogram is provided by a transfer vector located in the permanent subroutine package. It is defined by a DSB in the permanent package decks. There is thus no reason for the user to concern himself with absolute addresses, since each UDRS will b compiled with the aid of the permanent subroutines source deck.

The user must specify certain information, in
SPS, before the coding of his UDRS. This information becomes the header cards used by the relocator to select and relocate the subprogram properly.

For functions entered by BT -SVECT, ARG, the coding must look like:

| DORG | 0 |
| :--- | :--- |
| DC | 2, NN |
| DC | 2, II |
| DC | $2, J J$ |
| DC | 2, KK |
| - | -- |
| DORG | - |
| B\$SVECT $-9+5 * N N$ |  |
| DSA | START, 99999, NXX-80001 |
| DORG | 80000 |
| DS | 10 |

24. 

START function coding

N NXX
DAS
DEND

The list of DC's at the beginning define the subprogram number NN, followed by the numbers II, JJ, KK, etc. of the relocatabie subprograms required by this subprogram. These constants must be preceded by a DORG 0 (zero); the relocator identifies them as subprogram numbers by this fact. A subprogram may call a limit of 29 other subprograms, i.e. there may be a maximum of 30 DC 's in this list.

The next item is a DORG to the proper place in the transfer vector BgSVECT, followed by a DSA list. The first item in this ilst is the address of the first executed list must be 99999. The next item is constructed such that it will assemble to a 5 digit number which is the size of the subprogram. Note that NXX (or other suitable label) is a DAS 1 which must appear just before the DEND statement of the subprogram. Obviousiy NXX-80001 will be an even number and will be the number of digits occupied by the subprogram a DSA 99999 is the subroutine size.
by DORG 80000 .
In the case of multiple argument subprograms, two entries in the transfer vector are necessary. The subprogram arguments are transmitted through vector location arguments are transmitted through vin $+5{ }^{\text {min }}$, where NN is the subprogram number; the return address is transmitted through BgSVECT -9+5*NN. The programmer must provide coding to handle the argument and return address as they are transmitted. For such a subprogram, two DSA's for
programmed. For example,

| DORG | 0 |
| :--- | :--- |
| DC | 2, MM |
| DORG | BSSVECT $-9+5$ *MM |
| DSA | START, SOAK, 99999, NY -80001 |
| DORG | 80000 |

SOAK
START -

NY DAS 1

In such a case, SOAK is the entry for coding to handle argument addresses, and START is the beginning of the multi-argument subprogram.

MM is the 2-digit subprogram number. Note that the two entries in the transfer vector must be contiguous, and that the first one may not be used for any other subprogram. Thus, if MM is the number of this subprogram, MM+1 may not be used as the number of any other subprogram since the transfer vector location which it needs has
already been used by multiple argument subprogram MM.

For example, let us program a subprogram to calculate the hyperbolic sine of a floating point argument by the well known formula

$$
\operatorname{SINH}(x)=\frac{1}{2}\left(e^{x}-e^{-x}\right)
$$

To do this we will need the exponential routine, subprogram number 69 and we will use the floating subtract and multiply routines

| HEAD K |  |
| :---: | :---: |
| HYPER | LIC SINE OF X, SUBPROGRAM NO: 12 |
| DORG | 0 |
| DC | 2,12 |
| DC | 2,69 |
| DORG | B¢SVECT-9+5*12 |
| DSA | SINH, 99999,N12-80001 |
| DORG | 80000 |
| DS |  |
| TF | BIN2,B\$FAC |
| BT | B, |
| TF | BIN1, B\$FAC |
| TF | B\$FAC, BIN2 |
| BT | B\$RVSGN, B\$RVSGN-1 |
| BT | B\$SVECT-5+5*69,B\$FAC, 6 |
| BT | B, FFSBR, BIN2 |
| BT | B, ¢FMP, FLHAF |
| B | SINH-1, ,6 |
| DORG | *-3 |
| DC | 10,5050000000 |
| DS | 10 |
| DS | 10 |
| DAS | 1 |
| DEND |  |

## Several points should be noted

(1) This is an example only. Much better methods for SINH (X) exist.
(2) A UDRS must be headed. DO NOT USE HEADING CHARACTERS B NOR S. These are already used in the permanent subprograms.
(3) The first DC defines this subprogram as number 12. The second DS causes the relocator to load in Table II for a list of systems relocatables). (see
(4) The next DORG and DSA define the transfer vector entry and the subprogram length.
(5) Since this subprogram calls other subprograms, it will be entered by having the argument in BSFAC, and The compller trailer card entry would be:
I2SINH (IOO)
(6) The coding for the subprogram follows directly. The first instruction saves the argument $x$, the second result away. We then reverse sign of $x$ in the nex two instructions, and calculate $e^{-x}$.
The two exponentials are then subtracted, and multiplied by 0.5 . The result remains in ByFAC, and the subprogram branches indirectly to the re
the subprogram.

A special method must be used to handle DSA's which are used internally in a UDRS. A DSA used internally must have both its value and itslocation adjusted by the relocator. A true constant, defined by a DSC, DC or DAC, must have its location adjusted but its value left unchanged. Unfortunately In a condensed deck prepared by IBM $1620 / 1710$ SPS II, a DSA following rules must be observed.

RULE 1: Any DSA which is local to the subprogram and which is to have both its location and its value adjusted by the relocator, must be defined after the DORG 80000 statement and before the first instruction of the subprogram.
RULE 2: Any constant which is local to the subprogram and Wich is to have only its location adjusted by the relocator must be defined after the first instruction of the subprogram For example


The DSA Al, A2, A3, will be adjusted as required, because it occurs before the first instruction which in this case is location adjusted, but their value unchanged, because their occur after the first instruction.

## ASSEMBLY OF A UDRS

it behind the source deck for the as described above. Place Using IBM 1620/1710 SPS II, or AFIT SPS, put this combine source deck through Pass I of the assembly in the normal way For PASS II of the assembly, read in only the source deck for the UDRS; it is not necessary to read in the source deck of the permanent subprograms for Pass I. Get a condensed object deck for the UDRS. Throw away the first two and last seven cards of this deck. What remains is the subprogram coding

The UDRS condensed deck is to be inserted in the
The UDRS must be located physically in front of any subprogram
Will result when loading an object deck (see operating
instructions). Obviously the relocator cannot load a
instructions) Obviously the relocator cannot load a subprogram which it has already bypassed before the calling
subprogram appeared.

| Subprogram Number | Length of Subprogram | Sub.called by this Sub. | Entry to Subprogram ${ }^{1}$ | Purpose of Subprogram |
| :---: | :---: | :---: | :---: | :---: |
| 67 | 0 | 68 | BT -SVECT, ARG | Trigonometric COSINE of argument |
| 68 | 694 |  | BT -SVECT,ARG | Trigonometric Sine of argument |
| 96 | 132 | 69,70 | BT -B¢EXP¢3, ${ }^{\text {a }}$ | Reverse Float-Float Exponentiation A**FAC $\rightarrow$ FAC |
|  |  |  | BT -B¢EXP¢4, B | Float-Float Exponentiation FAC**B $\rightarrow$ FAC |
| 69 | 528 |  | BT -SVECT,ARG | Exponential function of argument, Exp (arg) |
| 70 | 578 |  | BT -SVECT,ARG | Natural logarithm of argument |
| 71 | 308 |  | BT - SVECT,ARG | Square Root of argument |
| 72 | 866 |  | BT -SVECT,*+12 | Arctangent of argument; arg. in B\$FAC |
| 76 | 54 |  | BT -SVECT, ARG | Signum of Arg; Argument: $\begin{aligned} &>0 \\ &=0 \text { Result: }+1 . \\ & 0\end{aligned}$. |
|  |  |  |  | <0 -1. |
| 74 | 304 |  | BT -SVECT, ARG | Random number generator; see spec.description |
| 77 |  |  |  | Larger of ( $\arg _{1}, \operatorname{argrg}_{\text {) }}$ ) |
| 78 |  |  |  | Smaller of ( $\mathrm{arg}_{1}, \mathrm{arg}_{2}$ ) |
| 73 |  | 72 |  | Arctangent of (argi/arga) |
| 75 |  |  |  | Sign of $\arg _{1}, \arg \mathrm{~g}$. Magnitude of arg. with the $\mathrm{N}_{\infty}^{N}$ sign of arg2. |
| 79 | 1048 |  | Special | Input of $\mathrm{E}, \mathrm{F}, \mathrm{I}$, or N -type numbers |
| $00^{80}$ | 1056 |  | Special | Output of E,F,I, or $N$ type numbers |
| ${ }^{\infty} 81$ | 124 |  | Special | Routine to handle Hollerith Fields |
| N2 | 100 |  | Special | Routine to handle I/O implied DO's |
| 83 | 104 | 84 | Special | Routine to handle I/O of arrays (formal) |
| 84 85 | 68 |  |  | Routine to handle I/O of arrays |
| 85 86 | 156 | 92 | Special | I/O subscripting routine for $A(I, J)$ |
| 87 | 74 |  | Special | Accept Type |
| 88 | 436 |  | Special | Print (on-line) |
| 89 | 122 | 92 | Special | Accept tape |
| 90 | 130 |  | Special | Punch tape |
| 91 | 268 |  | Special | Reread |
| 92 | 64 |  | Special | Snip (part of Accept and Accept Tape) |
| 93 | 1794 | 94,95 | Special | Variable Format |
| 94 | 180 |  | Special | Routine to handle repeated, parenthesized, Format |
| 95 | 176 |  | Special | Routine to handle A-type numbers |
| 97 | 188 |  | BT -B¢EXPø1, ${ }^{\text {a }}$ | Reverse Float-Fixed Exponentiation, ${ }^{* * * F A C \rightarrow F A C}$ |
|  |  |  | BT -BSEXP¢2, I | Float-Fixed Exponentiation, FAC**I $\rightarrow$ FAC |
| 98 | 226 |  | BT -BSEXP ${ }^{\text {5 }}$, I | Reverse Fixed-Fixed Exponentiation, ${ }^{* * * F A C \rightarrow F A C}$ |
|  |  |  |  | Fixed-Fixed Exponentiation FAC**I $\rightarrow$ FAC |
| 99 | 122 |  | $\begin{aligned} & \mathrm{BT}-\mathrm{B}, \mathrm{DD1}, \mathrm{I} \\ & \mathrm{BT}-\mathrm{B}, \mathrm{DD} 2, \mathrm{~J} \end{aligned}$ | Reverse integer division I/FAC $\rightarrow$ FAC Integer division FAC/J $\Rightarrow$ FAC |

1 SVECT is the location in the transfer vector which contains the link address for the subprogram.
Its exact position is BSVECT$-5+5 * N N$, where NN is the subprogram number

TABLE III
Permanent Subroutines

| Routine | Purpose | Symbolic Address |  | Entry to Subroutine |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Floating Add | $\mathrm{FAC}+\mathrm{A} \rightarrow \mathrm{FAC}$ | B\%FAD | BT | BSFAD, A |  |
| Floating Subtract | FAC-A $\rightarrow$ FAC | B\$FSB | BT | B¢FSB, A |  |
| Reverse Floating Subtract | A - FAC $\rightarrow$ FAC | B,FFSBR | BT | B\$FSBR, A |  |
| Fioating Multiply | FAC*A FAC | B\%FMP | BT | B\$FMP, A |  |
| Floating Divide | $\mathrm{FAC} / \mathrm{A} \rightarrow \mathrm{FAC}$ | B\$FDV | BT | B\$FDV,A |  |
| Reverse Floating Divide | A/FAC $\rightarrow$ FAC | B\%FDVR | BT | B\$FDVR, A |  |
| Reverse Fixed Subtract | I-FAC $\rightarrow$ FAC | BדFFXSR | BT | B\$FXSR, I |  |
| Fixed Multiply | FAC* $\rightarrow$ FAC | B\$FXM | BT | B ¢FXM, I |  |
| Reverse Sign | $-\mathrm{FAC} \rightarrow \mathrm{FAC}$ | B\$RVSGN | BT |  |  |
| Float | $(\mathrm{A}=\mathrm{I}) \rightarrow \mathrm{FAC}$ | B, \%FLOAT | BT | B\$FLOAT, I |  |
| Fix | $(\mathrm{I}=\mathrm{A}) \rightarrow \mathrm{FAC}$ | BSFIX | BT | B\$FIX, A |  |
| Zero Accumulator | Floating Zero $\rightarrow$ FAC | B\$¢ZERFC | BT | B\$ZERFC, B $¢$ SERFC-1 |  |
| Fo(sets error code) | $\pm \underset{\rightarrow F A C}{\text { Floating }}$ nines | B\%ER9 | BT | B/SER9, B/dER9-1 (sign of answer | $\bigcirc$ |
| ${ }_{W}^{(s e t s}$ error code) | $\rightarrow$ FAC |  |  | must be in location 00099) |  |
| Floating underflow | Floating zero $\rightarrow$ FAC | $B \$$ SRRø | BT |  |  |
| STOP N | See general specifications | B $¢$ ST $¢$ P | BT |  |  |
| PAUSE N |  | B/PPZUSE | BT | B\$PPAUSE, N |  |
| CALL ERRCK ( N ) | Check error field | B\$ERRCK | BTM | B¢CRRCK, N |  |
| CALL EPRT | Print out error field | B\$EPRT | BT | B\$¢EPRT, B |  |
| CALL RESET | Reset error field to zeros | B\$RESET | BT | B\$RESET, B\$RESET-1 |  |
| CALL SKIP | Find next block or file card | BSEXIT | BTM | B¢EXIT, 0,10 |  |
| CALL EXIT | Find next program | BSEXIT | BTM | BSEXIT, 1,10 |  |
| CALL EOFB (N) | Interrogate block and file indicators | BSEOFBR | BTM | B\$PEOFBR, N |  |
| Return typewriter carriage and type a messag? | Obvicus | BŞTWSR | $\begin{aligned} & \text { BTM } \\ & \text { of } \end{aligned}$ | BSTWSR,LOC, ,where LOC is the the record to be typed. |  |

30. 

## TABLE IV

Useful Constants and Their Addresses

## Address

Constant

| BSPLONE | Field Address of 5110000000 |
| :---: | :---: |
| BStNINES | Field Address of 9999999999999 |
| BSPNINE | Field Address of 9999999999 |
| BSFZERQ | Field Address of 000000000 |
| BTPRERC | Defined as DC 21, @ |
| BTONE | Defined as DC 14,10000000000000 |
| BS¢ERRP | Defined as DSC 18,0 <br> This is the error field. |

## HINTS AND NOTES

(1) All object time subprograms should assume that the arithmetic overflow light is ON. Fixed add and subtract are done in line, not by subroutine, so there is lots of opportunity for it to get turned on. All the routines of Table III assume the overflow is ON. Conversely, if your subprogram could not care less. They turn it off themselves if they need it.
(2) The console area (locations 00000 to 00099) is avallable for work area. Routines of all sorts use it for temporary storage. Watch out for possible complications if your subprogram calls other subprograms which also use the console area as a
scratch pad. The accumulator is in B, $f$ FAC, loc 50-59. scratch pad. The accumulator is in BgFAC, loc
Put the result of a function subprogram there.
(3) The error field has blank spaces in it for user-defined error codes. The high order digit of the error field
is in location BSERRF. USe is in location BSERRFF. USe a TDM instruction to put a suitable digit in the right place. Do not used flagged digits in the error field. It will foul up the compare zero or zero or not.

The following papers were presented at the joint Canadian and Mid-western Regional eeting of the IB4 1620 Users Group in Chicago, February 19-21, 1964
hese programs will be submitted to the 1620 Users Group Program Library in the near future.

## CAPLETON COLIEGE CO:PILEE by Donald H. Taranto, Carleton College, Northfield, Ninn.

The Carleton College Compiler is a load-and-go algebraic compiler designed especially for the 20Z, automatic floating-point card system with indirect addressing and additional nstructions. Compilation and execution are fast, and batch operation is handied quickly. and elementary function arithmetic. In addition, there are boolean, maximum-minimum, and remainder operations. Subroutine calls are allowed and flexible alphameric typed output
is avallable.
The entire compiler occupies 9-1lk of core (depending upon what function subroutines aro included) and is practically fool-proof. Source statements are thoroughiy checked for legality during compilation
(bot not serious ostrictions on variable and statement formats.

CARLETON BINARY SI: ULATOR by William R. Gage, Carleton College, Northfield, Minn.
The Carleton Binary Simulator is an interpreter which turns the 1620 into a fixed-word-length, single address, binary computer. There are 4096 words of 16 its ( 15 bits and sign) each, as a input-output instructions.

This versatile and unusual interpreter is bought at the price of rather slow xecution of a source program. Machine requirements are 2OK Card System, Autcmatic Divide, Indirect Addressing, and Additional Instructions.

# Modifying Monitor I <br> to Include other Programming Systems 

by
Alan V. Purcell
Engineering Computing Laboratory
University of Wisconsin
Madison, Wisconsin

## Modifying Monitor I

## Modirying Monitor I

to Include othar Prograreming Systens

I Introduction
A. Objectives of Modification

1. Monitor I Compatibility
2. Compatibility with system
B. FORGO as an exmple of such a Modification

II Integration of the Systems
A. Modifications to Monitor I
B. Modifications to FORGO--a typical systea to be added
C. Operation of the Resulting System

III Soms Suggested Changes to Monitor I

## appendi

## I Introduction

The purpose of this paper is to show how it is possible to includ other programming systems in the Monitor I package, even if the systems to be added require different types of control cards and occupy the same cation, the system would have to be in use frequently enough to justify including it on a level with FOH TRAN II-D, the Disk Utility Program, and SPS II-D and it would presumably be undesireable to re-assemble it under SPS II-D and use it under the XEX option of Monitor I.

The resulting modified monitor system would have complete compatibility with Monitor I, i, e. all Monitor I functions would be performed cards for the additional system and transfer control to it when such an option is specified. The system to be added would require some modification to require it to return control to the Supervisor routine when a Monitor I control card is specified.

In this paper the necessary changes to Monitor I are explained. As an example of a typical system to be added, the FORCO Fortran comis a compiler which is uniquely suited for educational use because:
(a) FORGO is a load-and-go FORTRAN compiler. Since it resides in memory at all times, it eliminates processor reloading in memory at all times, it
and object deck handling.
(b) It has exrememly complete diagnostics, both at compile time and run time. Even at run time, all comments are referred and run time. Even at run time, all commen
(c) FORMAT is optional, permitting the postponing of this single FORMAT is optional, permitting the postponing of this sing most complicated rinal

It should also be noted that the version of forco used was the two pass system, in which the compiler section is overlayed in memory by the subroutines at program execution time. The compiler section is known as FOR-TO-GO $A$ and the subroutine section is known as FOR-ro-to B.

Under this scheme, if a FORGO control card is recognized by the Monitor I Supervisor, FOR-m0-G0 A is called into core. If the program is accepted, FOR-TO-GO $B$ is called in and the program executed. If a Monitor I Control Record is then read in, control returns to the super jobs (i.A. FORTRMN II, SPS, FORGO, previously assenbled or compiled object program, etc.) is perfectly allowable and requires no operator intervention to load decks.


Figure 1-IEM 1620 Monitor I System


Figure 2 - Educational Monitor System

II Integration of the systems
A. Modifications to Monitor I

The basic modification to the Monitor I systen is, of course, the inclusion of the additional system to be added. FQRGO is used here as an example.

This modification is made more difficult by the fact that the supervisory routine of Monitor I requires all core locations below location 2402, as does the FORGO compiler. This means that FORGO will have to replace the Supervisor in memory, yet be called into memory under control of the Supervisor. Also, patches to Monitor I and must be replaced every time they are destroyed. The specific patches to accomplish this are found in the Appendix; it suffices to outline them generally here.

The patches to Monitor consist of two main parts; one is the routine which reads in the patch area of the Supervisor every time it is destroyed, and the other is the routine which scans the incoming cards for FORGO control cards--2s well as for Monitor I conthe Supervisor, reads the Monitor I Supervisor patch area into location 13162 and branches to it to execute the instructions dis. placed by the first patch area. The choice of location 2914 to begin these read instructions was not arbitrary. The instructions in this area are executed every time the Supervisor is read into core, thus assuring that the second patch is in core also. It is location that makes certain that several disk indicators are reset, in the second patch area does not cause erratic disk operations.

The second patch area forms the linkage between the Monitor I systen and the FORGO compiler. Upon recognition of a FORGO control card, the FORGO campiler is read in and supervisory control passes to it. Thus, in this patch area is the routine which scans for FORGO control cards.
B. Modifications to FORCO-A typical System to be added

The patches to $\operatorname{FORGO}$ are chiefly those required to link FORCO and the Monitor I Supervisor (see flow chart, Fig. 3). Using the modified system, if a FORGO control card is recognized by the Super visor, FOR-TO-GO A (the compiler) is called into core from disk. If the program is accoptable, FOR-T0-G0 B (the subroutines) is called in and the program is executod. Control is then returned to the Supervisor, and the process repeated. Every card read under the supervisory control of FORGO is checked to see if it is a Monitor I
control card; if it is, FORGO operation is terminated with an orror contront if appropriate, the Supervisor is read from disk, the card is set-up in the Supervisor input area in menory, and supervisory control is relinquished to the Supervisor.


Figure 3 - Flow-chart of Modifiec System
92
C. Creation of the Resulting System

The procedure used in creating the working version of the resulting system is given here. The pertinent listings and typewriter sheets are
given in the appendix of this paper.

The same basic procedure is used in adding the main patch area to Monitor I and in adding the additional system. It is necessary that the actual changes to the Supervisor, which are done using the D. U. P. routine DALTR, be done last.

The basic procedure was to first load the Monitor I system on disk as described in the Monitor I Systems Reference Mamual. After this has been accomplished the system to be added, for example, FOR-TO-GO A, is loaded into core. The Disk Write Program is used to transfer it to the
work cylinders, and the Monitor I D. U. P. routine DLOAD is used to move the information from the work cylinders to the desired disk cylindersin this case cylinders twenty-six and twenty-seven were used to contain FORGO and the Supervisor patch area. Exactly the same procedure is followed for adding the chiof Supervisor patch area (which starts in core at 13162).

To make the patches within the Monitor I Supervisor itself, the Disk Utility routine DALTR was used, and the desired changes were typed in (see typewriter sheets). Now the entire system in on disk in the form required for operation.

To get decks which will load under control of the Monitor I System Loader and to eliminate the need to do all of the preceding steps every time it is desired to reload the system on to disk, the DUP routine DDUMP was used. The system tables, the modified Supervisor, FOR-TO-GO A, FOR-T0-G0 B, and the Monitor patches were dumped on cards. It was then necof which is described in the Monitor I Systems Reference Manual. The systems tables deck replaces deck two of the original system, the Super visor deck replaces deck seven, and the other decks are added at the end of the other Monitor I decks when it is desired to load the system on to disk.

Concerning ordinary operation of the modified system, it is the same as the Monitor I system. Cold start procedures are exactly the same. however. These cylinders are protected by the Monitor I system tables.

III Sone Suggested Changes to Monitor I
B. Improvements to Monitor I

Other systems could be added to Monitor I, using much the same techniques as were used in adding FORGO to Monitor I. Possible additional systems could be ALGOL, UW-SPS, COGO, etc. Suitable cori-
trol cards could be designed, and the routine which scans for FORGO control cards could easily be expanded to include a scan for the other control card types.

A very important modification which should be ma'e to the Nonitor I system loader, whether Fofico has been added to the Monitor I system as described in this paper or not, would be one which puts read-only flags on the sector addresses of the Monitor I system routines as they are loaded onto the disk. The purpose of these sectors; information contained thereon may then be read but cannot be written over and destroyed. Although parts of the system must be left capable of being changed (i.e. the system tables), the unchanging parts could be file-protected by the loader--perhaps signaled to do so by a punch in a certain column in the heading control card of the decks to be loaded. Not file-protecting the system routines is a serious orror on the part of the creators of the syit, and as sitate reloading the entire system from cards.

| U |  |  |  |
| :--- | ---: | ---: | ---: | ---: |
| U |  |  |  |
| 02914 |  |  |  |
| 02914 | 49 | 02938 | 00000 |
| 02926 | 48 | 00000 | 00000 |
| 02938 | 34 | 04088 | 00701 |
| 02950 | 36 | 04088 | 00702 |
| 02962 | 46 | 02926 | 01900 |
| 02974 | 49 | 13162 | 00000 |
| 04080 |  |  |  |
| 04080 | 49 | 13242 | 00000 |
| 04088 |  |  |  |
| 04088 |  | 1 |  |
| 04093 |  | 5 |  |
| 04096 |  | 3 |  |
| 04101 |  | 5 | $J 3162$ |
| 04340 |  |  |  |
| 04340 | 45 | 13310 | 13001 |
| 13162 |  |  |  |
| 13162 | 25 | 09794 | 02878 |
| 13174 | 31 | 02110 | 04046 |
| 13186 | 26 | 02103 | 02857 |



| 13198 | 25 | 00440 | 02857 |
| :--- | :--- | :--- | :--- |
| 13210 | 32 | 00456 | 00000 |
| 13222 | 15 | 01967 | 00009 |
| 13234 | 49 | 02986 | 00000 |
| 13242 |  |  |  |
| 13242 | 25 | 13265 | 02855 |
| 13254 | 26 | 04941 | 10700 |
| 13266 | 44 | 04104 | 13160 |
| 13278 | 15 | 09828 | 00001 |
| 13290 | 33 | 13160 | 00000 |
| 13302 | 49 | 04104 | 00000 |
| 13310 |  |  |  |
|  |  |  |  |



| 13594 | 49 | 01342 |
| :---: | :---: | :---: |
| 13601 | 00000 |  |
| 13602 |  | 1 |
| 13001 |  | 0 |
| 04056 |  | 0 |
| 13602 | 1 |  |
| 13607 | 5 |  |
| 13610 | 3 |  |
| 13615 | 5 |  |
| 13162 |  |  |





| 18463 | 5 |  |  | 182 | INAR | DS | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 00595 | 0 |  |  | 183 | INPUT2 | DS | , 595 |
| 18464 | 1 |  |  | 184 | MON | DC | 1.1, |
| 18469 | 5 |  |  | 185 |  | DC | 5,19636 |
| 18472 | 3 |  |  | 186 |  | DC | 3,113 |
| 18477 | 5 |  |  | 187 |  | DC | 5,102 |
| 18478 | 48 | 00000 | 00000 | 188 | HT | H |  |
| 18490 | 36 | 18440 | 00702 | 189 | READB | RN | FORB, 702, |
| 18502 | 46 | 18478 | 01900 | 190 |  | BA | HT |
| 18514 | 46 | 15918 | 01400 | 191 |  | BV | 15918, ${ }^{\text {, }}$ |
| 18526 | 49 | 15918 | 00000 | 192 |  | B | 15918, , |
| 18534. |  |  |  | 193 |  | DORG | *-3 |
| 18540 |  |  |  | 194 |  | MORG | 10 |
| 18540 |  | 1 |  | 195 | FIRDIG | DS | - |
| 01070 |  |  |  | 196 |  | DEND | 1070 |

THIS IS A DDA TO CALL MONITOR

READ IN 8 DECK FROM DISK
TURN OFF OVERFLOW INDICATOR AND GO,GO,GO



| 141 |  | SF | 13160, , |
| :---: | :---: | :---: | :---: |
| 142 |  | BTM | 17104,53432,7, |
| 143 |  | B | * +20 |
| 144 |  | DORG | * -3 |
| 145 | HALT | H |  |
| 146 | READM | K | MON, 701 |
| 147 |  | TDM | 31,5 |
| 148 |  | RN | MON,702,. |
| 149 |  | BA | HALT |
| 150 |  | B | 2402 |
| 151 |  | DORG | *-3 |
| 152 |  | WACD | 595, , |
| 153 | END | BC4 | * +24 |
| 154 |  | H |  |
| 155 |  | B | READM |
| 156 |  | DORG | *-3 |
| 157 | INAR | DS | 5 |
| 158 | I NMON | DS | 5 |
| 159 | MON | DC | 1,1, |
| 160 |  | DC | 5.19636 |
| 161 |  | DC | 3.113 |
| 162 |  | DC | 5.102 |
| 163 |  | DEN | 1070 |

INDICATE MUN. C. RECORD ALREADY READ. ERROR LC-2
$18232 \quad 1717104$ N3432
8244
8252
18252
18264
$\begin{array}{lll}15 & 00031 & 18374 \\ 36 & 180702\end{array}$
$18300 \quad 461825201900$
18312490240200000
390059500400
480030000000
18356491826400000

2
$N$

| 19000 |  |  |  |
| ---: | ---: | ---: | ---: |
| 19000 | 34 | 00000 | 00102 |
| 19012 | 39 | 19263 | 00100 |
| 019024 | 34 | 00000 | 00102 |
| 19036 | 36 | 19254 | 00100 |
| 19048 | 34 | 00000 | 00102 |
| 19060 | 39 | 19321 | 00100 |
| 19072 | 34 | 00000 | 00102 |
| 19084 | 36 | 19257 | 00100 |
| 19096 | 31 | 00000 | 19228 |
| 19108 | 34 | 00000 | 00102 |
| 19120 | 34 | 19248 | 00701 |
| 19132 | 38 | 19248 | 00702 |
| 19144 | 36 | 19248 | 00703 |
| 19156 | 47 | 19204 | 01900 |
| 19168 | 39 | 19397 | 00100 |
| 19180 | 48 | 00000 | 00000 |
| 19192 | 49 | 19108 | 00000 |
| 19204 | 39 | 19487 | 00100 |
| 19216 | 48 | 00000 | 00000 |
| 19228 | 41 | 00000 | 00100 |
| 19240 | 49 | 01070 | 00000 |
| 19247 |  |  |  |
| 19247 |  | 1 |  |


| 19248 | 1 | WK | DC | 1,1., | THIS IS THE DISK CONTROL FIELD | 00083 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 19253 | 5 |  | DC | 5,4000 |  | 00086 |
| 19256 | 3 | 1 N | DC | 3.0 |  | 00089 |
| 19261 | 5 | BEGIN | DC | 5,0 |  | 00092 |
| 19263 | 29 | MES1 | DAC | 29, TYPE A 3 OIGIT | SECTOR COUNT ©, | 00095 |
| 19321 | 38 | MES2 | DAC | 38, TYPE A 5 DIGIT | CORE STARTING ADDRESS @, | $00099^{\circ}$ |
| 19397 | 45 | ME S 3 | DAC | 45, INCORRECT DATA | TRANSFER, PUSH START TO RETRY@, | 00103 |
| 19487 | 26 | MES 4 | DAC | 26,DISK OPERATION | SUCCESSFUL@, | 00107 |
| 19000 |  |  | DEND | START |  | 00111 |



160000800000 RS
EQUTAB LOADED FROM ic 5000 TO $10 \overline{0} 5079$ DIMFOR LOADED FROM iU？800 TO 100409 SEQ PL LOADED FROM 0 O801 TO 019200 DUP A LOADED FROM 10139 TO 118599 DUP B LOADED FROM 119300 TO 119399 DUP C LOADED FROM 117084 TO 117127 SUBSUP LOADED FROM 017024 TO 01.7074 ALLSUB LOADED FROM O 161,00 TO 016799 SPSIID LQADED FROM 018600 TO 01929 SUPERI LOADED FROM 19600 TO $1 \overline{19799}$ PH 1＋2 LOADEA FRAM 017200 TO 017313 PH $1+2$ LOADED FROM 017400 TO 016199 LOAD 2 LOADED FROM OIG940 TO 016964 SET 1 LOADED FROM OI9400 TO OT9599 SET 2 LOADED FROM 016800 TO 016939 DIM FS LOADED FROM OOG4802 TO 00̆4807 FLN FS LOADED FROM O 6200 TO 01621 FEXPFS LOADED FROM Oí6212 TO 016227 SUB FS LOADED FROM O16228 TO 01623 SXIC FS LOADED FROM O 16268 TO 016280 FATNFS LOADED FROM 016281 TO 01629 SQRTFS LOADED FROM OTG299 TO 01630 ABS FS LOADED FROM 016307 TO 016308
－ます 50 B 5
ますDUP 5
＊OFINE

## tゅPAUS

END OF JOB

```
3-62A FOR-TO-GO
YPE A 3 DIGIT SECTOR EOJNT
TYPE A 5 DIGIT CORE STAETING ADDRESS
00000RS
DISK OPERATION SUCCESSFUL
\ddagger\ddaggerJOB 5
                                    VIRITE FROM WORK CYLINDERS
\ddaggerDUP
*DLOADFORGOA 020010400010418500520000000001070DIPO26027
IUP* TURN ON WRITE ADDFESS KEY, STARI
DUP* TURN OFF WRITE ADDRESS KEY* STLR
OK LOADED FORGOA 0}2000\overline{0}52001860\mp@code{2402\overline{D}1070
END OF JOB
```

3－62B．FOR－TO－GO
TYPE A 3 DIGIT SECTOR COUNT
175RS
TYPE A 5 DIGIT CORE STARTING ADDRES 00958 RS
DISK OPERATION SUCCESSFUL

キキJOB 5
WRITE FROM WORK CYLINDERS
\＃\＃OUP
＊DLOADFORGOB 0201104000104174005400009580107001 P027028
DUP＊TURN ON WRITE ADDRESS KEY．START
DUP＊TURN OFF WRITE ADDRESS KEY STAR
DK LOADED F
END OF JOB

## TYPE A 3 DIGIT SECTOR COUNT

005 FS
TYPE A 5 DIGIT CORE STARTING ADDRESS 13162RS
DISK OPERATION SUCCESSFUL
まキJOB 5 WRITE FROM WORK CYLINDERS

キ末DUP
＊DLOADMONPAT 0202104 $10001040040053871316202402 \mathrm{DIP026027}$
OUP＊TURN ON WRITE ADJEESS KEY，START
OUP＊TURN OFF WRITE ADE：ESS KEY START DK LOADED MO
END OF JOB

## ままJOB 5

ALTER MONITOR SECTORS

## $\ddagger \ddagger$ OUP

*DALIR
SECTOR
$119664 R S$
ST.HALF 34000000010225097940287831021100404626021030285725 ORIGINAL ND. HALF 00440028573200456000001501967000094303162004781509 ORIGINAL SECTION
0225097940 TYPE CHANGE
$\times \times 490208000004800000000003404080007013604038007024602926019004913162 R 5$ IST. HALF 3400000001022509794020783102110040462602 . 1030285725 ORIGINAL IST. HALF 34000000010249028380000048000000000034040880070136 CORRECTED
$\begin{array}{lllllllll}\text { 2ND. HALF } & 0044002857 & 3200456000 & 0015019670 & 0009430316 & 2004781509 & \text { ORIGINAL } \\ \text { 2ND }\end{array}$ 2ND HALF 0408800702460292601900491316200009430316200478150

## TRS <br> OUSK SECTOR 119664 CORRECTED <br> 119675 RS

 2NO MALF OLI 01509828000002504127028552504103028552604941107 ORIGINAL

SECTION
OERS
OERS
1270285525 TYPE CHANGE Note typing error

 IST. HALF $566 \overline{0} 403322 \overline{0} 4018 \ddagger 1 \overline{19} 966 \geqslant 001 \overline{0} 2802 \ddagger 2209732 \ddagger 0000 \ddagger 010101$ CORRECTED


## SECTIION

| $\begin{aligned} & \text { SECTION } \\ & \text { OBRS } \end{aligned}$ |  |
| :---: | :---: |
| $12702855 . \overline{3}$ | TYPE CHANGE |
| XXXXXXXX491 | 1324201053870051 |
| IST. HALF 56 | 5660403322 04018\#1 |
| 1ST. HALF 56 | 56604033220 |
| 2RD. HaLF OT | IT 1015098280000 |
| 2ND.HALF OT | $1 \ddagger 0450982800000$ |
| SECTION |  |
|  |  |
| DISK SECTOR | R 119675 Corrected |
| SECTOR |  |
| $119678$ |  |

SECTOR
119678

IST. HALF $60440432804127340000 \quad 000102150982800001450405613001$ ORIGINAL 2ND HALF $45040561300316097040 \overline{0} 00417080381300545044440973045$ ORIGINAL SECTION
OTCK5613001 TYPE CHANGE
yoouns $\leftarrow \leftarrow$ Typing error
1ST. HALF $6044043280412 \overline{7340000} 000102150982800001450405613001$ ORIGINAL IST.HALF 60440432804127340000000102150982800001454664613001 CORRECTED 2ND. HALF $4504056130031609704 \overline{0} 000417080381300545044440973045$ ORIGINAL SECTION
SEC
055.5
4.66
TY664613001 TYPE CHANGE Correction of error
$1331085 \$ 6044042804273$
 $\begin{array}{llllllll}\text { IST. HALF } & 6044043280 & 412 \overline{7} 340000 & 0001021509 & 8280000145 & 4665013001 & \text { ORIGINAL } \\ \text { 1ST. HALF } & 6044043280 & 4127340000 & 0001021509 & 8280000145 & 1331013001 & \text { CORRECTED }\end{array}$ 2ND. HALF $45040561300316097040 \overline{0} 00417080381300545044440973045$ ORIGINAL 2ND. HALF 45040561300316097040 0004170803 81300545044440973045 CORRECTED SECTION
$\neq$ FS
DISK SECTOR 119678 CORRECTEO
SECTOR
$\ddagger$ RS
$\ddagger \ddagger$ DUP
＊DOUMP CsO
END OF JOB
ままJOB 5
まキDUP
＊DDUMP Cl
END OF JOB
\＄$\ddagger$ JOB 5
まぁDuP
＊DDUMP CE
END OF JOB
まキJOB 5
ま¥DUP
＊DDUMP
CL 105200105385
END OF JOB
まキJOB 5
$\ddagger \ddagger D u P$
＊DDUMP
CL 105387105391
END OF JOB
$\ddagger \ddagger$ JOB 5
\＃\＃DUP
＊DDUMP
CL 105400105574

END OF JOB

## A New Course

in
Computer Appreciation

> Charles H. Davidson

Engineering Computing Laboratory
University of Wisconsin

Computer Education is becoming a recognized necessity for the technical student in college. at Nisconsin it has been incorporated in the required experience of all enzineers for some time, and is being made
increasingly available to interesteu students with various backgrounds and degrees of preparation, as is indicated in Figure I, which lists the courses available in the Numerical Anaiysis Department.

The first entry in this table, however, represents an innovation in the teaching philosophy. Here for the first time is a course deliberately aimed at the non-technically tra ned student. As is pointed out in Figure II, the catalog descriftion of the course, the only prerequisite is intermediate level high school algebra, equivalent to about two and one half University freshmen are eligible to take this course. "Introduction to Computing Machines" is intended to be more of a
cultural than a professional course. Many of the students who take it
may indeed never use a computer again, but they will all hear about canmay indeed never use a computer again, but they will all hear about cam-
puters every week of their lives. ihenever they receive a paycheck, reputers every week of their lives. Whenever they receive a paycheck, register for a class, pay an insurance premium, make an airline reservation,
or watch a rocket launching or an election return, it is almost certainly an IBM card or a computer-produced document they will be dealing with.

As the course is taught, the first two weeks are devoted to acquiring enough of a rudimentary knowledge of foriran to be able to present simple problems to the computer. The rest of the course consists of examining some of the areas of significant application of the computer, classified as far as possible according to the particular advantages or capabilities of the computer. In each case, the students actually do simplified, hopefully point out and make meaningful the true role of the computer in these areas. During the first semester it was offered, the students each did about twelve problems on the computer, including problems in:

1) finding roots of polynomials
2) class scheduling
inventory control
3) missle tracking
4) library information retrieval
and several others.

All of this laboratory work has been done in the Engineering Computing Laboratory using the FORGO system, which is ideally suited for this type of teaching, with the exception of one problem near the end of the semester in which the use of the CDC 1604 and monitor syster
operation were demonstrated.

Figure III presents a condensed outline of the course, indicating some of the topics discussed and their sequence. Perhaps, however, one of the best pictures of the scope of the course can be obtained from the
list of feview vuestions shown in Fifure IV , which was distributed shortl list of Review wuestions show in Figure IN, which was distributed shortl hefore final exam time,
pected to have learned.

Since there is obviously no text-book existing which treats such a ranfe of material in this fashion, we are preparing all of our own notes for the course, which will be published as a textbook. A preliminary version of the notes will be printed for use with the third offering of the course in the fall of 1964, and the official published version of the book is expected to be out in the late spring of 1965 .

Some people are referring to the course in a colloquial fashion a Computer Appreciation". This we accept as an apt description, provided self course in computer apprectation".

## THE UNIVERSITY OF WISCONSIN <br> colleot or enainemina

madison 6

UNIVERSITY OF WISCONSIN
Courses in Computer Programming

| NUMBER | TITLE OF COURSE | PREREQUISTTE | CREDITS |
| :---: | :---: | :---: | :---: |
| NA 132 | Introduction to Computing Machines | Intermediate high school mathematics | 3 |
| NA 301 | Computer Programming in the Physical Sciences | Differential Equations | 2 |
| NA 315 | Introduction to Data Processing Methods | One semester college math | 3 |
| NA 413 | Introduction to Numerical Analysis | Differential equations | 3 |
| NA 415 | Intermediate Programming Methods | Differential equations and elem. FORTRAN | 3 |
| NA $814 \mathrm{a}, \mathrm{b}$ | Advanced Numerical Analysis (year) | NA 413 | 3,3 |

Plue seminars and short courses

## Numerical Analysis 132

"InTRODUCTION TO COAPUTING R.ACHINES"

How computers work; conmunicating with concuters; areas of application and significance; simple FOFRRAN programning; elementary dats processing and problem solving. Prerequisite, intermediate level of high school mathematics. offered each semester, 3 credits. An opportunity for the non-technically trained person to acquire an
understanding of the uses, method of operation, and significance of the electronic computer in the world around him. Students will both hear about and actually use the computer in solving problems in mathematics, business, game playing, and many otber fields.
The course will be taught jointly by the Numerical Analysis Department and the Electrical Engineering Department, with two lectures and a laboratory period each week. It will be first offered in the fall of 2963.

[^0]Figure II

## NA 132

Numerical Analysis 132
"INTRODUCTION TO COMPUTING MACHINES"

## The Information Machine

The FORTRAN Language
Things Worth Computing: (A) Routine Repetition
The Second Industrial Revolution
Things Worth Computing: (B) Try and Try Again
Further FORTRAN
Things Worth Computing: (C) When Mistakes are Costly
What Goes on Inside Computers
Things Worth Computing
(D) Hurry, Hurry, Hurry The Language of the Machine Things Worth Computing: (E) Simulating the Real Thing Other Kinds of Computers

Things Worth Computing: (F) Memory Like and Elephant
Things Worth Computing:
(G) Just Plain Curiosity

1. Actual FORGO operating procedure on the 1620.
. Distinguish between: a) machine language b) symbolic language c) algebraic language
2. What is the difference between "compile" time and "axecute" time? How does FORGO mark the transition?
3. Nane two (data handling) processes at which the muman is more officient than the computer
4. Below are listed five characteristics of computers. List three important areas of application that take advantage of each (not necessarily mutually exclusive).
a) high speed
b) accuracy (freedom from mistakes)
c) repetetive ability
d) large non-forgetting memory
e) logical ability
5. What are "pseudo-randon" mumbers? What good are they?
6. How are computers used in inventory control?
7. What trends are observed in business uses of computers?
8. How are computers used in product design? How does this compare and contrast with automation?
9. What is a "critical path"?
10. When is a computer operating in "real" time? Illustrate.
11. Elementary binary arithmetic.
12. Why is binary arithmetic used?
13. What are the five main functional units in a general purpose digital computer? Diagram then, showing the principal paths of data flow and control.
14. What is meant by a single address computer? two address? one-plose one address? three address? cive an example of each type of instruction.
15. Compare analog and digital computers.
16. Name the three main logical components of an analog computer. Which is used to get distance from velocity? How?
17. How do you program an analog conputer?
18. Why are libraries concerned with "Information Retrieval"?
19. What are some of the problems in attempting to upgrade the inteliigence of a computer?

## Figure IV

## COMPUTER CENTER

## Western Michigan University

The Computer Center was established in Room 372 of lood Hall in August 1962. Professor Jack R. Meagher was appointed Director.

The Computer Center is organized as a University-wide service, like the University Library, to provide research,
training and service facilities for faculty, staff and
students. A basic policy of the Center is to encourage
widespread interest and use of all its equipment. Highly technical knowledge is not required. Information oncerning the use of the Center's equipment is being prepared and will soon be distributed.

An Advisory Committee, consisting of the Director of the Computer Center, the Dean of the School of Graduate Stud ies, and nine other faculty member's have been appointed by the Vice President for Academic Affairs. This committee will (1) be representative of the whole Univer ity, (2) present the Computer Center's operations to the University, and (3) establish broad, general policy for the Center.

The followin
organization


Secretary-Key Punch Operator
Graduate Assistants

## March, 2964

following equipenent has been installed in the Computer Conter at Western Michigan Oniversity:

IBM 1620 Central Processing Unit - ( 20,000 position
of core storage, a console panel, and an
input-output typewriter.)
Autconatic Divide
Indirect Address in
Additional Inetructione
Floating Point Arithetic
1622 Card-Read Punch
1623 Storage Onit (additional 20,000 positions of core atorage)

In addition to the IBM 1620 Date Procesaing Syster, which is an electronic computer syston for scientific and technological appichines:

2 Key Punchy (026) A besic machino for traneforring data to punched cards. It also can print the punched data on other cards.

Sorter: (082)-with Counting Unit) This machine sorts cards into a nunber of pre-selected categorios. The counting

Collator: (077) The basic function of the oollator is "filing". It is capeble of making comparisone between decks of cards; and then merging, selecting, or check-

Reproducer: (514) This machine can produce carde that have been previously punched. It can daplicate the original Interpretary (552) This machine prints on the face of
cards the data that is punched in them. It facilitates cards the data that is punched
reading and editing the cards.

Accounting Machine: (L07) The Computer Center will use this machine primarily to print the imput and output data of the computer. This machine has many other capabilities.
A. Mathemation Dopartmont:

## Fortran Workehop

A short, intonsive, no-credit course for 20 clock hours. The workshop 10 non-tochnical in nature, and has no pre-requisite. The purpose of the workshop 18 to teach the fundementale of ing. This workshop is offered each semester and Progreming for camputore - 506

Organization of, problon proparation for, and genoral noe of, high-epoed computing suchines from the point of viow of aciontific and ongineoring computations. Flow charts and prograve will be prepared for problens such as: social security, mitrices, solution of polmonials and correlation. Problem will bo dope in machine language followed by the use of a com piler (Fortran). Booloan algebra. Integration of one ordinary difforontial equation nuerically. Pre-requisite: Calculus. This is offorod overy memestor.

Mreorical Amalyeie - 507
memerical mothode as appliod to matrix inveraion, sete of linear equations, linpear prograving problems, eigen-values and eigon vectors: Integration of ordinary differential equatioas and integration of partial differential equations vilil prosented. Pro-roquieite: Math 530 (Vectore and Matrices)

## B. Breimese Adelaistrationt

## Inteprated Data Processing - 359

A survey of mochanical and electronic data processing mothode vith partioular emphasia on the application of the -liectronic ayaton and with special reforence to adninistrative probleme oxporiencod in introducing computor systent.

## Introdeoticen to Managmont Sorionce - 554

Modorn eciontific tachniques ueed in businese and
indostry for controulling oporations, meximising profits and mininizing costo. Allocation of mon, memoy and machinoe mong altornat ive weos. Other atrategios and control mothode applicable to
managomint, martoting and financo. Proq.--a course in Statietics.

## Mectronic Data Processing Seminar - 555

Examination of carrent literature in electronic data procousing with epecial emphasis on systons andiyais, applications procosesing with apecial enphasis on sys tons anayzis, applic
of computers to bufiness probiems, and foasibility studies. Pro-Requifite: A Computer Course or Coneent.

## Exercises Assigned in Math 506 Programming for Computers

1. Volume of Right Circular Cylinder

Machine Language
2. Social Security Problem Machine Language
3. Square Root by Newton's Method Machine Language
4. Ouadiatic Equation

Machine Language
5. Volume of Right Circular Cylinder, Use

Fortran Sense Switch to Compute
$V=\pi r r^{2} h ;$
$V=\pi r^{2} h$
$V=\pi r^{2} h$
6. Ouadratic Eouation (Use Hollerith Statement) Fortran
7. Given the coordinates of two line segments, Fortran find coordinates of the points of intersection.
8. Evalcate $e^{x}$
9. Multiply two matrices

Fortran
Fortran
Fortran
Fortran
Fortran
Fortran
Fortran

Fortran

- a. Calculate an integral by Trapezoidal

Calculate an integral by Simpson Rule
b. Solve a differential equation by the
Runge Kutta Method.

# KANSAS STATE UNIVERSITY 

The following is a resume of my talk presented to the joint meeting of the Canadian and Midwestern Regions of the 1620 Users Group in Chicago, February 21, 1964

Miami University, having no engineering school, has concentrated its computer education courses in the new Department of Systems Analysis. This department functions as both a degree granting department and a service department for other University departments.

In its role of a service department, a course in 1620 FORTRAN ( 2 credit hours) is offered each semester and during the summer term. In addition, students from other departments are free to take any Systems Analysis courses offered provided they have the necessary prerequisites (proper mathematics background in most cases).

For majors in Systems Analysis, two alternatives are offered, business or scientific. In either case, the first two years are devoted to programming, computer analysis, and an introduction to systems analysis. The programming progresses from machine language, to assemblers, and then to the various compilers. The third and fourth years are devoted to the tools of analysis where all examples are worked on the computer.

The Systems Analysis courses offered are:
Introduction to Systems Analysis I and II
Computer Analysis I and II
Systems Design and Selection
Linear Programming
Analog and Hybrid Systems
Operations Research I and II
Simulation and Model Building
Dynamic Programming
Advanced Data Processing Applications I and II
Management Science
Commercial majors are required to take some business and accounting courses as well as 20 or more credit hours of mathematics. Scientific majors are required to take some physics as well as 30 or more credit hours of mathematics.

## manhattan, kansas <br> 66504

## Department of Mathematice

Physical Science Building
Pebruary 27, 1964

The following is a brief outline of my talk at the 1620 Users Group (Panol on Education), February 21, 1964, at Chicago.

Kansas State University, a Land Grant school, has approxirately 9000 students in a wide variety of curricula. Our basic computer course, 2 hours credit, of fered every semester, has an enrollment Enrollment will be larger since the Englneering school is making the course mandatory. We teach pericharting, then sone then 1620 and $1401-1410$ series. We stres Fortran. We use McCracken's book as toxt, with IMM manuals, and we recommend Germain's book as well.

The Business College uses Schmidt and Meyers as a text
We teach Scientific Computing Techniques, requiring differentia equations and the basic course as prerequisites. Our text is Ralston and Wilf. In addition we have a number of computer-oriented courses such as our Numerical Analysis I, II and III and cortain courees in Network Logic, Components, etc., taught in Engineering.

Our staff consists of four regular faculty menbers, with halftime computing center appointments, a mumber of graduate assistants each one-quarter time, $21 / 2$ key-punch operators, and a machine operator.

Yours very truly,
S. Thenas Parker, Director
S. Thonas Parker
Camputing Center

A SURVEY OF THE BEGINNING FROGRAMMING COURSE
Clarence B. Germain
College of St. Thowas
February 20, 1964
Last Fall, a questionaire was sent to the 280 schools which are mexbers of the USERS Group. 175 schools responded. The results are tabulated on the following pages.

1. No allowance has been made for non-respondents. This does bias the results.
2. Since the survey covers only schools having 1620's, the figures for the end of 1964 do not reflect the influence of schools which will acquire their first l62 during the year.
3. A suprising number of respondents gave incoaistent answers; e.g., they indicated floating-point hardware, but not divie hardware, or they indicated that 35\% of their students run their own SPS programs, while they taught SPS only to $20 \%$ of their students.
4. Figures for index registers, binary capabilities, and the 1627 plotter may not be indicative since the questionaire was circulated too soon after announcenent of these features.
5. Average enrollment in the beginning programming courses in 170 students per school per year.
6. Many of the Model II 1620 's will supplement existing Model I's, not replace them.
7. Relatively few schools indicated any plans to obtain the 1443 printer.
8. The disk units will more than double in popularity during 1964 with $1 / 3$ of all schools having at least one disk unit by the end of the year.
9. While $3 \%$ of the schools offered no course involving Fortran, $35 \%$ of the students were taught more than one version of Fortran.
10. At the end of $1963,51 \%$ of the schools had the hardware necessary to run Fortran II; by the end of 1964, this figure will rise to $59 \%$
11. $85 \%$ of the students get "hands on" experience in running their own programs on the computer. This percentage is about the same regardless of what programming systems (SPS, GOTRAN, etc.) are taught.
12. Jim Moore's Multi-Trace, 1.4.CO3, was the most commonly mentioned trace program taught to students. However, 85\% of the schools indicated that they used no trace program in their courses.
13. The figures for textbooks are for use in at least one course. Many schools use more than one text in a course. 3le, of the schools use only IBM publications as texts. While a wide variety of texts, many unrelated to either Fortran or the 1620, are in use, only four comiercial texts and a half-dozer IBM publications are used with any frequency. of the non-programming type texts, numerical analysie books, particularly Stanton's, were most often mentioned.
14. The textbook percentages i: no way indicate sales of books; these figures are quite different from the percentages shown here and were not a part of this study.

Results are given as a percentage of the number of schuols replying to the questionaire. Probable errors do not exceed $\pm 3$ except for itens marked with an asterisk and for the end of 1964. Changes for 1964 are only for equipnent now on order. Slight discrepancies in the percentages are due to rounding.

| 1620 Model: | 1963 | 1964 | Number of 1620's in the sshool: |  |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 98\% | 89\% | One | 95\% |
| II | 2 | 11 | Two | 5 |
| Special Features, Model I |  |  | Special Features, :10del 11 (1904) |  |
| AFP, Div, IDA, Edit | 31 | 31 | Automatic Floating-Point | 6\%* |
| AFP, Div, ILA | 3 | 3 | Index Registers | c* |
| AFP, Div, Edit | 0 | 0 | Binary Capabilities | 5* |
| AFP, Div | 1 | 1 |  |  |
| Div, IDA, Edit | 31 | 31 | Installations with Printer ( 1954 ) |  |
| Div, IDA | 14 | 14 | No disk | 23* |
| Div, Edit | J. | 1 | 1 disk | 15* |
| Div |  | 3 | 2 disks | $54 *$ |
| IM, Edit | 1 | 1 | 3 disks | 0 |
| IDA | 3 | 3 | 4 disks | と* |
| Edit | 1 |  |  |  |
| No special features | 13 | 13 | Type of Courses Offered: |  |
| Summary: |  |  | Both credit and non-credit | 5 |
| Automatic Floating-Point | 34 | 35 | Non-credit courses only | 30 |
| Automitic Divide | 82 | 82 | Credit courses only | 13 |
| Indirect Addressing | 82 | ¢2 | No answer or no courses | 47 |
| Additional (Edit) Instructions | 64 | 64 |  |  |
|  |  |  | Departments which offer courses: |  |
| Storage: |  |  | Engineering | 40 |
| 2OK core, no disk | 48 | 38 | Education | 1 |
| 40k core, no disk | 21 | 18 | Mathematics | 45 |
| 6\% core, no disk | 17 | 13 | Business | 31 |
| 20k core, disk | 5 | 12 | Other | 40 |
| 4ok core, disk | 4 | 9 |  |  |
| 60k core, disk | 5 |  | Subjects Taught: |  |
| Saput-Output: |  |  | Machine Language Operation of the Computer | -32 |
| Paper Tape only | 4 | 4 |  | $2 \%$ |
| Peper Tape end Cards | 10 | 10 |  |  |
| Caids only | 86 | 80 | GOTRAN | 17 |
| ilegnetic Tepe | 4 | 4 | FORTRAN with FOR1AT | 47 |
| Paper Tape | 13 | 14 |  |  |
| Cards 1622-1 | 83 | 81 |  |  |
| Cards, 1622-2 | 13 | 10 | Use of some library trace | 13 |
| Cards, RPQ to read 800 cpm | 3 | 3 | Blosl: Liagramuing | 5 |
| 1443 Printer |  | b | Ptonitor I | \% |
| Disk, one or more | 14 | 3- |  |  |
| 1 l 27 Plotter | 4 | 4 |  |  |
| 1710 | 2 | 3 |  |  |


| :isks: |  |  |
| :--- | ---: | ---: |
| No disk | 86 | 68 |
| 1 disk | 8 | 20 |
| 2 disks | 5 | 11 |
| 3 disks | 0 | 0 |
| 4 disks | 1 | 1 |
| Hardiware necessary to run: |  |  |
| Fortran II only | 37 | 29 |
| Fortran II and II-D | 9 | 19 |
| Fortran II-D only | 5 | 11 |

Students are experted to write and run the + r own programs using:
SPS II
th FORMAT FORTRAN Pre-Compiler FORTRAN II

Hardware necessary to run:
29
19
Fortran II-D onl
11

Required or recoumended texts:

## IBM Publications

162́ Reference Manual
710 Reference Manua
SPS Reference Manual
GOTRAN Reference Manual
1520 FORTRAN Reference Manual
1620 FORTRAN II Bulletin
OITRAN General Information Manual
1620 Program Writing and Testing Bulletin
Introduction to IBM Data Processing System
Programming and Block Diagramming Techniquesommercial Publications
Germain-Programming the IBM 162039
6
ng Concepts and the IBM 1620 Compute
rucnberger-McCracken-Introduction to Electronic Computers
HcCracken-A Guide to FORTRAN Programmin
Organick--A FORTRAN Primer
olman-Smallwood-Computer Languace
Snith-Johnson-FORTRAN Autotester

DATA Procesining technician training
The Need; The Attempts;
The Need; The Attempts;
Computers: Are the nucleus of an extrenely large field of operations called Electronic Data Processing. All hancling of information within present day large organizations must be done with the electronic conputer in mind. The rate of growth of that organization, coupled with the rate of developnent of compact, fast, efficient, econonical computers demands that any and all internal operations be designed with the computer as a possible, if not central, thene. Many more smaller organizations enter the field of computer operations each week, to say nothing of the acquisition of electronic data processing equipnent on the part of larger corporations. Saxe of these companies decide to make use of computers because of profit notives. Others wake the switch to computers defenisvely because their conpetition down the block has installed a computer. These basic reasons and many more subtle factors are at work in forcing businesses toward the world of Electronic Data Processing.

Agility, ability, capability and speed of the electronic computers cause complete revamping of internal operating systems. Even the word "Systens" takes on a different significance when used in conjunction with "Electronic Computers." Information processing nuw has to be looked upun on the "Total Systems Concept," that is, the processing, handling, generation, and analysis of data through a single neans; the electrunic computer. Siall centers of activity in the line of infomation travel, and for tint matter entire lines of travel have been eliminated by the computer. The Total Systens Concept dictates a complete review and analysis of infomation requircients, methuds of handling data, necessity for various reporting nodes, lines of data niovernent and necessity for generation of information. The computers capzbility of retention of data in its original fomat in many cases conipletely eliminates the need for rugenerition centers along the lines of infomation travel. The speed of operation and manthenatical as well as storage ability oftentines pronoted an entirely new systeri of operation. What before had to be done because of pure necessity could now be accoaplished "on line." Even "Eapire Building" touk a seriuus setback. These things were a seri
127

## Page 2.

accoriplished only if a cuncerted effort was made to get them accomplished. Only the foolish attenpted to incorporate a conputer as a single iten part of an ovarall system now operating for the single purpose of getting a single job done. Foolish or not, this has often been done.

Integrated computer operations deluanded integrated personnel operations.
People, or groups of people within an organization, that before never had any interrelationshipe now found themselves stuabling over one another wondering what next to be done. The Tabulating Departicent people on the one hand found that the Systems Department people on the other hand seealed to be working at add ends with them. The corputers promise of the sc far intangible brought about a coordinated effort on the part of these two groups. In fact, some data processing people were even caught taking courses in Systens Analysis and vice versa. Most major computer installations today are nizde up of two categories of persunnel, Data Processing and Systens Analysis, working together quite harmoniously. Thair acconplishmenta have been fantastic to say the least. But sonething is definitely lacking; a sonething which could and would provide s.s nuch more; a sumething which could and would reduce conputer operational cost quite significantly. That sowithing is a single brain thinking and wirking an integrated Dita Processing, Systems Analysis approach.

Simple econonics derands that we now find persmnel with bcth the Data Processing and Systens Analysis training and experience. The shicrtcominge of single field training when considering cverall coraputer managetient are becoming more and more significant every day. There are several reasons for this, first, single field training limits an individual's apprisach, definition, and solution selection to a problom. Secondly, reduced cust of actual equiprent negates the advisability of employing twu to du the job of une. Thirdly, because of cost of uporations, vision as well as practicality is required in the selection of fields of computer applications. Fourth, the sualler urganizations cannot maintain high computer overhead cost. Fifth, from a profit standpoint, efficiency must be maintained in direct propurtion tc capability of the equipnent involved. 128

Page 3.
The denand for proper, effective training, therefore, is fantastically greater today than it has ever been in the past and it continues to grow more and more with each conputer installation. Far too often we in industry find that our present staff is not adequately caprble to provide our managenerits with the desired level of results frop a computer operation. All too soon, we realize that the answer lies in integrated training, formally applied, and practical experience. All too soon, we realize that there is no source of supply for this category of individual. Training, therefore, becones a major problern to us.

Proper adequate training is the focal point of the single major problem of industry in the field of Electronic Data Processing. Training in the practical way of doing scmething has always been accomplished by a given organization within its own environment. Different companies within the same industry had much different ways of accomplishing the same thing, and, therefore, each organization trained its own personnel in its own way. Naturally, industry relied, and still does rely, upon fomal elucation to provide the basic general concepts as well as related principles. Industry solved its training problem for the nost part by setting up In-house, On-the-Job training programs designed to get the nost for the least cost. Many tines these procsrams were extranely limited in scope simply because of the fact that industry chose to use personnel with extrenely limited backgrounds. Huch of the reason for this was a lack of willingness to pay higher wayes for lesser scale jobs.

Profit motive restricted training to a MST level and added none of the
frills of peripheral, or related areas of training. The objective of "Adequate Button Pushers" seemed to be the most efficient level of in-house training. In reality, this is all that inclustry should be responsible for providing. In all categories of jobs, this in-house training was enough to allow profitable operation. Most jobs did not require a great deal of knowledge, if any, about the last operation or the next operation in the line of process. It was only necessary for the individual to know his or her own special function.

Until the conputer came along this was a fairly satisfactory method of 129

Page 4.
training. The O-J-T apirfach was profitable fron tw standpoints,
first, few dollars invested, secınd, appreciably high production after training. Without having to be cognizant of the previous cperation or the next operation to cone, an operator could attain maximun production efficiently and quickly. This was true also in the Data Processing field. For the rost part, training of personnel was accomplished in relation to operation of a specific machine or group of nachines. Key punch operators learned to simply key punch and verify. Tab operators learned the operation of a series of machines, and in sume cases also learned to wire cuntrol panels for these machines. Fron a training standpoint, these data processing jobs were just as any other jub in any ccalpany, i.e., learn a specific process fur a specific operation without consideration of any rolated areas.

Computers brought about the necessity for training even more categcries of personnel. Systems analysts, prograrmers, cuders, prograni librarians, infurmation librarians, cunsóle operators, became new and inpusing personnel categories. New, because they came in the frunt door just ahead of the computer. Imposing, because for the first time a jub category cme elong that demanded an acute interest in what has happened bef.re "this operation" and what will happen after "this operation." No longer cuuld an "operater" be trained to simply accomplish a single operation. Sune syster: of training had to be developed which would allow these new categories to be trained in a reasonable period of time and at reasonable cost. The on-the-job training approach again was utilized by industry in conjunction with short term courses put on by the manufacturers. Initially these two media proved to be just adequate. The only reason that they were adequate was that the personnel originally selected tu enter the training progranis, and then to handle the computers, were parsonnel with lung experience with the conpany involved. The fact that they did have the conpany experience, and, therefore, knew the internal aspects of the organization quite intinately, alluwed them tu sclve most all major problens without to nuch loss of time or noney.

At the satue time, these persunnel were garnering the necessary hands-on 130
experience on the cmputer invclied. This perici of tias has been a substantial one. Same of the early camputers deliveres to the industries carne along in the early 1950's. The personnel selected for the ca.:puter cperitions did through trial and error, and OTT rethois, finally attain a dagree of prificiency in the handling of buth the computers and the informintion invcived. However, this took several years of hard work and a severe cotpronise of uriginal gials and target dates.

Numal attrition fur varicus reasons iictate: that en adequate attempt be nacie in-house tu train replacenents. The major problem here wes ne of tire. Incustry could not afford to invest tiree tu five years of training fur each of the replacenents. Job attrition rate was far beyond this replacenent rate. Sone fast neans of training wes abs.ilutely essential. Here tine question was raised, "Do we do this in-house again, cr do wa go outside for cur sujply of people?" Obviously, the in-house training e:st maje ancther suurce of supply nore desirable. What then was the source to be? Wuuld tha apperent returns of amployment draw very many capable people into private training cperations? Wculw, in turn, the private training operations privice alequate levels of reliible training for reasonable costs? Did any trining facility, privite or public have the necessary instructers availible? what prugran wiul: the industries have to uniertake to attain guod levels of alucation in the jublic schuol systerns? liost major induatries gathared $t$ ixpother for the jurpose of letemining sure of the answers to nost of the questions.

Meny answers were founc, and, as a result, many propusals by iniustry were made to education. All of then were robuffed for varicus reasins. In sune cases, education administration personnel were willing to take on the responsibilities of these new requirecients but cculii nut find faculty to staff such an enclavor. More often than not, a nexjative attitude on the part of ajministration personnel in public olucation restited in imiustry going hack to costly in-house methods. People in universities and colleges cansidered the field tu be a rocational one and nut an acodemic ine, ani, therefure, it culd not be touched
with a "ten foot pole." The jurple in vucational schocls were all tal willing to accept the challenge, but campletely nognted the requirements of industry by telling industry that their desires for anything beyond the uperatur status were ridiculous, and, thereby, vucatimal education fell down on the joh. Incustry then racted in the negative quite viulently. hll propisals to education were withdrawn and in-huuse, expensive, time-conswaing training was put into effect. In sone of the more comprehensive of these prograns, it was not at all uncoumon $t$ - find the cust of training at the $\$ 30,000.00$ to $\$ 40,000.00$ mark. Time stretched out from the nomal one or tw, munth periol to sonewhere in the area of three to five years, with all its built-in rarifications.

Public education finally entered the field of Data Processing on a late, reager, but welcome basis. First if all, the educators hed to be educated. Those acrainistraturs an: faculty perscnnel of various public school systens who desired entry into the ficld of Data Processing had to leave their pusts full time or at least part time to get a bit of education themselves. The problens involved here were many and varied. The oricinal estimites on the part of both manufacturers and users that at least a college degree in mathematics was an essential prerequisite to computer operations was inuressive and rany university and college personnel tuok this to heart. Leaves of absence were granted to scrae very few PHD Mathematics type people willing to exjose thenselves tu the rigors of the industrial wurld. Others went to the minufacturers' short courses in sjecific operations to acquaint thenselves with sunde of the computer requireants. This training suon becarue pretty much of a bandwagen effurt. If the exiucation people were at all interested, which they prubably weren't, they tried to get on the banciwagon. Sunchiw they got tienselves exposed to a course or two, and tu a lot of conversation so that they at least knew the terminology of the field. Because of the influence of the manufacturexs initially, almost all first coners from education to the fiell of Data Pricessing were in the mathenatics area. To converse with these people on their uwn level, an attenit was mace to train them in the finer arts of connutor utility by mans of manhenticel problem solution.

This, indeed, servec its purpose, but it also ha: some very undesirable results. The first and nost injortant of these was to indefinitely postrone industry'e desire of Data Prucessing training. The reasin was quite cbvious, of course. Mathematicians would naturally set up mithenatics type courses first, and perhaps other courses later.

Educators from other fields graiually cane to either industry or the manufacturers te gain somis insight int, the world of cumputers. Sone went to the manufacturers for their short courses in specific operations and specific machines. Others left the field of education completely and entered in lustry bent on learning all they could about the entire fiel:! of Datc Processinc; and then returned after several years to education to set up courses of their own in their own professional fields. Thise that did return to education found thenselves beset with obstacles sonetimes insumiountable. Of these, nany becane disillusioned quickly and again left education. Of the few that were left, only a hanciful persisted in the effirts to establish the desired courses. The remaining yroup soon diverted their attentions frori setting up ccurses desired by industry to setting up the courses which their particular ajainistration harjened to think fit well into the schene of every iny living. For the nost part, these turned out to be personal research project type courses, unproductive ani inviluable to the students that male the mistike if taking then. Elucation becarle quite wrapped up in the business of trying to set same decent cuurses established. Intermingled with this was the perscncl desire of the particular indivinual instructor, and an unendiny avalanche of propaganha from any and all sources.

Gradually, intustry has lessened its requires.ents in the selection of personnel. This is due in most part initially to the fact that poople with training were simply nun-existent. is industry accepted lower scale personnel, it becane apparent that perheps a Dncturnte Degree in matherntics wasn't quite the most essential single pre-requisite. This fauling has swie how permeated into the education field until tuday suan of wasel that maybe even lowly college freshram just raight heve a chance of unierstaniing computers, providing, of course, that
he first attain 20 years of experience an: four college degrees.
There is still a basic cuntradiction in the aporoach to the problem by educational personnel. The zeal on the part of many educators to accomplish personal gcels, as concerns ccaputers, has caused many of these people to lose sight of their original purpose. Incustry requests well-ciefined, practically orientel courses of training. Eilucation has cone up with a hadge-pocige of anequarter courses which are, fur the must part, unrelated and unguided. Sone universities offer only one section of one course each year, and that course is usually nothing more than an intronuct.rry type of course. FORTRiN is often taught as the means of solving business problens. Systens courses can usually be defined as courses in machine caprbility raticer than in their true light.

This has been due in çreat part to the shortconings of computer education of the educators. For purposes of quick exposure, each learned about computers in his or her own field. The mathematician learned how to solve math problems and never talked to the business department. The business people learned huw to solve the accounting type probleras and never tilked to the encinuering department. The engineerinj department pecple learned to solve the stenderd stress prublem and never talked to the science departwent. The science iepartment people leamed to do some of their wcrk on the comyuters and forsot about the rest of the campus crowd completely. Hany and variei requests for equipant came to the acministrators from all of these yroups. Noun of these were coordinated nor even exposed to the scrutiny of any other departaents. People on the aministrative staffs were rather prone to allowing each and every departwent to function inderendently as in every other facet of their operations. In many cases, it was a first-com, firstserved type of operation in the acquizition of a computer. The results were, of course, chaos in the salection, ordering and installation of both the munk of junk" invalveci, and alsu the courses decided upan by the jowers to be to be offered. is is usual, a tremendous anount wes left to be desirei in setting up Data Procesainc education in vur public school systais.

The evolution of computer and data processing courses followed an almost 134
identical path in every case. First cinie the "hunk of junk." After sume semblance of study within a particular department, a computer was ordered and installed. In general, there was very, very little ccordination between the various university departaents relative to how the comizuter couli be used. In general, there was always the stipulation on the part of the adrainistration that it was to be used also for adruinistration purposes. I ara tempted to wonder if this is also true of the microscopies of the biology department, and the typewriters of the secretarial departaent and the football shoes of the athletic department.

Next cane the exaiting question, "What an I going to do with this crazy aditing wachine?" The individuals involved in the overwhelming tabk of convincing the administration to acquire a computer had spent all their time in just that, and no tine at all in the practical development of courses to be installed after the computer had been installed. The short space of time left in between finai orcler date and installation date of the computer was not at all adequate for developing a good ccurse of instruction on the machine. Result: an unrealistic approach of "Getting something tojether before the actuinistration finds out." For the must part, this turned cut to be a hurredly put $t$ cjether FORTRAN course built on the notes frial the instructors uwn attenciance at a manufacturer's short course. In sume cases, these even proved to be enough to get through a full semester cuurse. The main problea with this was the fact that this nethod was actually beiny used. Under the pretext of being toc busy with other aspects of educational life, usually because the individual hinself was still quite in the dark about what actually a connuter was all about, the stujents were thruwn the bone of sample problens from the mnnufacturer's course, while the Prof. went on his roerry way trying to find out for sure just what did hapipen when a multiply comand was given. Generally, being unfaniliar with a computer language, led to the development of many cuurses beinc put tujether on nothing more than machine lansuage. Machine lancuase and FORTRAN becane the ever present by-laws and bywords. Heny, in fact most, courses began and ented on this level.

Of particulariy significant interest to incustry was the method in which the computer itsclf was hanilci within the school operation. There semad to exist therein a fervent desire to restrain the stu.unt fron ever having ary contact whatsoever, except by reference urinc; a lecture, with the comsuicer. Perheps the administration was fearful of possible rejair costs; perhais the Profs. involved were afraid that the stuients wiuld find out which were the right buttons to jush before the Profs. did; at any rate, the actual operation of the computer center was built arcund a selected staff of gracluate students who did all the actual operations, processel any an : all student projrans, and laughei rather hideously when a logic error appeared in a student's work. The said pari of all this was that the students never did get to find out what the computer really did look like, nor what it did while in operation. On-line diacnistics and debuging techniques were never even riontioned to the stuctents for fear that some questions night be asked. Sadly enough, sorie of this was justified siniply because of tine. It would be injossible to cran intu a single quarter course any more than an exposure to a language such as FORTRAN and expect the student to get as far as writing a simgle jrugran. In a senester course, he might be exiected to write two short frix, raus, punch then into cards or tape and just akyide get theri int, the computing contor. ifter all, this was more than the Prof. haid accimillishei at the manufacturer's short course in slightly less time. It is possible to accomillish only su filucin in a 60 -hour quarter or 90 -hour semester, and this was the only interest oricinally--the one quarter or une sendester course.

Unfortunately, this is still true of almest every college anci university computer center in the country. Tuday's cfferings in courses actually amount to nothing more than a conslomeration of at is and ends which, for the most part, reflect only the lack of knowlodje on the pirt of those setting the course up. The lack of truly dilident effort is a thorn in the side of Efucation.

Just as in industry, the computer on campus becane a status symbol.
Many schools began to wear it as a badge of some sort. Other schools without a computer soon found ther.selves in a race to the wire in acquiring a "hunk of junk" 136

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and getting it into operation. It becane very fashionable to be setting up "Computing" centers; computing centers, not computer centers. The terminology was indeed indicative of understanding on the part of both faculty and acministration people as regards the computer's place in industry. It was just another machine for the solution of a particular problem, preferably a mathematical problem. The true implication of the coaputer in the nodern business and scientific world was realized by only a very few across the country. These fee comprehended the computert ramifications, but they made the significant mistake of placing the "hunk of junk" on the "graduate school level only," and, thereby, effectively eliminated almost all students. The result could only be that of ineffective application insofar as the general situation was concerned. Those nost in need of exposure to computer education could not be expused simply because they never got into graduate school.

Again, we have the situation of a Nachine languege or a FORTRAN course for under-graduates, wherain a program was limited to being writton, passed through the keyhole to the graduate student and the garbage results received back through the keyhole with a note telling the peor freshran to do it over again. In most cases, even the graduate studint on the inside nevor git to run any diagnostics of debugging on the prograsi simply because he had never been taught to. However, they did get to help the Prof. while the prof. was guing abcut getting his own computer education, so they were able t.: garner some extra tidbits of knowludge regarding coraputers.

This is where we stand in academic education today. The requests of industry have been furg:tten or relegated to the area of unir:portance, and nost on-canpus computers have been gubbled up by Profs, dcing personal research for doctorate degrees while the only effective courses are on the graduate school level. In other words, almost t.tal ineffectiveness.

The attenpts of vocaticnal schouls and area technical schcols have also been ineffective. The traditicnal approach of the wational school in training fur a specific skill has resulted in just another series of "cperator" type courses which industry has been sble to supply for many years. Vecational schools have been successful to some degree in supplying industry with adequate input trainee personnel for specific job categ:ries in the oporator jobs. These personnel still had to complete in-house, on-the-jub training after being hired by a company. True, because of their training in school, the in-hcuse OJT training programs could be significantly reduced in length.

Again a failure to coliprehend the true ramifications of computers within a business caused the vocational people to continue on their merry way setting up operator type courses in the various job cateugories of a chaputer center. All of these were specific in neture, that is, the Key Punch operator was concerned only with funching cards; the Tabulatir operator was concerned unly with prucessing the cards in a tabulatur or surter; the Conputer Conscle operator was taught to push buttons and munt taje reels; and the Progranaer was just ancther individual job concerned with writing instructions for the computer. li, Me of these categories received any additicnal triining ir even ex sure to adjacent opurational areas. Even the previous cr next upirations were left out of the triining courses.
The stress on individual jub ceteguries by the vocetional schs,ol people has relegnted the prograrmer's job to that of just anuther operator in the cycle of business events. Again, this was due to almost the sane facturs as those arising in the acadenic world. Tou little education on the pirt of faculty and administratiun led to impractical courses being set up. An unwillingness to adnit that there just might be a need firs education beyond just the "operatur" level left all related course tri:ining out. In thisse nost advanced schocls, there sanetines appeared a course in mathematics $t$., about the level of beginning algebra. Never did we find the aroa of systems being c.vored, fur this was felt to be unrealistig and, therefore, acaderi.ic in scope.

Thuse course: in "C stiputer Progrerring" which were set up followed almost exactly the efforts within the ac:demic world in difing the sarie thing. Short courses in the use of a conputer lingu:ge such as Abs lute and FORTRAN made their appearance, and were handled in virtually the same way. After an expusure to a language, the student was expected to write a progran and subject it tu the processor by way of either the Prof. of his assistant. Alriost invariably, what little hands-on experience that was provided was channeled only into the area of what buttons to push "to get the darned thing to run." All of these courses were set up on the "lab" basis, with little or no solid lecture centent. For the most part, the instructor was a converted Business Education type jersin with a specialty of office machines or typing who had bean exposed to a short course at a nanufacturer's school soniewhere. The results again were very similar to that in the colleges and universities. The principal prublem here was a reluctance to adnit that any job could have iriplications or ramifications beyond its own seemingly frmediate scope. The adninistration and faculty peuple refused to even atternt to deviate from their set ways of education and set up sune semblance of an adequate course in ccomputers.

This satisfied the requirunents for "opurator" type jeople but left the original problem conpletely unsatisfiad. The sc-called computer progranmer was nothing nure than a language coding clerk, lacking any and all knuwledge of how to really put a computer to effective use within an urganization. The Systerns Analyst dealt only with the abstract it seened, and, therefore, had no place in vocational education. Becausc of this, so-called frugraraier courses could give the student nothing rave than a language background. The coci;anies hiring these graduates found thenselves right buck where they started with their cwn in-house OJT prograras. The vucational schocls did effectively provide input trainees for operatur jobs, but left much to be desired when it cane to effectivo use of equipnent within a Data Processing center.

Computers and their effective use demand an integrated training prograni. In general, every business computer installation dejends upen a staff of persconel 139
which has had a good acaderiic background in a particular field such as Aocounting, Engineering, Matheratics, Science, etc., and also a vocational skill training in machine use and operation. Industry has fuund that it wasn't enough to juat be an accountant or engineer, a scientist or mathematician, just a systems analyst or prugranmer. It wasn't enough tu have just a high school oducation followed by quicky type operator courses. It wasn't enough to have an exposure to a quarter course in a couputer language. It wasn't encugh to apuruach a computer with simply problem solution in mind. Somehow the benefits of college or university academic training had to be molded toyether with hands-on vocaticnal training into a useful level of competency and judgrient. The far-reaching aspects of every computer application made it very desirable to provide the type of training which would allow the individual to make the utnost use of a particular "hunk of junk."

During the last two to three years, it has becone more and more apparent that more than one acadenic field had to be included as well as more than one type of computer training in any effective cucuputer ccurse. In addition to accounting, sone mathenatics, English, and statistics were very necessary. In addition to an exposure to computer progranming via learning a c:aputer language, a background in prublem analysis and s.jlution, in Symbelic languace as well as FORTRAN, in handson debugging netheds as well as ctesk checking were all vitally necessary.

Conputer operations tricining was the inauediate cuncern, and primary courses had to be directed towerd this end. However, the langer espects of conjuter ability had to be made the gal of all training. Somehuw the Methods Analyst, Systems Engineer, Computer Pruyraraier, Data Processiny Manager, Controller, Accountant, Sales Mianacjer, Production Sujerintendent, Factory Foreman, Inventory Clerk, Grounc's Keaper, and Garbage Collector had to be rolled up into a single indivicual via an effective trainins; progran.

Fran a practical standuint, this conglumeration of far apart fields had to be rolled into one, but this isn't quite possible within the short periods of tine available for training. Still it is apparent that quite a different
eruhasis in training is required. Rether than being just ancther $t \infty 01$ or method, 140.
the conjuter has becume the center of operations affecting all cther departments of an organization. No sinçle operation escaped the inevitable scrutiny of the computer. Training, therefore, had to inclute all pussible fields of endeavor so as to provide the computer personnel with as broad a scoje as possible to enable then to make sound lecisions. Exiosures to other fields had to be realistic and sound as well as effective, but these expsures had to be made within realistic time allocations.

The iressure of telescoped tinee hes nut allowed industry the luxury of retraining older staff nembers. Though these personnel had extreniely good knowledge of the organization, it cften required nore tine than we had available to bring them to a point of canpetency in cumputer utility. Additional personnel with "Wide angle" canputer backgrounds had to be discovered and acquired. Most of these carie frua the fields of either Data Processing or Systers Analysis, but even these did not have the proper backgrounds of mutliple field. The sreatest deterent to these in aclimatizirg thenselves $t$. computer operations was professional prejulice. Until comijuters, these two fiells stocd at alus with one another. This factor becane a serious restriction to further develoment with in the computer field.

The two year Data Processing Technician Curse seuns to offer soule indication of an adequate answer to the probler. The intecration of all the required facets intu a single applied course can, of course, be the only true solution to the problen of acquisition of trained, capable jersonnel. This is not going to take place very soon because of some of the reasons already mentioned. In the reantire, sone adequate substitute must be found. To ask industry to continue their con extrenely expensive training prourans is not realistic. In the first place, this is far too expensive a mole of training. Secondy, it is unrealistic in the consumption $f$ tine.

Develoments in the field of computer utility arrive sc fast and in such quantities as to render ineffective any long rance in-house, on-the-job training projram. Industry training precgrans are usually based on a set way of doing things which is expected to.continue as the way of doing things forminy years to conc. In conputer operations, this is nit at all true. Yesterday's methocl was ancient history as socn as it was used. Toriay's methex will be outroded before the job is dune tonight. Tonorrow's method is already getnering pale, green rold of disuse.

As an intemediate solution to the problen of prividing industry with adequate input personnel, the two-year technician jrograria has been suggested and put into use. These, too, have fallen into the same traps for the same reasons as the acadenic courses and the vocational cuurses. The reason for this is obvious. The very same faculty and adiuinistrative people are making the very same unintelligent decisions about this ciurse curriculum and setur.

During the last two to three years, there has taken place a yreat rush to "get on the Data Processing bandwayon." Unfortunately, the depth of sincerity here seems to go only that far. Xgain we find unacquainted admınistrative personnel and untrained instructor personnel attempting to set up and teach a totally unfaniliar curriculum. For the riost part, these attempts have been made in junior colleges and vocational schools on a post high school basis. In almost every instance a basic two year curriculum, sugcested by several of the manufacturers and approved by the U. S. Department of Health, Education and Welfare, has been tlie sum and substance of these attempts. These sugsested curriculums had been set up on a purely theoretical basis, and had not been put into practical operation before being foisted upon an unsuspecting education group. Perhaps in awe of the suggesting body, perhaps for lack of personal knowledge, perhaps for desire to be "one of the bunch," education accepted these curriculuns and attempted to do their best at training people in Deta Processing, without first doing any extensive exploration of the curriculum.

This is the point at which the most significant of failures occurs. Scrutiny of the suggested curriculums by those in Data Processing management positions in industry would perhaps have pointed out some of the most glaring inadequacies. Sone of these are: first, a purely theoretical approach to subject 142
matter without adequate experience emphasis; second, basic courses being taught last in sequence, with advanced courses coaing first; third, emphasis on language cormunications with the machine rather than a solid foundation in machine operation characteristics; fourth, relagation of the Data Processing courses to a status of just another course rather than a stantus of core course.

As an example of this, let us exanine the most anmonly found curriculura. It is set up as follows:

First Year

| First jenester | Second Seriester <br> Credit Hours |
| :---: | :---: |
| 2 | 4 |
| 4 | 4 |
| 3 | 3 |
| 3 |  |
| 5 | 3 |
|  | 4 |
|  | Fours |

Computer Progratrining I and II Social Science
Statistics
Business Organ
Cust Accounting
Systens Development and Design
Advanced Computing \& Frugranting Systens
Data Prucessing Field Project

Credit Hiours

4
4
3 Accounting I and II
Communications I and II
Unit Record liachines
Data Prucessing Applications
Introduction to Prograv.ming Systens

## Second Year

An exanination of the $c$ intent of each these Data Processing courses generally reveals the fellowing ccurse descriptions:

BASIC COIPCTILG taiCHINES. This is a survey course of coimin fundarental concepts of data processing systers. It describes the ev.lution of caputer systens--frua manual to stored progr.un metheds.

UNIT RECOPD ILSCHINES. This cuurse is a survey of unit record equipnent. It illustrates the need for machine-processable silutiuns to accounting and recordkeeping prublers. Laburitory priolens iaciude wiring of contrul panels. DATA PROCELIING APPLICATIONS. This course is designed to ecquaint the student with actual business data pricessing applications. The student learns through lecture and case studies to apply the dita processing equipaient previcusly studied to
various applications. Throuch this study, the student gains an understanding of how machines and systens are c-sbined, and the advantages of mechanization INTRODUCTION TO PROGRISIING SYBTAS. The basic cencepts of progranieing systeme are taught in this course. During this cless, the student becorues aware tha prugranaing systeas are as inpurtant as the machine hardwire. This curse familiarizes the student with the purpose and function of the variuus types of programming systens or languages.

COIPUER PROGRUIING. The Basic Confuting Machines course in the first senester provides the the,رretical basis for detailed study of data processing machines in this course. Prograraing drills, case studies and exercises serve tu bridge the gap fron the theoretical ts the practical use of data pricessing. The two hour per week laboratury sessions provide further reinforceajent of basic principles by providing "hands-on" training. The FORTRiN language is the rain media of training, while the student is intriduced to hachine Lancuage and Symbilic Programing Systen.s.

SYSTEIS DEVELOPIENT iND DESIGN. i survey course discussing the effective use of data processing equipnent in lieeting the infermation needs : f businuss. The course $s$ designed to guide the student through the virious stages of systerit develcprient. ADVINCED COLPUTING IND PROURIIIING SYSTELS. The ubjective of this course is to provide the student with sufficient kniwledge of projrawing language concepts so that he may easily master any specific systen with a minirara of instruction, nctual programaing languages are nut taught. However, individual phases of certain selected 1 inguage systeris are treated in detail in order that the student may learn advanced progranming language techniques contaimed in scphisticated systens.
Let's exanine these ciurses a little more minutely frcra the standpoint of "what is being taught when." In the first semester we have twu parallel courses, Basic Conputing lachines and Unit Recurd Nachines. The Busic Computing Machines course is almost always a pure theory c.urse exanining the varicus styles and types of machines. Little or no off ist is made $t$ a acquaint the student with the methods of probleta sulution required by ench of these types of machines. Since

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this is usually a three hour per week course, there is really no time to go beyond a tem definition stage of learning. The Unit Record Machines course is a little nore definitive in that the student dees get some mands-on" experience in control panel wiring. This, too, is very limited since the five hours per week during one senester must be spread over several types of machines and all the punched card processing philosophy involved in each of them. The student receives a total of about 20 hours per machine type. Certainly nut enough even tu cumplete the acquaintanceship status of kn wledge.

The simple fact that these two courses are so drastically limited in scope negates their desirability as foundations for further data processing courses. The Basic Ccaputing Machines course should have as its prine objective teaching the student the various methods of priblem solution used in the varivus types of conputers. Since problem solution is really the prine consideration of all suba sequent courses, and all activities involving cuaputers, it would be for more desirable to teach this tupic rather than mechanical configuration and operation in the initial course.

During the second senester, the student is exposed to sumething called Data Processing Applications. During this course, he "learns through lecture and case study to apply the dita processing equipnent previously studied" to business applications. This is all well and good, but since the Basic Conputing Machines course did nothing nore than acquaint hin with machanical configuration, this cuurse will still leave him asking "huw, what, where?" This course would be infinitely nure appropriate were it taught fullowing sone exposure to practical prugraming experience. It least, then the student would have some means by which he could relate the machines to the applications. Far too many students and yraduates come to industry knowing all about computers or language systems, but are unable to put this knowledge to work on a practical application.

Also, during this econd semester, the student is subjected to a course called "Introduction to Profromming Systems." This is basically a course which examines the various types of programing languages. It is an exploration of the 145

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"suftware" wherein the student "becones aware that procraming systems are as important as hardware." Asjain, this course is pretty nuch a theoretical one with little or no practical profranuaing experience. For the must part, the languages generally discussed are not a part of the software package of the computer which is installed. Here again, the student is left wundering "what to do with it* as concerns all of these languarjes.

So far, two full senesters have gone by and the studiant still hasn't
"soloed" on the computer." He has still to write his first practical prublem and run it on the computer. It would seers to be an awful waste of time,

Finally, in the third senester, a course called Computer Programing I shows up. Welcume at long last, even though it falls far short if its rightful goal. During this course, "prox;raming drills, case studies and exercimes serve to bridge the gap from the theoretical to the practical." This objective is perhaps a sound one, but since the FORTRAN language is generally used, with only an exposure tu Symbolic and lachine Language, it is doubtful that it can ever be reached. The FORTRIN lancuarge still gives the student no insight into data manipulations within the machine. FORTRid does not allow un-line debugying and diagnostics. FORTRAN dues nit even allow the student to develop his own prociamming losic techniques. FORTR'N limits hini entiraly tu a rigid set of rules evolved from someone else's logic. In th:se curses where hichine language is taught as the basic media, the student is severely linited by the clerical activity involved, and also by the fact that only relatively simple problems can be attempted. We find, therefore, that in the third seaster when the student should be at an advanced level, he is in reality just beginning. in examination of the nuruber of corrputers installed and in use reveals that apprcxirately $95+\%$ are used in business type operations. Why then use a mathenatical language such as FORTRAN, with all its inherent restrictions and linitations, as a training media? Why nut give the student the type of training which is going to equip him for 95\% of the job market?

In the fourth scmester, another course is given in Prosramaing Systens. 146

This usually is a survey type enurse designed as an extension of the introduction course given in the second semester. These two cuurses could well have been combined into a single course during this senester. By the tiane the fourth semester has begun, the student is just barely capable of naking effective use of the high-powered languages usually discussed in this course. The philusophy of operation involved in COBAL, iLGO and scave of the other more scphisticated languages are beyand practical cumprehension until the stuxdent has had an adequate exposure tu manipulation of data through the use of some lessor language system. The third seasester cuurse in comuter proyranaing will accomplish this to a certain dagree, but places the second semester course, "Introduction to Pro, raidainy Systens," in a wasted status.

The "Systeris Develupwent and Design" course in the fcurth semester is a practical one, though it cones a little late. Far nore emphasis needs to be placed on "the effective use of Deta Prucessing equipment in business needs." This theme must effectively be built into each and every segnent of each and every data processing course beginning with the very FIRST day of instruction. Without thia, the student in his theoretical surroundings loses sight of the practical application of what he is studying.

Because of the inadequacies of sugcested and aiopted courses, a new approach to course setup and content had to be taken. it Hibbing, we first tried to detemine what type of individual was really in demand by industry. It was all well and good for us to listen to the clains of almost everyone that the field of Data Prucessing was une of onlinaited opprtunity and a never-ending sponge which woull gather up any and all graduates of any and all types of courses. Having spent a few years in the business world, I found this quite hard to believe. We spent a great deal of time and effurt finding out what we believed in frum the first--that not just any cld one-quarter course approach would suffice; that somehow, we would have to bersin at the level of a good workable cominuter lansuage from both the practical and ejucational point of view and go un from there.

Realizing that we had opened the door to a vast area of extrencely hard 147
work, we went about the task of developing our core courses. After ruxch serious investigation as to where the computers were being used, we decided to place the emphasis of our core courses on business applicatiuns. We, therefure, asked our college instructurs in Accounting, Matherratics, Econoraics and English to put tosether a group of integrated courses sufficient to support an intensive level of training in Data Processing.

M1l courses developed were to be integrated with the Data Processing courses. The probleas discussed in the ficcounting and Hathematics courses were to be ciscussed from in intergrated computer operations point if view. The Cormunications Enylish courses were to emphasize public speaking and technical report writing, with Data Pr.cessing applicaticns as topics. These courses were accelerated versions of the same basic courses taught in our Junior College, by the sanie instructurs, but with a much different objective in sight. The level of training, therefore, was intensive, but it was also very well directed along the Data Processing lines.

The Data Processinc cuurses, built around the IBM 1620 coraputer and IBM 407 accounting machine emphasized a titel integration of Computer Programing and Systexs Analysis. No prubleri was to be discussed in the Data Processing course grouping without a thurcugh investigation of 211 the systens reanifications of the problen. In this manner, we hujed to be able to acquaint the student tu a good degree with all factors involved with a particular type of problen, and not just with "a typical proyraming"approach. The significance of the several means and nethols of problem solution was alsu brought $t$, the student in the discussion of each problem.

Early examination of the field of data processing showed that a particular type of person was in great lemand. This was a persun with more than just an exposure to machines and computer prograraning. This was a jerson with sound fundamental training in Business courses and mure than just an acquaintance with Systens Analysis and Pricelures. This was a person capable of evaluating the relative costs of several methols of problern solution and data handling and able 148

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to make a suund, profitable juisment and lecision. This was a persun capable of more than just conscle operativn, cr debugging through a list of error codes. This was a persun who locked at evory data jrocessing prublean through two sets of eyes, thuse of the Systeas Analyst and thuse of the Data Processing Technician.

To achieve satisfactorily the guxl of training this person, we put
together the following curriculum.

## Course Title

rinciples of Accounting I
Data Prucessing Mathematics
Intractuction to Computer
Unit Record Equi, ment
Cocmunications English I
Second Sernester:
Principles of iccounting II
Data Processing Mathematics I
Carmunications English II
Conputer Prugranming
Third Semester:
Cost riccounting
Human Relations
Data Processinization introxuction to iphlications

Fourth Semester:
ystens Develonnent
Advanced Prog ramaing
Data Processing Field Project


Totals

## Beginning in the first semester

Beginning in the first semester, our individual Data Prucessing course content is as follows.
UNIT RECORD EQUIPAENT. This course examines the use of must unit record fanched card machines including the key punch, verifier, scrter, reporducer, collator and accounting machines. Heavy emphasis is place on jroficiency on the IBM key punch and verifier, and on complex board wiring for buth the 085 collator and the 407 accounting nachine. Foms design for buth card fomats and printed output is also thuroughly covered. This course forms the basis for all future laboratory probllems in that the stulent must wire all necessary control panels for each machine
used in any laburatory problem solution.
INTRODUCTION TO COMPUTERS. This course is the key to success or failure in computer programing. This course is divided into three major segments each of which covers a single basic type of computer. These are Disk-Drum type machine, the Core-card prucessing machine and the Core-liaynetic Tape machine. The logical approach to problem solution for each of these basic nachine types is stressed in this course. Flow charting and detail block diayraminy of probler solution becones the stulent's central concern. The laboratory porticn of this ccurse consists of setting $u_{j}$ the IBM 1620 computer for problera processing and of console operations using 1620 user-group library prograns and problens for these programs. COIPUTER PROGRINIING. This second semester course in IBM 1620 computer procramaing forms the solid foundation on which all future proyraming courses are built. This course has the two-fold cbjective of teaching the student computer proyramaing techniques, and of acquainting the stuient with how a computer is used in business through carefully developed laboratury problems. The first three weeks of this course are devoted to the ibsclute Kachine Lanyuacse of the 1620 computer. Besic techniques of on-line debugying are also stressed during this jeriod. The remaining 15 weeks of this course are given over to the use of the 1620 Symbolic Procraming System Lancuace. Business problems of increasing conajlexity are handled as the course projresses. With each problem, the significance of the computer relative to overall systems and procosures is stressed to the stiudents. The laboratury problens are ciesigned to extend and reinfurce the basic comunter logic ideas covered in the first semester as well as tu develop proficiency in 1620 computer programing.
DFAI PROCEDSING APPLICITIONS iND INTROXUCTION TO SYSTEAS. These two parallel third senester courses bring to a practical working level all the principles of Computer Proyraming and Systems and Prucedures luarnod in the second senester The student cuntinues his Sywablic Projraming with each laboratory problem, but he now expands his operations by developing the source and handiling of all data for a particular prublem. For each laburatory jrcblen, the student develops a

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coraplete system of information handling culminated by a complex computer program necessary to arrive at desired results. Conplex applications such as incentive payrolls, complete accounts receivable processing including aging, inventory processing and item use and scrap analysis, general ledger and other integrated systems of information handling. The student also designs and develops any and all necessary documentation of the system including both manual and machine operations. The stress in these two courses is on polishing computer progranming techniques and acquiring practical systen and procedures knowledge. SYSTEIS DEVELOPMENT given as a fourth semester course continues the third semester Introduction to Systems course with heavy emphasis on the total systems concept and the development of systers and procedures throughout an organization which will support the necessary profitable operation of a computer. Discussions and laboratory problens include practical exposure to PERT and Critcal Path techniques both on and off the computer, in addition to standard systens of Information Retreival.

ADVANCED PROGRAMIING in the fourth semester consists of IEM 1401 computer Symbolic Programing training. Most basic laboratury prublens from the second and third semester Programing and Applications courses are reviewed and 1401 prugrams are written and tested solving these problens. FORTRAN is also taught during this course.

DATK PROCESSING FIELD PROJECT during the fcurth semester consists of the student actively engaging in shop operation of a local area data processing department of local industry. During this period, the student selects an information system whic: he completely documents and prugrams for the craputer. His sulution must be one which is better than the system in operation which he selects to study. The objective of training Data Frucessing technicions dictated the attainnent of a thurough kn wledge of computer operations. To achisve our desired end, we decided early in our investigations that we would utilize the Symbolic

Programing Language as our major computer instructional tool. Our foundation was to be thorough understanding of internal data handling by use of Nbsolute Machine 151

Language. The relative advantages and disadvantages were thoroughly explored and the decision fur Symbulic Language was based upon the primary requirement of solid understanding of the internal capabilities of the equipment involved. All laboratory problems were designed with hands-on assembly, testing, debugging, and processing as a significant part of the problen. A requirement for thirty clock hours of sclo time on the 1620 computer by the end of the second semester became a mandatory objective. "Console Confidence" could be attained only through personal contact with the machines. Mastery of the FORTRAN Language was also included in the curriculum, but as a secondary rather than prinary language. FORTRAN progranming, as well as 1401 Symbulic prograraming was included in the fourth semester area of the cuurse. A course in Systens Analysis was designed which emphasized methods of data handling outside of, but urientatad to computers. The how to do it approach of integrated data flow operations was tied in directly to a computer program to solve a given problem. In all cases, the discussicns of various problens included and revolved around the ramifications of a computer in the systems area. Topics in the Data Processing group of courses ranged from simple payroll type problems to integrated general ledgers; frora production control to sales analysis; from historical rec.rds to uperational research; fram infurmation retrieval to business sinulation. $i l l$ of these tupics were arranged with two things in mind; first, the huw and why of cuaputer solution; and, second, the nethod of programaing the problem within the computer.

In all computer applicatiuns, each studont was required tu do his um on-line debugging and diagncstics. Each leburatury problem required the submission of a written report on the problens which the student had enccuntered while solving the problem. This technical report had to include a curuplete explanation of the prugranuing method used, the assenbly and processing techniques, and the Diagnostic and Debugging procedures utilized by the student. The original objective of the overall outlook and integrated problen solution techniques were repeatedly brought to bear in each of the courses. Various systems and procedures of appruach were explored with each laburatory problen, and students were each 152

Page 27. encouraged to attenpt different micthods of arriving at a solution to the particular problem. No two like solutions ware to be acoepted in the computer programming phases and systens phases of the course. Individual thinking and exploration was thus encouraged to the utmost throughout the course structure. Failure on the part of the faculty to foster and nurture this aspect of student development would in reality be a failure of the entire course structure. The two year program is not the answer to the problem, and will probably soon be outmoded. The two year program came about as a stop-gap measure necessitated by the inadequate fumblings of colleges, universities and vocational schools. To date, only meager attenpts have been made to provide integrated training. Most of these have been of the too little, too late variety. Most courses of any value are on the graduate school level, where most students never appear for training. Cuurses on the undergraduate level are ineffective because of too narrow scope and FORTRAN type approaches. Much hard work remains to be done in course developrient before university, college and vocational schcol prograns offer the type of training necessary to provide industry with adequate input personnel. Without this course development work, all such procyrans will be ncthing more than a waste of time and money. Universities, culleges and vocational schools must bring thenselves to recognize the fact that conputers have becume a factual way if life fur both organizations and personnel. Withuut this, Education can never hupe to catch up to the world of reality. Where does your program stand?

## INTRODUCTION TO MATRICES

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Intended for users with no knowledge of matrices and little background in mathematics. What a matrix is, matrix operations, singular matrices, how errors arise in matrix operations. Example of matrix inversion by Gaussian elimination.

In working with simultaneous linear algebraic equations, it seems reasonable to work with the coefficients only. For example, in the system

$$
\begin{array}{r}
x+3 Y=4 \\
2 X-9 Y=-7
\end{array}
$$

We would expect to find the solution values by some set of operations on the numbers

$$
\begin{array}{rrr}
1 & 3 & 4 \\
2 & -9 & -7
\end{array}
$$

Indeed we would expect to find the same solution values if the equations were

$$
\begin{array}{r}
a-3 b=4 \\
2 a-9 b=-7
\end{array}
$$

It now seems reasonable to make the following definition:
A rectangular array of numbers is called a matrix.

> Ex.:

$$
\left[\begin{array}{rrr}
1 & 3 & 4 \\
2 & -9 & -7
\end{array}\right]
$$

The size of a matrix is characterized by the number of rows and the number of columns.

$$
2 \times 3
$$

A matrix consisting of exactly one row or exactly one column is called a vector.

$a_{i}$ denotes the element in the $i$-th row and $j$-th column of a matrix.

$$
a_{21}=2
$$

$a_{i}$ denotes the $i$-th element of a vector.

$$
\left[\begin{array}{ccc}
1 & 3 & 4 \\
2 & -9 & -7
\end{array}\right]\left[\begin{array}{ll}
a_{2}=-7 \\
a_{11} & a_{12} \\
a_{21} & a_{13} \\
21 & a_{22}
\end{array} a_{23}\right]\left\|\left\|a_{i_{j}}\right\|\right\|,\left[\begin{array}{l}
a_{i_{i}}
\end{array}\right]\left(\begin{array}{l}
\left.a_{i_{j}}\right), \quad \text { A are }
\end{array}\right.
$$

equivalent symbols to denote a matrix.
Definition: Two matrices are equal if and only if they have the same size and correspondingly placed elements are equal.

We will define a multiplication process by introducing the concept of linear substitutions to matrices. Suppose we are given the set of equations:

$$
\begin{aligned}
3 x+2 y+7 z & =a \\
2 x-y-3 z & =b \\
x+y+z & =c
\end{aligned}
$$

In matrix form this looks like:

$$
\left[\begin{array}{rrr}
3 & 2 & 7 \\
2 & -1 & -7 \\
1 & 1 & 1
\end{array}\right]\left[\begin{array}{l}
x \\
y \\
z
\end{array}\right]=\left[\begin{array}{l}
a \\
b \\
c
\end{array}\right]
$$

For the present, this means:

$$
\left[\begin{array}{lll}
\text { coefficients }
\end{array}\right] \times\left[\begin{array}{lll}
x^{\prime} s, & y^{\prime} s, & z^{\prime} s
\end{array}\right]=\left[\begin{array}{lll}
a^{\prime} s, & b^{\prime} s, & c^{\prime} s
\end{array}\right]
$$

Later we will show that the form used is consistant with our definition of multiplication.

Now suppose further that:

(2)

It would not be very helpful to use this thing called a matrix unless we could substitute from equation (2) into equation (1) and obtain

$$
\left[\begin{array}{rrr}
3 & 2 & 7  \tag{3}\\
2 & -1 & -3 \\
1 & 1 & 1
\end{array}\right]\left[\begin{array}{rr}
1 & 1 \\
2 & -1 \\
1 & -3
\end{array}\right]\left[\begin{array}{l}
u \\
v
\end{array}\right]=\left[\begin{array}{l}
a \\
b \\
c
\end{array}\right]
$$

We would also like to believe that this represents the same relationships that would be obtained if we had performed the actual substitutions and written the results in matrix form. The steps in making the substitutions are:

$$
\begin{align*}
& 3(u+v)+2(2 u-v)+7(u-3 v)=a \\
& 2(u+v)-1(2 u-v)-3(u-3 v)=b \\
& 1(u+v)+1(2 u-v)+1(u-3 v)=c \\
& (3 \cdot 1+2 \cdot 2+7 \cdot 1) u+(3 \cdot 1+2 \cdot(-1)+7 \cdot(-3)) v=a \\
& (2 \cdot 1-1 \cdot 2-3 \cdot 1) u+(2 \cdot 1-1 \cdot(-1)-3 \cdot(-3)) v=b  \tag{4}\\
& (1 \cdot 1+1 \cdot 2+1 \cdot 1) u+(1 \cdot 1+1 \cdot(-1)+1 \cdot(-3)) v=c \\
& 14 u-20 v=a \\
& -3 u+12 v=b \\
& 4 u-3 v=c  \tag{5}\\
& \qquad\left[\begin{array}{rr}
14 & -20 \\
-3 & 12 \\
4 & -3
\end{array}\right]\left[\begin{array}{l}
u \\
v
\end{array}\right]=\left[\begin{array}{l}
a \\
b \\
c
\end{array}\right]
\end{align*}
$$

We want (3) and (5) to say the same thing. Multiplication will defined so that

$$
\left[\begin{array}{rrr}
3 & 2 & 7 \\
2 & -1 & -3 \\
1 & 1 & 1
\end{array}\right]\left[\begin{array}{rr}
1 & 1 \\
2 & -1 \\
1 & -3
\end{array}\right]=\left[\begin{array}{rr}
14 & -20 \\
-3 & 12 \\
4 & -3
\end{array}\right]
$$

By examining (4), we can see the manner in which the product matrix should be formed.
(a) Each element of the product matrix is the sum of three products. (b) Each product contains one factor from the left matrix and one from the right.
(c) Elements of the $i$-th row of the product matrix are formed from elements of the $i-t h$ row of the left matrix.
(d) Elements of the j-th column of the product matrix are formed from elements of the $j$-th column of the right matrix.

If $a_{i j}, b_{i j}$ and $c_{i}$ are typical elements of the matrices $A, B$, and $C$ where $A$ is the driginal coefficient matrix, $B$ is the substitution matrix and $C$ is the product matrix then

$$
c_{i_{j}}=\sum_{k=1}^{3} a_{i_{k}} b_{k_{j}} \quad i=1,2,3 \quad j=1,2
$$

In general: IF $A_{r x s}$ and $B_{s \times t}$ are multiplied, the result is given by

$$
A_{r \times s} B_{s \times t}=C_{r \times t}, c_{i_{j}}=\sum_{k=1}^{s} a_{l_{k}} b_{k_{j}}, i=1,2, \cdots, r, j=1,2, \cdots, t
$$

Notice that matrix multiplication is not defined unless the number of columns of the left matrix equals the number of rows of the right matrix. Even when such multiplications are defined, it is not true in general that $\mathrm{AB}=\mathrm{BA}$. Examples:

$$
\begin{array}{ccc}
{\left[\begin{array}{ll}
1 & 2 \\
3 & 4
\end{array}\right]} & {\left[\begin{array}{rr}
1 & -1 \\
0 & 2
\end{array}\right]=\left[\begin{array}{ll}
1 & 3 \\
3 & 5
\end{array}\right]} & {\left[\begin{array}{l}
1 \\
2
\end{array}\right]\left[\begin{array}{ll}
3 & 4
\end{array}\right]=\left[\begin{array}{ll}
3 & 4 \\
6 & 8
\end{array}\right]} \\
{\left[\begin{array}{rr}
1 & -1 \\
0 & 2
\end{array}\right]\left[\begin{array}{lr}
1 & 2 \\
3 & 4
\end{array}\right]=\left[\begin{array}{rr}
-2 & -2 \\
6 & 8
\end{array}\right]} & {\left[\begin{array}{ll}
3 & 4
\end{array}\right]\left[\begin{array}{l}
1 \\
2
\end{array}\right]=\left[\begin{array}{ll}
1 & 1
\end{array}\right]} \\
& {\left[\begin{array}{rr}
1 & 2
\end{array}\right]} & \left.\begin{array}{ll}
1 & -1
\end{array}\right]=\left[\begin{array}{ll}
1 & -2
\end{array}\right] \\
& {\left[\begin{array}{rr}
1 & 0 \\
0 & -1
\end{array}\right]\left[\begin{array}{ll}
1 & 2
\end{array}\right] \text { is not defined }}
\end{array}
$$

When the multiplication is defined $\quad A(B C)=(A B) C$
The proof is omitted here but it can be shown to be true by applying the definition of multiplication twice to each side to determine the typical element.

We can see that our original matrix equations are consistant with this definition.
A square matrix with l's on the diagonal and zeros elsewhere is called the identity matrix. If there are $n$ rows and columns, it is denoted by In. When no confusion is apt to arise about size, the subscript is dropped.

Thm For every matrix $A, A I=A$ and $I A=A \quad$ (The size of $I$ may have to be adjusted if $A$ is not square)

Proof Let $\left(a_{i_{j}}\right)=A,\left(b_{i_{j}}\right)=1$ then $b_{i_{j}}=0$ unless $i=j$ and $b_{i i}=1$.

> consider a typical element in the product AI:

$$
\sum_{k=1}^{n} a_{i_{k}} b_{k_{j}}=a_{i_{j}} \begin{aligned}
& \text { The only term in the summation that survives is the } \\
& \text { one for } \left.k=j \text { (otherwise } b_{k_{j}}=0\right) . \\
& \text { This leaves } a_{i j} b_{j j}=a_{i_{j}} \quad l=a_{i_{j}}
\end{aligned}
$$

The other half of the theorem is proved in an analagous manner.
For some matrices $A$, there exist corresponding matrices $B$ having the property that $A B=I$. When this occurs $B$ is said to be a right inverse of $A$ ( $A$ is a left inverse of $B$ ). If $A$ is square then $A B=B A=I$. $\quad \bar{B}$ is the inverse of $A$ and $i s$ usually denoted by $B=A^{-1}$. Just statement - no proof here.

## $\left[\begin{array}{ll}1 & 2 \\ 2 & 5\end{array}\right]\left[\begin{array}{rr}5 & -2 \\ -2 & 1\end{array}\right]=\left[\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right]=\left[\begin{array}{rr}5 & -2 \\ 2 & 1\end{array}\right]\left[\begin{array}{ll}1 & 2 \\ 2 & 5\end{array}\right]$

A diagonal matrix is a square matrix with all non-diagonal elements equal to zero The identity matrix $I$ is a special case

$$
\left[\begin{array}{rrr}
1 & 0 & 0 \\
0 & 0 & 0 \\
0 & 0 & -7
\end{array}\right] \text { is a diagonal matrix }
$$

The multiplication of a matrix by a number is called scalar multiplication. The multiplier is called a scalar and the product matrix is obtained by multiplying each

$$
\text { IF } A=\left[\begin{array}{lll}
1 & 2 & 3 \\
6 & 5 & 4
\end{array}\right] \text { then } \quad 7 A=A 7=\left[\begin{array}{ccc}
7 & 14 & 21 \\
42 & 35 & 28
\end{array}\right]
$$

incidentally, the elements of a matrix are scalars too.
A scalar matrix is a diagonal matrix with all diagonal elements equal.
The identity matrix is a special case

$$
\left[\begin{array}{ccc}
-3 & 0 & 0 \\
0 & -3 & 0 \\
0 & 0 & -3
\end{array}\right] \text { is a scalar matrix }
$$

For every square matrix $A$ and every scalar matrix $S$ of the same size $A S=S A$
When the terms are defined $\quad(A B)^{-1}=B^{-1} \cdot A^{-1}$

$$
\left(B^{-1} A^{-1}\right)(A B)=\left[\left(B^{-1} A^{-1}\right) A\right] B=\left[B^{-1}\left(A^{-1} A\right)\right] B=\left(B^{-1} B\right)=I
$$

so $\left(B^{-1} A^{-1}\right)$ is the inverse of $(A B)$
Addition of matrices is accomplished by adding correspondingly placed elements. It is obvious then that the matrices must be of the same size.

$$
\begin{aligned}
& A+B=C \quad \text { if } \quad c_{i_{j}}=a_{i_{j}}+b_{i_{j}} \\
& {\left[\begin{array}{lll}
1 & 2 & 3 \\
6 & 5 & 4
\end{array}\right]+\left[\begin{array}{rrr}
1 & 0 & -1 \\
2 & 1 & 2
\end{array}\right]=\left[\begin{array}{lll}
2 & 2 & 2 \\
8 & 6 & 6
\end{array}\right]}
\end{aligned}
$$

Properties of addition: When the operations are defined
(1) $\mathrm{A}+(\mathrm{B}+\mathrm{C})=(\mathrm{A}+\mathrm{B})+\mathrm{C}$
(2) $\mathrm{A}+\mathrm{B}=\mathrm{B}+\mathrm{A}$
(3) $A+Z=Z+A=A$ (where $Z$ is of proper size and all elements are zero)
(4) For every matrix $A$ there is a matrix $B=(-1)$ A such that

$$
A+B=B+A=0 . \quad B \text { is usually denoted by }-A \text {. }
$$

When the operations are defined $A(B+C)=A B+A C$

$$
\text { and }(A+B) C=A C+B C \text {. }
$$

Suppose we are presented with matrices $A_{3 \times 5}, B_{5 \times 7}, C_{5 \times 7}$ and we wish to determine $D=A(B+C)$. The following computer program will accomplish this.

The matrix $B$ will be lost in the process.
DIMENSION $A(3,5), B(5,7), C(5,7), D(3,7)$

## 

C
C
NOW TO ADD B AND C

\section*{| 0 | 2 | $1=1,5$ |
| :--- | :--- | :--- |
| 00 | 2 |  |}

$2 \begin{aligned} & D 0 \\ & B(1, J)=B(1, J)+C(1, J)\end{aligned}$
$C$
$C$
$C$
NOW TO MULTIPLY a tIMES THE SUM
$\begin{array}{lll}\text { DO } & 3 & \quad l=1,3 \\ \text { DO } & 3 & J=1,7\end{array}$
$D(1, J)=0$
$3 D(1, J)=D(1, J)+A(1, K) * B(K, J)$
C
C
C
NOW TO PRINT THE RESULTS
PRINT $4,((D(1, J), J=1,7), I=1,3)$
FORMAT $(5 E 15.8 / 2 E 15.8 / i /)$
FORMA
STOP
END

$$
-6-159
$$

Now let's start looking for this nebulous thing $A^{-1}$. Remember - it doesn't always exist. Suppose we are presented with

$$
A=\left[\begin{array}{lll}
2 & 3 & 4 \\
3 & 1 & 2 \\
2 & 4 & 5
\end{array}\right] \quad \text { and we wish to determine } . \quad A^{-1}=B=\left[\begin{array}{lll}
b_{11} & b_{12} & b_{13} \\
b_{21} & b_{22} & b_{23} \\
b_{31} & b_{32} & b_{33}
\end{array}\right]
$$

This is equivalent to solving three sets of simultaneous equations

$$
\left[\begin{array}{lll}
2 & 3 & 4 \\
3 & 1 & 2 \\
2 & 4 & 5
\end{array}\right]\left[\begin{array}{lll}
b_{11} & b_{12} & b_{13} \\
b_{21} & b_{22} & b_{23} \\
b_{31} & b_{32} & b_{33}
\end{array}\right]=\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right]=\left\{\begin{array}{l}
{\left[\begin{array}{lll}
2 & 3 & 4 \\
3 & 1 & 2 \\
2 & 4 & 5
\end{array}\right]\left[\begin{array}{l}
b_{11} \\
b_{21} \\
b_{31}
\end{array}\right]=\left[\begin{array}{l}
1 \\
0 \\
0
\end{array}\right]} \\
{\left[\begin{array}{lll}
2 & 3 & 4 \\
3 & 1 & 2 \\
2 & 4 & 5
\end{array}\right]\left[\begin{array}{l}
b_{12} \\
b_{12} \\
b_{22} \\
b_{32}
\end{array}\right]=\left[\begin{array}{l}
0 \\
1 \\
0
\end{array}\right]} \\
{\left[\begin{array}{lll}
2 & 3 & 4 \\
3 & 1 & 2 \\
2 & 4 & 5
\end{array}\right]\left[\begin{array}{l}
b_{13} \\
b_{23} \\
b_{33}
\end{array}\right]=\left[\begin{array}{l}
0 \\
0 \\
1
\end{array}\right]}
\end{array}\right.
$$

If we choose the elimination technique, we can solve the three sets simultaneously since the operations depend only on the coefficients. Writing the constants in a rectangular array:

|  |  |
| :--- | :--- |
| Dividing the first equation in each set by the leading <br> coefficient (2) we get | $\left[\begin{array}{cccccc}2 & 3 & 4 & 1 & 0 & 0 \\ 3 & 1 & 2 & 0 & 1 & 0 \\ 2 & 4 & 5 & 0 & 0 & 1\end{array}\right]$ |
| Copying the first equations: then subtracting 3 times <br> the first from the second: and then 2 times the first <br> from the third. | $\left[\begin{array}{cccccc}1 & 3 / 2 & 2 & 1 / 2 & 0 & 0 \\ 3 & 1 & 2 & 0 & 1 & 0 \\ 2 & 4 & 5 & 0 & 0 & 1\end{array}\right]$ |
| Interchange 2nd and 3rd equations in each set. | $\left[\begin{array}{cccccc}1 & 3 / 2 & 2 & 1 / 2 & 0 & 0 \\ 0 & -7 / 2 & -4 & -3 / 2 & 1 & 0 \\ 0 & 1 & 1 & -1 & 0 & 1\end{array}\right]$ |
| Subtract $3 / 2$ of 2nd from 1st <br> Subtract $-7 / 2$ of 2nd from 3rd | $\left[\begin{array}{cccccc}1 & 3 / 2 & 2 & 1 / 2 & 0 & 0 \\ 0 & 1 & 1 & -1 & 0 & 1 \\ 0 & -7 / 2 & -4 & -3 / 2 & 1 & 0\end{array}\right]$ |
|  | $\left[\begin{array}{lccccc}1 & 0 & 1 / 2 & 2 & 0 & -3 / 2 \\ 0 & 1 & 1 & -1 & 0 & 1 \\ 0 & \theta & -1 / 2 & -5 & 1 & 7 / 2\end{array}\right]$ |

What have we accomplished thus far
Let's interpret that portion which represents the first set of equations


By looking at the second and third sets of equations we can see that
$\mathrm{B}=\left[\begin{array}{rrr}-3 & 1 & 2 \\ -11 & 2 & 8 \\ 10 & -2 & -7\end{array}\right] \quad$ This Means $\quad\left[\begin{array}{lll}2 & 3 & 4 \\ 3 & 1 & 2 \\ 2 & 4 & 5\end{array}\right]\left[\begin{array}{rrr}-3 & 1 & 2 \\ -11 & 2 & 8 \\ 10 & -2 & -7\end{array}\right]=\left[\begin{array}{lll}1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1\end{array}\right]$
How did we do it? We wrote the given matrix and appended the identity on the right. We transformed the given matrix into the identity using only the following operations.

1. Multiplication of a row by a constant.
2. Interchange of two row $s$.
3. Addition of a multiple of a row to a different row.

By carrying out these same operations on the identity, it was transformed into the identity.

While no special order is necessary, only these operations are valid.

## ILL-Conditioned Sets of Simultaneous Linear Algebraic Equations

Suppose we are presented with the system:

$$
\begin{aligned}
& \mathrm{L}_{1}=10 \mathrm{x}_{1}+7 \mathrm{x}_{2}+8 \mathrm{x}_{3}+7 \mathrm{x}_{4}=32 \\
& \mathrm{~L}_{2}=7 \mathrm{x}_{1}+5 \mathrm{x}_{2}+6 \mathrm{x}_{3}+5 \mathrm{x}_{4}=23 \\
& \mathrm{~L}_{3}=8 \mathrm{x}_{1}+6 \mathrm{x}_{2}+10 \mathrm{x}_{3}+9 \mathrm{x}_{4}=33 \\
& \mathrm{~L}_{1}=7 \mathrm{x}_{1}+5 \mathrm{x}_{2}+9 \mathrm{x}_{2}+10 \mathrm{x}_{1}=31
\end{aligned}
$$

Suppose further that we have by some means arrived at an approximation to the solution: $x_{1}=9.2, x_{2}=-12.6, x_{3}=4.5, x_{4}=-1.1$
How good is it? Is it acceptable? We can substitute these values into the left members above and see if the equations are satisfied. This gives:

$$
\begin{aligned}
& \mathrm{L}_{1}=32.1 \\
& \mathrm{~L}_{2}=22.9 \\
& \mathrm{~L}_{3}=33.1 \\
& \mathrm{~L}_{4}=30.9
\end{aligned} \quad \text { worst relative error } \quad \frac{1}{230} \approx .43 \%
$$

This looks like it might be acceptable. The worst error is less than $1 / 2 \%$. But is it? The true solution is: $x_{1}=1, x_{2}=1, x_{3}=1, x_{4}=1$.

## The worst error is $1360 \%$. That is not acceptable. What constitutes an accept able criterion? It depends upon why the problem is being solved but some possibilities are:

(a) Make the residuals small. (the first test applied)
(b) Make the solution nearly exact. (the second test applied)
(c) Determine numbers such that only a small change in the coefficients is necessary to make the solution exact.

Unfortunately b) is usually the test which must be satisfied.

A FAMILY OF TEST MATRICES

$$
\begin{aligned}
& \text { University of Alberta, Calgary, Alberta, Canada }
\end{aligned}
$$

A family of test matrices with the following properties is here described: (a) An explicit inverse is given, (b) The characteristic polynomial is easily obtained, (c) A large measure of control over the eigenvalues is possible, (d) In special cases the eigenvalues and eigenvectors can be given explicitly, and the P-condition number can be arbitrarily assigned.

Consider a matrix of the form $Q=\left[\begin{array}{ll}S & R \\ C & D\end{array}\right]$, where $S$ is a scalar, $R$ is a row-matrix $\left\{r_{2}, r_{3}, \ldots, r_{n}\right\}, C$ is a column-matrix $\left\{c_{2}, c_{3}, \ldots, c_{n}\right\}^{T}$ and $D$ is a diagonal matrix with elements $d_{2}, d_{3}, \ldots, d_{n}$. By use of the bordering method [l] the inverse is found to be $Q^{-1}=\left[\begin{array}{cc}S^{\prime} & R^{\prime} \\ C^{\prime} & M^{\prime}\end{array}\right]$, where each submatrix of $Q^{-1}$ has the same form as the corresponding submatrix of $Q$, except that $M^{\prime}$ is generally not diagonal. Letting the subscripts of $R^{\prime}, C^{\prime}, M^{\prime}$ run from 2 to $n$, we find that

$$
\begin{aligned}
& s^{\prime}=1 /\left[S-\sum_{2}^{n} r_{i} c_{i} / d_{i}\right], \quad c_{i}^{\prime}=-s^{\prime} c_{i} / d_{i}, \quad r_{i}^{\prime}=-s^{\prime} r_{i} / d_{i} \\
& M_{i j}^{\prime}=\left[\delta_{i j}-c_{i} r_{j}^{\prime}\right] / d_{i}
\end{aligned}
$$

where $\delta_{i j}$ is the Kronecker delta. The inversion can be performed in $2(n-1)(n+2)+1$ long operations; it might be possible to improve this figure with some ingenuity.

The eigenvalue problem. Let $\lambda$ be an eigenvalue of $Q$, and let $\bar{x}=\left\{1, x_{2}, \ldots, x_{n}\right\}^{T}$ be the associated eigenvector. This leads to the following set of $n$ equations:

$$
s+\sum_{2}^{n} r_{i} x_{i}=\lambda, \quad c_{i}+d_{i} x_{i}=\lambda x_{i} \text { for } i \geq 2
$$

On eliminating the $x_{i}$ we obtain
(1) $\quad S+\sum_{2} r_{i} c_{i} /\left(\lambda-d_{i}\right)-\lambda=0$.

If we write $\Pi(\lambda)=\frac{\pi}{2}\left(\lambda-d_{i}\right), \quad \pi_{i}(\lambda)=\pi(\lambda) /\left(\lambda-d_{i}\right)$, then on clearing the fractions in (1) we obtain
(2) $\quad(\lambda-S) \Pi(\lambda)-\sum_{2}^{n} r_{i} c_{i} \Pi_{i}(\lambda)=0$.

This is the characteristic equation. The following statements can be made concerning the eigenvalues:
(A) If all $r_{i} c_{i}>0$ and all $d_{i}$ are distinct, then all the eigenvalues are real and are separated by the $d_{i}$.
(B) If all $d_{i}$ are equal to $d$, then there are $n-2$ eigenvalues equal to $d$; the remaining two are zeros of the quadratic function $\lambda^{2}-(S+d) \lambda+S d-\sum_{2}^{n} r_{i} c_{i}$. These zeros are real if, and only if, $(S-d)^{2}+4\left[r_{i} c_{i} \geq 0\right.$.
(C) If all $d_{i}$ are equal to $d$, then the eigenvectors associated with the multiple eigenvalue d have zero as their first component, and they are orthogonal to the vector $\left\{0, r_{2}, \ldots, r_{n}\right\}$. Eigenvectors corresponding to the other two eigenvalues are $\left\{\lambda_{p}-d, c_{2}, \ldots, c_{n}\right\}$, where $\lambda_{p}$ is a zero of the quadratic given in (B).

Proof of (A). Let $H(\lambda)$ denote the left side of (1), and let $\left\{d_{i}^{\prime}\right\}$ denote a reordering of the $\left\{d_{i}\right\}$ so that $d_{i}^{\prime}<d_{i+1}^{\prime}$. We note that $H(\lambda)$ is continuous in any interval which does not enclose any of the $d_{i}^{\prime}$, and that for sufficiently small $\varepsilon H\left(d_{i}^{\prime}+\varepsilon\right)>0$ and $H\left(d_{i+1}^{\prime}-\varepsilon\right)<0$. Hence there is a zero of $H(\lambda)$ between each consecutive pair of the $\left\{d_{i}^{\prime}\right\}$; moreover since $H(-\infty)>0$ and $H(-)<0$, there are two more real zeros of $H(\lambda)$ outside the interval ( $d_{2}^{\prime}, d_{n}^{\prime}$ ).

# THE IBM 1620 AS AKALITICAL ARD PRE-CONPOSITIOMAL ADD II 12-TORE MUSIC 

Proof of (B). If all the $d_{i}$ are equal to $d$, then $\Pi(\lambda)=(\lambda-d)^{n-1}$ and $\Pi_{i}(\lambda)=(\lambda-d)^{n-2}$. The characteristic equation (2) then reduces to $(\lambda-d)^{n-2}\left[(\lambda-S)(\lambda-d)-\int_{2}^{n} r_{i} c_{i}\right]=0$. The discriminant of the quadratic factor is $(S-d)^{2}+4\left[r_{i} c_{i}\right.$. Statement ( $C$ ) may be directly verified.

The P-condition number, i.e. the largest absolute ratio to two eigenvalues [2], can most conveniently be assigned by letting $d_{i}=d_{i}$ then, using statement ( $B$ ), we can choose $S$ and $\sum r_{i} c_{i}$ in such a way as to assign any desired zeros to the quadratic; hence any desired maximum ratio of eigenvalue magnitudes may be procured.

Remarks. If the inverse matrices are included along with the original family, then we have freedom within the family to specify sparse, non-sparse, symmetric, non-symmetric, well- or illconditioned matrices; furthermore we can require that the eigenvalues shall be all real or mixed real and complex. This should provide sufficient versatility for most test purposes.

## REFERENCES

1. FADEEVA, V. N., Computational Methods of Linear Algebra. Dover New York, 1959
2. MARCUS, M., Basic Theorems of Matrix Theory, N.B.S. Appl. Math. Ser. 57, i960.

Bofatre University
computare centere
1620 Users Group Mo. 1320

*     *         *             *                 *                     *                         * 

Time reguired for presentation: 20 nimute
Special projection equipment required: map recorder, overhead projector
*******

In the early 1920's the Austrian musichan Arnold Sohoenberg evoived a compooltional

 pitch classea in the chromate acale are arranged in some specific erder called a "toce rem", "rom" or "series". The total number of rowe posadble, by the way, is $12!$ i.e.s 479,001,600.

The row is a constant group of relationshipe for a particuler compoaition and all aspecte of pitah arganisation derive fros itt two or more aequential pitches played succesaively eroate melody; two or mose sequentinl pitches played aimitenoously areate harnody.

When reed foruard (from left to right) the row is seld to be in ite "original" or "prime" form. Reed beckwerds the row in in ite "rotrogredo" form-an irror inge. Another mirrer image-cthe inversion-ais ereated by altering the direction af each
 goore pitch on, ite invorsion will lie three semi-tenes belaws if pitch \#3 lies one

## Tho IEM 1620 An Amantional And Pro-Compocitional Aid in 12-Tone Muence (Cont'd.)

semi-tone below pitch $/ 2$, ite inversion will lie one send-tone above. A backnard reading of the inveraion gives the retrograde inveraion. These four form of the same row-prine, rotrogrede, inversion and retrogrede inversion-econatitute the mbasic setr". Rech basic eet is capeble of being moved-uthat 1s, transposed--from ite own pitch lovel to overy other pitoh lovel of the chromatic ecale, twolve plich levels in all. Thene fortymaight apecifle pitch eederinge are spemand by oce row. The compoear choces from amoge the forty-aight in any ardor he sees IIt.

Mifiton Babuitt of Princeton Onivorsity hae shown that the four original form of the row pive all tranepositions have the propertise of a set and may be atated as a matrix. Rathoor than labal the first pitch in the prime form $N$, the acond pitch $N$, and 00 on, let us desiduate wech pitch by its send-tocol distance from pitch $n$, whieh is set at saro. Shace our intorest is in pitch clamsee rathor than specific pitchos (ill c's have the gase valve, all P sharge have the came valoe, all B flats have tho same value, ote.), let we aleo arbitrarily aspue $C$ to be pitch fil with the vilue of sere. In our prosent equally tempered tuning ayotem, $C$ sharp and $D$ flat ase the game pitch and lie one acmi-tose above $C$, thereby havise the value of $1 . D$ bas the value of 2 , D sharp and 5 flat the value of 3, $B$ the value of 4 , etc. $B$, one acmi-tone below $C$, is also eleven ami-tones above, and therafore bes the valne of 11 。

As the distance betwean any two pitches aan mover be leas than sero, and as any powitive valwe greater than 11 duplicatea a pitah cleas in the sero to 11 ranga, it followe that we are 13 inded to whole mumbere with base 12.

A $12 \times 12$ pitch matolx can thus be atated in purely aritimetical torme. Bach rank is both prime and retrograde forve at one of the trolve pitch levels, each colum is both inveralea and rotrograce invarsion forme at one of the twoive piteh levele. Since the matrix sheme all row possibilities in compect form and at a glanco, its value to both 167
the 12-tone composer and musical analyst is obvious. Bat while the 144 celle of the matrix may be filled in by "hand", the Job is a todious one, taking 20 minates, with 132 initial possibilities for orror. It somed worthmile, therefore, to progran the conpatar to produce a metrix from a given row.

Mr. Lowry $I_{n}$ Meloe, Asasistant Directore of the Hofatre Oniversity Compater Center, guided, instrected, holped and sustaired me while I atrageled with the problim. Cortain refinomats were added as we weat aloog, an followes

1. Since ach pitch class alrady had an aseigued value, it wae no longer necessary to start aseh row udth sero. The troive cards of the data deck, each with a numbor from eaco to 11, may be placed in the Read Hoppor in any order.
2. The matix is stated in three formes as a set of numbers as a sot of pitch classes desifgrated by the lettors of the marical alphabet from $A$ to $O$, in their nataral and sharp variente (the plus sign substitutes for the aharp); and as a sot el pitoh classea frem a to $O$ in their metural and flat variants (the wine aign subetitutes for the flat).
3. An intersesting phenommon, whioh can be usefal to the 12-tocio pompowers ia the ability of cortain row forms to combine and create permatations. Georce Rochberg of the luivarsete of Peansyivanta ham dovised an arithmotical teat for this. An ode number frem 1 to 11 is added as a constant to asch of the tirat eix veluce in the prime form which begine with soro. The ame conetant is then added to every pair of the same six values. If the sua in each inetance is neithor 12 nor 24 , the first six valuce (that is, the first helf) of the prime form and the first haif of the invorsion will combine and create a 12-tone pormetation at the aced-tore distapce of the constent. The ececod halves of both prime and invaresion will also combine in the sam mamer. The result is of courss tranoposable to all pitch levels. The progrm devised by Hro Feriee and ayself parforms this operation and supplies the realt in thome instances where the result is positive.

## 3.

(3)

## - 2 -

Delivered to the 1620 Users Group Meeting, 1964, in Chicago.

## Wgic_Theorem Detection Program

The program is designed to take conventionally written (1.e., not in a bracket-free notation) well formed formulae (WFF) of the propositional calculus as input, test them for theoremhood, and state the result as output. There are several subsidiary output results possible. Input and output are via the typewriter. The program is written in SPS for the IBM 1620 computer. It uses about 5500 cores and consists in about 400 commands plus storage.

Conditions of use: The original WFF may contain only three primitive varlables ( $P, Q, \& R$ ) and four operators (those for conjunction, disjunction, implication $\&$ negation). The WFF may be up to 49 symbols in length and may contain up to seven pairs of brackets. Thus the WFF which may be processed conform to the requirements of a fully developed propositional calculus and there is, in any case, no theoretical difficulty in extending the range of WFF which may be processed. The computer does not take all the conventional logical symbols and the following symbolisation has therefore been used: disjunction '+', conjunction '.', implication '/', negation '-'.

The rules for WFF are formulated in different ways for the propositional calculus. The following formulation is used here: Any primitive variable is well formed. If anything which is a WFF is designated by $X, Y$, etc., then: -X is well formed; ( $\mathrm{X} . \mathrm{Y}$ ) is well formed; $(X+Y$ ) is well formed; $(x / Y)$ is well formed. The brackets round the whole of a WFF to be tested for theorembood need not be included, e.g., $P /(P+Q)$ may be tested for theoremhood as it stands. It should be noticed that ( $P \cdot Q . R$ ), $(P+Q+R)$, etc. would not be well formed in this formulation but would have to be written ( $\left.P_{0}\left(Q_{0} R\right)\right),((P+Q)+R)$, atc. These rules are entirely typical for a propositional calculus.

The program operates as follows (see attached sheet for sample): It announces itself and invites typein of a WFF. It then types the result. The following subsidiary results may be obtained on the Consul switchess (1) By well known theorems of the propositional calculus, any number of negatives greater than one ('stacked negatives') before a WFF may be reduced to one or none. On switch 1 , the original WFF is typed without stacked negatives. (2) The mothod of processing employed is to break the original WFF down into a two variable form, the computer supplying new variables where required. These new variables themselves stand for which are broken down in the same way. The effect is to produce a two variable list in which no brackets are required (they are not required for the same reason that brackets are not needed round the whole of a WFF to be tested); the first item in the list is the original WFF in two variable form and the subsequent items define the new variable or variables introduced by the computer. This process continues until all the introduced variables are defined. On switch 2, the list is tyed, with each introduced variable explicitly defined. (3) The method employed in the logic section of the program is to build a truth-table, with a set of values for each variable, primitive or defined. On switch 3 this table, or a desired portion of it, can be obtained. The operator types in a variable and the computer gives the associated set of values; by typing in all the variables used or introduced by the computer, plus ' $F$ ' for the original WFF, a complete table is obtained. The table is biniary, containing either 01 (true) or 00 (false) in each of its eight columns; if the WFF being tested is a theorem, the table will contain eight entries of 01 for the original WFF. Typing in ' $N$ ' returns the computer to the main programo

LOGIC THEOREM DETECTION PROGRAM - WHEATLEY, FHILOSO: HY, QUEELSS, HOV 1963

```
YPPE IN WFF
(P/-Q)/(Q/-P)
THEOREM
TYPE IN WIFF
```



```
(P. \(-P) \cdot Q) /(((Q+-P)+(R,-Q))+-P)\)
EST ON C2 - WFF AS TWO VARIAELE LIST
WFF S/U
\(S=T \cdot Q\)
```



```
\(V=W+X\)
\(W=Q+-P\)
\(y=R .-Q\)
THEOREM
TEST ON C3 - TRUTH TAELE ON DENAND
PRSO10101010000000
RRSO100010001010000
SRSO000000000000000
TRTOO0000000000000
```



```
RO1010100010101
FOTO100000101010
30000010000000100
FRSD 10101010101010
NRS
```

[^1]An Additive Pseudo-random Number Generator
H.T. Wheeler", J.K. Lewis, E.A. Cherniak

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Department of Chemistry
Carleton University
Ottawa, Canada
```

INTRODUCTION - This generator was developed for use in a machine language programme (1) requiring random digits and short random fields. The method of generation exploits the variable field length feature of the 1620 by adding fields of several hundred digits in length. A small table of random digits is generated and stored in memory. From this table are selected randon digits and/or fields as required. When any table is used up a new table is generated using the old table as input data

The original programme has been modified and rewritten in SPS for use as a Fuitain suiroutine. Since the method of generation involves addition only, this generator is faster than the usual multiplicative generator

The tests for randomness which have been performed on the output of th generator have given quite satisfactory results.

METHOD - The generator requires an initial randon number of 501 digits
This initial number may be conveniently obtained from a table of randon numbers such as the Rand Corporation, " $1,000,000$ Random Digits with 100,000 Normal Deviates".

The initial number, which will be denoted $N_{1}$, is divided into two component fields, $A_{1}$ and $B_{1}$, of 311 and 190 digits respectively. Thus:

$$
N_{1}=\left(A_{1}\right)\left(10^{190}\right)+B_{1}
$$

A second number, $C_{1}$, is formed by reversing the order of the two com-
ponent fields. Thus:
*Speaker (to whom enquiries concerning this program should be sent)
-2-

$$
c_{1}=\left(B_{1}\right)\left(10^{311}\right)+A_{1}
$$

The second random number, $\mathrm{N}_{2}$, is formed by adding $\mathrm{C}_{1}$ to $\mathrm{N}_{1}^{\prime}$ and discarding the high order carry, if any:

$$
N_{2} \equiv\left(c_{1}+N_{1}\right)\left(\operatorname{modulo} 10^{501}\right)
$$

The number $\mathrm{N}_{\mathrm{i}}$ is generated from $\mathrm{N}_{\mathrm{i}-1}$ by the same procedure.
The choice of the values 501,311 , and 190 for the field lengths was largely arbitrary although it was intuitively felt that better performance would be obtained if each of the values had few prime factors and no common factors existed among the three values. 311 is a prime number; 501 and 190 factor into (167) (3) and (19) (5) (2) respectively.

RATE OF GENERATION - The 501 digit number is generated in 61.5 milliseconds (for a Model 1). The average time taken to obtain an 8 digit field, normalize, and store in FAC, when the generator is used as a Fortran floating point subroutine, is about 4.5 milliseconds. The time taken by the Fortran 2 variable precision subroutine is roughly given by $(3.5+f / 8)$ milliseconds, where $f$ is the mantissa length.

TESTS FOR RANDOMNESS - The major tests which have been performed on the generator were for the freauency distributions of single digits, of ordered pairs of digits, and of runs of repeated like digits. These tests were performed on the 501 digit numbers without any division into smaller fields. Some of the test results are shown in the following tables.

In Table 1 the results $\boldsymbol{f}$ a digit frequency test on one million digits are shown. Except for the somewhat large chi-square values for blocks 9 and 10 the results are very satisfactory.

## -3-

Table 2 shows a typical result of the ordered pair analysis. The expected value for each entry in the matrix is 501 . The frequency of the ordered pair xy is the yth term in the xth row.

In Table 3 the repeated like digit analysis results are shown.
The results of these tests are sufficiently good to indicate a usable degree of randomness. If a greater degree of randomness is required the output of two separate generators could be added, to produce an improved 501 digit table.

We are grateful to the Nationai Research Council of Canada for the financial assistance which made this work possible and the Computer Policy Committee of Carleton University for granting us the necessary machine time.

1. Lawis, Wheeler, Cherniak - A Model Diffusion-reaction programme for the L wis, Wheeler, Cherniak - A Model Diffusion-reaction programme for the
$1620-1620$ Users Group Joint Meeting (Canadian and Mid-Western Regions) Chicago, February, 1964.

TABLE I
digit frequency test
ONE MILLION DIGITS

| Block |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | CHI |
| 1 | 4956 | 5014 | 5025 | 5077 | 4960 | 5050 | 4909 | 5009 | 4996 | 5004 | 4.24 |
| 2 | 5038 | 4927 | 5054 | 4934 | 4943 | 5056 | 5008 | 4965 | 4967 | 5108 | 6.85 |
| 3 | 5039 | 4954 | 4994 | 4978 | 5006 | 5061 | 4923 | 4926 | 5035 | 5084 | 5.52 |
| 4 | 4979 | 5002 | 5073 | 5041 | 5056 | 4947 | 4980 | 4967 | 5027 | 4928 | 4.16 |
| 5 | 5005 | 4907 | 4906 | 5117 | 5025 | 5094 | 4909 | 5079 | 4976 | 4982 | 11.21 |
| 6 | 4973 | 5108 | 4983 | 4996 | 4914 | 5010 | 5079. | 4877 | 5079 | 4981 | 9.63 |
| 7 | 4938 | 5028 | 4995 | 4902 | 5096 | 5063 | 5087 | 4999 | 4974 | 4918 | 8.48 |
| 8 | 5011 | 5047 | 4938 | 5064 | 5006 | 4871 | 5036 | 4957 | 5064 | 5006 | 6.85 |
| 9 | 4995 | 4806 | 4966 | 5040 | 5011 | 4884 | 4960 | 5026 | 5163 | 5149 | 20.78 |
| 10 | 5125 | 5063 | 5000 | 5062 | 4832 | 5117 | 5060 | 4924 | 4992 | 4825 | 21.08 |
| 11 | 4974 | 5032 | 4908 | 5062 | 5021 | 5019 | 4961 | 4908 | 5109 | 5006 | 7.34 |
| 12 | 4964 | 4934 | 5111 | 4930 | 5096 | 5018 | 4862 | 5004 | 5121 | 4960 | 13.54 |
| 13 | 4965 | 5004 | 5027 | 5021 | 5076 | 5044 | 5021 | 4995 | 4931 | 4916 | 4.48 |
| 14 | 5056 | 5077 | 4898 | 5081 | 5053 | 4972 | 4897 | 5000 | 4856 | 5110 | 14.61 |
| 15 | 4960 | 5094 | 5037 | 4876 | 4990 | 4995 | 5108 | 4963 | 5006 | 4970 | 8.24 |
| 16 | 4981 | 4930 | 5046 | 4982 | 5077 | 4970 | 5035 | 5083 | 4970 | 4926 | 5.80 |
| 17 | 4977 | 5071 | 5096 | 4955 | 4982 | 4863 | 4972 | 4962 | 507.7 | 5045 | 9.22 |
| 18 | 5116 | 4996 | 4990 | 5009 | 4981 | 4972 | 4848 | 4987 | 4943 | 5157 | 13.19 |
| 19 | 5008 | 4880 | 5042 | 4943 | 5008 | 5093 | 5024 | 4968 | 5014 | 5020 | 6.08 |
| 20 | 4015 | 4998 | 4989 | 4950 | 5106 | 4968 | 5012 | 4963 | 4970 | 5029 | 3.67 |
|  | 100075 |  | 100078 |  | 100239 |  | 99691 |  | 200270 |  |  |
| Total |  | 99872 |  | 1.00020 |  | 100067 |  | 99562 |  | 100125 |  |
|  | $\mathrm{CHI}^{2}$ | (total | s) $=4$. | 660 |  | Probabi | lity (> | $\mathrm{CHI}^{2}$ ) | 0.86 |  |  |

Of the 200 frequencies 64 deviate by more than sigma ( $=67.08$ )
(expected number $=63.4$ ) and 9 frequencies deviate by more than two sigma
number $=8.2$ )
Tests on column totals $\mathrm{CHI}^{2}$ Probability Odd versus even digits 0.498 Within odd digits
0.49
0.68

Within even digits
2.287 0.69

## TABLE II

ORDERED PAIR ANALYSIS ON 100 NUMBERS

$$
\text { OF } 501 \text { DIGITS. }
$$

|  | 0 | 1 | 2 | 3 | 4 | 5 | 0 | 7 | 8 | 9 | $\mathrm{CHI}^{2}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 0 | 472 | 504 | 544 | 477 | 509 | 490 | 496 | 496 | 493 | 454 | 11.54 |
| 人 | 1 | 519 | 494 | 511 | 516 | 487 | 527 | 503 | 516 | 503 | 506 | 3.64 |
|  | 2 | 502 | 490 | 497 | 514 | 474 | 502 | 530 | 505 | 519 | 511 | 4.62 |
|  | 3 | 514 | 520 | 499 | 494 | 451 | 517 | 479 | 505 | 507 | 518 | 8.31 |
|  | 4 | 479 | 480 | 489 | 493 | 472 | 496 | 508 | 456 | 462 | 530 | 12.84 |
|  | 5 | 511 | 502 | 520 | 529 | 482 | 492 | 505 | 514 | 472 | 475 | 6.76 |
|  | 6 | 495 | 542 | 498 | 476 | 521 | 495 | 517 | 530 | 527 | 513 | 9.38 |
|  | 7 | 468 | 507 | 507 | 506 | 489 | 513 | 486 | 483 | 498 | 509 | 4.18 |
|  | 8 | 476 | 562 | 492 | 496 | 508 | 469 | 544 | 475 | 479 | 487 | 17.42 |
|  | 9 | 500 | 483 | 493 | 509 | 469 | 498 | 540 | 479 | 530 | 499 | 8.65 |

Probability (CHI $\left.{ }^{2}>16.92\right)=0.05$
table III
REPEATED LIKE DIGIT
run analysis results - tests on
50,100 DIGITS
LENGIH OF RUN

|  | TEST NO. | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\pm$ | 1 | 40723 | 3987 | 421 | 40 | 2 | 0 |
| $\checkmark$ | 2 | 40592 | 4079 | 404 | 49 | 1 | 0 |
|  | 3 | 40639 | 4036 | 406 | 34 | 7 | 0 |
|  | 4 | 40488 | 4122 | 391 | 45 | 3 | 0 |
|  | 5 | 40570 | 4068 | 397 | 42 | 7 | 0 |
|  | AVERRGE | 40590 | 4058 | 402 | 42 | 4.0 | - 0.0 |
|  | EXPECTED | 40581 | 4058 | $406$ | 41 | 4.1 | 0.4 |

## A MODEL DIFFUSION-RLEACTION PROGRAME FOR THE 1620.

J.K. Lewis, H.T. Wheeler, E.A. Cherniak*

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Diffusion, particularly neutron-diffusion, has been studied by Monte Carlo on digital computers since the introduction of the ENIAC. However, as far as we know, no extensive applications of this method, to diffusionreaction problems of a chemical nature, have yet been given. This paper describes one approach to such a problem.

In the radiolysis of liquid benzene, it is well known that a high energy particle leaves behind it a cylindrical track of excited molecules and ions. The track is of varying density, depending on the energy of the incident particle. It was belfeved that certain phenomens, notably the variation of hydrogen yields with stopping power, could be explained, in a way, suggested by Burns(l), by assuming that these activated molecular entities were of one form, $\mathrm{B}^{*}$, which could react in the following way:

$$
\xrightarrow[{\mathrm{B}^{*}+\mathrm{B}^{*} \xrightarrow[\mathrm{BR}]{\mathrm{B}} \mathrm{BR}_{\mathrm{UR}} \mathrm{~B}_{2}}]{\mathrm{B}}+\mathrm{P}(3)
$$

The main feature then to be explained was the variation of $H_{2}$ yields with stopping power. This is shown in figure 1 where the experimental average values of the $H_{2}$ Fields, compiled by Burns and Barker(2), from the results of the investigations of a number of workers, are given as a logarithmic function of the Ganguly and Magee(3) average stopping power 2.

[^2]In the programme which we eventually used, a particle was represented by i*s coordinates, each coordinate having four digits and the total comprising a field of twelve digits with a single flag on the high-order digit. Reacted particles were denoted by a flag on the low-order digit. The quenching reaction (UR) was treated as an unimolecular process and for the bimolecular process (BR) the coordinates of each particle had to be compared.

The "tracks" (see flow chart l) were set up in the most elementary fashion. A few cards were read in, each with the coordinates of a particle and the number of particles with those coordinates to be set. When all the cards were read, the track could be stored elsewhere in memory. The numbers controlling the rates of reaction and the width of the initial distribution were then read in.

The initial particle distribution was then generated by allowing the particles to be moved the specified number of times without reacting. The distribution generated in this manner by, say, six pre-reaction moves is quite close to Gaussian.

The particles were then moved and reacted, alternately; (see flow chart 2) until all the particles were gone, after which the numbers of particles reacted was typed and the programme repeated.

Each particle was moved by adding to it a 10 digit field with a random digit in the first, fifth and the ninth positions from the right. Thus the centre of gravity of the particles "drifted" steadily through model space. It was found that random digits with a rectangular distribution, i.e. equal probabilities for all the digits, caused the particles to diffuse off at an inconveniently high rate. We were thus raced with the problem of generating large numbers of digits rapidly with a skewed distribution. The obvious method, playing a game of chance, proved cumbersome. However, a simple modification of the random number generator, described by Wheeler(4), proved successful.

To produce a distribution of digits the programme replaced the add tables with special add tables having digits in the desired frequency. Thus these digits could be produced in an average time < $250 \mu \mathrm{sec} . / \mathrm{digit}$. Furthermore, the frequencies of the digits could be controlled to l part in 100 , although as our particles had a moving centre of gravity, the frequency distribution had to be symmetrical about the mean move length, restricting our control to 1 part in 50 . This was far more than sufficient.

The "react" routine (flow chart 2) contained a scanner which scanned the appropriate section of memory until it found either a record mark, indicating the end of the particles, or an unreacted particle. Then, depending upon the state of a simple flip-flop operating on bd's and tdm's, the particle would be "reacted" first unimolecularly....and then bimolecularly, or vice versa. This altergration on unimolecular and bimolecular from one particle to the next was found necessary at high concentrations of particles.

To ascertain whether a particle was to have reacted unimolecularly or not, a four digit field was taken from the random number generator and compared with a control number. If the random number chosen was less than the control number, the particle was assumed to have reacted, a flag was placed on its units position, a counter was incremented, and control returned to the scanner to find another particle. The four digit length was actually found to be necessary to give adequate control over the unimolecular rate. If the random number was greater than the control number, the program would proceed to the next particle or would consider the particle for bimolecular reaction, depending on the status of the flip-flop.

For the bimolecular reaction, the particles above the particle under consideration were examined for whether or not they were reacted. When an unreacted one was found, its coordinates were compared, by a single c instruction, with the particle under consideration. Analysis showed that it would probably be faster to compare all twelve digits of each sets of coordirates
at once than divide them into 3, of which only the first four would be compared for two non-coincident particles. When two particles were found to coincide, the usual chance game was played to aetermine if reaction had taken place. Unlike the unimolecular reaction, however, only a three digit control number was used and two digits would have sufficed.

The programme described above, which was written in about 1000 machine language commands on a 40 K 1620 with automatic divide, will "react $\sim 150$ particles to completion in 5-15 minutes, depending on conditions, but typically 7 minutes, with a standard deviation of $-15 \%$ in the results. A comparison of our results with the experimental data is shown in figure 1. By varying the control numbers it was found that the experimental data could be fitted quite closely and that the values this fitting procedure gave for the rate constants were in fact plausible.

We are now engaged in refining our interpretation to get improved values for rate constants. Actually, this problem of interpretation is the main disadvantage of our approach vis à vis a numerical integration method. Our programme is probably as fast or faster than a numerical programe for the same mechanism, and the $\cdots$ deviation is not excessive for experimental values accurate to better than $10 \%$ are rare in this field. However, the process of getting from our model to the physical situation is rather involved. First we work out a one dimensional distribution of particles which have moved several times with the move distribution we use. We then fit a Gaussian curve to this and from this obtain a model diffusion coefficient. A good value for the real self-diffusion coefficient is available, so this gives us a value for "model length $)^{2} /$ model time" in real units. If a good model length is found, then the model time drops out. From the diffusion coefficient and the control numbers the two rate constants are readily obtained. However,
the "model length" poses the problem. After some thought we decided it should be twice the "collision diameter" of the molecule, but, in liquids this is a rather ill-defined quantity, and reasonable values based on various definitions tend to differ somewhat.

The main virtue of our program was its flexibility. It can handle ragions of intermediate stopping power, where the track resembles billiard balls strung together on a cord, which are particularly difficuit for standard numerical integration procedures. It can also handle varying amounts of particles corresponding to different input power, and with modifications could treat other problems, such as effects of small amounts of reactive solutes. These last two features were never used, partly because of a paucity of experimental data, because the effects are notable chiefly through their absence, but principally because crude hand calculations upon the "plausible" rate constant values were sufficient to show that these effects should in fact be small

We are grateful to the National Research Council of Canada for the financial assistance which made this work possible and the Computer Policy Cormittee of Carleton University for granting us the necessary machine time.

1. Burns, Trans. Faraday Soc. 29 (1963).
2. Burns and Barker, United Kingdom A.E.R.E. Report 4240 (1963)
3. Ganguly and Magee, J. Chem. Phys. $25 \quad 129$ (1956).
4. Wheeler, Lewis, Cherniak - A new random number generator ${ }^{1520}$ Users Group Joint Meeting Cnicago, February, 1964.


FIG 1 Vapiation of experimental $G\left(H_{2}\right)(0)$ with average L.E.T. in the radiolysis of liquid $\mathrm{C}_{6} \mathrm{H}_{6}$, obtained by diffusion reoction programme, -----predicted by diffusion reaction programme


FLOW CHART 1: Diffusion-reaction programme track and initial particie distribution generator.


# AUTOSPOTLESS NUMERICAL CONTROL WITH THE 1620 

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## AUTOSPOTLESS NUMERICAL CONTROL

WITH THE 1620

A great deal of emphasis is being given to the 1620 and its role in the numerical control of machine tools. This is certainly as It should be. However, the resulting emphasis on the APT (Automatically Programmed Tools) language and the Autospot subset of this language is unjustified.

The use of Autospot assumes:

1. The only output desired is a paper tape and a listing of its contents.
2. Sufficient 1620 time to use a four deck processor (including post processor) for each workplece.
3. The existence of a post precessing program.
4. The existence of trained "parts programmers".

Due to the specialized nature of our numerically controlled machines, operator's instructions must accompany the tape as it enters the shop. Furthermore, Industrial Engineering must prepare standard hours for entry on the shop routing or traveler. Thus, It has been decided that all these documents should be computer created. Autospot does not lend itself to this effort.

Over 175 workpieces are processed monthly on our Ingersoll header drill. This represents drilling and chamfering some 70,000 holes each month. For the Autospot processor, this represents over 70 hours of computer time. This would mean second shift operation for almost any 1620 facility.

The creation of a post processor involves understanding of Autospot, the tool to be controlled, the 1620 and the controlling mechanism itself. This, coupled with the fact that Autospot is really more comprehensive than is necessary for our applications, makes the creation of a fixed format input processor most advisable. With such fixed format input programs, no "parts programmers" are required. Industrial Engineering members can readily interpret engineering drawings and compactly represent this information on input sheets.

The total time from the interpretation of the drawing to the creation of pertinent documents is greatly reduced by use of this concept. To 111 ustrate, the Ingersoll header drill with its accompanying functions and required documents can be cited. The $\mathrm{N} / \mathrm{C}$ Ingersoll header drill is used for drilling and counterboring cylinders on the order of 60 feet long, 1 ft . outside diameter and two inch ( 2 ") thick walls. The holes in this cylinder normally align themselves into six (6) or less rows down the header. The hole spacings are highly irregular and are a function
(
of the boiler system of which the header is a part. The work which preceeds the actual drilling of a header is best described by fig. 1. The three (3) documents entering the shop serve the following functions:

1. Routing slip
a. Provides operational sequence
b. Shows standard hours allocated for each operation
c. The approximate date on which each operation should occur is also shown
2. Tape contains
a. Positions for drilling
b. Drilling feeds and speeds
c. Counterboring feeds and speeds
d. Spindle starts and stops
e. Gear changes
3. Operators instructions
a. Shows angularity of each row from a given point
b. Tells the operator when to use what tools
c. Provides settings for limit switches
-4-

Proper representation of input data permits the creation of all these documents. Autospot does not lend itself to such a representation. For example, Autospot must be told which tool to use. Our feeling is that the program should select the tool. The computer selection of a tool eliminates a great deal of human thought and potential error since tool choice is a function of material type, nipple o.d., nipple wall thickness, thickness of header, etc. This selection then fixes the counterboring diameter, counterboring depth, drilling feed and speed, counterboring feed and speed, gear range, etc.

The input sheet used by our program is shown in fig. 2. The manner in which the completion of this sheet fits into the overall picture of fig. 1 is shown by fig. 3 . Several points are worth noting about this system:

1. No parts programmers are required. Technicians complete the input sheets.
2. No post processor is required
3. Two SPS programs can create all the described documents.
4. A typical header can be processed through the 1620 in less than . 1 hour to produce all documents.
t. Autospot would require no less than .4 hours to create tape information alone

When the total systems approach is applied to N/C problems, the fixed format input exemplified by this system and other systems like the IBM 1401 Autoprops seems to have definite advantages over APT processors.

Figure '*



$4$

C


## Technical Publication

## AUTOSPOT II PREPROCESSOR PROGRAM

By D.F. McManigal PRG 26.0006

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## ABSTRACT

The Autospot II Preprocessor is an IBM computer program used to help the parts programmer prepare correct input data for Autospot 11 .

January 2, 1964

## . 0 INTRODUCTION

Autospot II (AUTOmatic System for POsitioning Iools, Model il) is a omputer program for the IBM 1620 Data Processing System (see Figure 1 ). t was designed to aid the parts programmer in preparing instructions for numerically controlled point-to-point machine tools. Autospot permits the use of easily remembered codes, such as DRILL, TAP, and MILL, instead of the more complicated numeric codes used by numerical control machine tools. Autospot performs many computations for the parts programmer, and retieves him of much redundant coding.
autospot a


Fizurs 1. Autospot 11 Progiam Flow

Autospot II consists of a General Processor which is common to all machine tools and a Post Processor for each machine tool. The Genera Processor performs such operations as translation to numeric codes and machining pattern manipulation. The Post Processor tailors the output o the General Processor to suit the individual machine tool requirements. The input to the General Processor is a source stotement card deck and the output from the Post Processor is a punched tape containing machine tool commands in the proper code.

### 2.0 THE NEED FOR A PREPROCESSOR

To reduce the number of passes required in the General Processor error detection and diagnosis were limited to a minimum. Most source statement errors result in general error messages; however, many errors cause a computer check stop or hang-up condition, without an erro message.

The lack of extensive diagnostic information is not a serious problem when the parts programmer has adequate experience with Autospot. Much time is lost, however, in identifying errors and the assistance of a 1620 programmer is frequently required. An inexperienced parts programmer often encounters so much difficulty with source program errors that much of the advantage of Autospot is lost. For example: If a parts programmer nadvertently substitutes a decimal point for a comma at the end of a coordinate dimension, the 1620 will hang-up in an-infinite loop when the General Processor reads the statement. The parts programmer may then need the assistance of a 1620 programmer to locate the error.

### 3.0 PREPROCESSOR DESCRIPTION

The Autospot Preprocessor (see Figure 2) is a one pass program for the 620 system. Its purpose is to detect and diagnose most of the errors which occur in Autospot Il source statements. Error detection is sufficiently etailed to permit immediate recognition of most common errors, and to significantly reduce the time required to diagnose unusual errors. On-line editing permits immediate correction of most errors during preprocessing.

The Preprocessor is capable of detecting two types of error: format errors, such as typographical mistakes; and, violations of Autospot rules, such as illegal pattern manipulation. Most of the 35 possible error messages efer to rule violations because these errors are usually more difficult to diagnose than are errors of form.


## AUTOSPOT

 PREPROCESSORFigure 2. Autospot Preprocessor

## EXAMPLE 1

The use of too many machining patterns will result in the error messoge
e COUNT PAT PAT 1.
where PAT 1 is the symbolic label assigned to the pattern by the parts programmer. This error messoge is specific because the noture of the error is not readily evident.

## EXAMPLE II

The use of the letters DQ instead of DP for specifying a depth will result in the error messoge:

## C FORM AUX DQ.

This indicates a format error in the auxiliary section of the statement.
This indicates a format error in
The specific nature of the error is readily evident.
When on error is encountered, the preprocessor will type:
one of the 35 different error messoges,
the entire erroneous line
the contents of the data field in question, and the punctuation terminating that fielc.
The dota field $\alpha$ stotement section is not necessarily in error, but this indicates that the error was recognized at that point. The actual error may appear anywhere up to that point.
3.1 PREPROCESSOR ERROR MESSAGES

The error messages are in abbreviated form and contain error type cades which indicate the corrective action to be taken. A blank code indicates that the typeout is for information only and requires no action. A "P" code indicates that the field in question is acceptable but unusual and is a possible error. An "E" code indicates that there is a definite error which connot be corrected on-line, but which will result in on erroneous edited deck. A "C" code indicotes that the error is definite but can be corrected on-line.

The computer takes no action on a blonk or "P" coded error. The erroneous statement is deleted on on " $E$ " type error but no halt occurs. Program switch settings determine the action on a "C" type error. If the editing feature is disabled, the error is treated as on " $E$ " type error. If editing is required, a program halt accurs to permit correction or amission of the erroneous statement (at the discretion of the operator).

The non-stop mode of operation permits operators who are not fomiliar with Autospot to run the Preprocessor. The Preprocessor will also calculate effective drill lengths, a feature which reduces the number of calculations the parts progrommer is required to make.

### 3.2 PREPROCESSOR ADVANTAGES

The effectiveness of the Preprocessor is illustrated by a test problem which was run at IBM Poughkeepsie. The part being programmed was an act:al production piece, requiring opproximately 3,000 lines of numerical controls for the Kearney and Trecker Milwaukeé-Matic machine tool. The Autospot source deck required 126 lines, including 107 lines of machining statements. Using the Preprocessor, this large program was debugged in less than 30 minutes, of which only 14 minutes was 1620 computer time. This time included the initial run and two reruns after corrections (corrections being made off-line due to type " $E$ " errors). The same source program was partially debugged, by the parts programmer who wrote it, in four hours. The experiment was then terminated and the job completed using the Preprocessor

Littie time is lost in running good source statements through the Preprocessor. Error free source cards are processed at the overage rate of one line per second, assuming nearly full lines. If no errors are found, most source decks may be checked in less than one minute (including Program lood time).

### 4.0 SUMMARY

The Autospot II General Processor provides limited error diagnosis
Because of this, many advantages are obtained by using the Autospot
Preprocessor. The Preprocessor pinpoints most common errors and provides sufficient diagnostic information to significantly reduce the diagnosis time for unusual errors.
5.0 PREPROCESSOR DEBUGGING (SAMPLE)

Figure 3 shows the General Processor listing of a sample problem. Note error messages.

Figure 4 shows the output of the Autospot Preprocessor for the same program. Note error messages.

Figure 5 shows the rerun of the edited program deck.

1 rdark/ general processor error messages s
2 DASHA(3.5,2.75)S
3 DASHI=DASHA $(0.0,5.25,-1.0) S \quad x, y, 2$ entries should agree with dasha
4 DASHC $(9.0,7.5)$ ) should have table position
$5 \mathrm{CL}(0.3) \mathrm{S}$
6 DH(1.0,1.0,1.0)s
$7 \mathrm{DH}(0.5,0.3,0.3) \mathrm{S}$
8 DH(1.0,0.5,0.5)s
9 dh(0.5,0.5)\$ Limit is three deep hole sequences
10 TOOL/ORILL $13010.25 \quad 7.5 \quad 2000 \quad 10.0$ 07\$NO EFF LENGTH
$\begin{array}{llllllll}11 & \text { rOOL/SPDRL } & 1302 & 0.5 & 120.0 & 7.0 & 2000 & 8.0 \\ 0.0\end{array}$
12 TOOL/DRILL 1303 0.4 $119.0 \quad 6.5 \quad$ 8.0 O7SNO SPINDLE SPEED
13 STARTS
14 PATI=/DM, SX(0.0)SY(0.0)EX(9.0)NH(5)S INCREMENTAL SEQUENCE
15 PAT2-SPORL, 1302/PAT1/OI (0.2)THEN, PAT1(0.0,1.0)THEN, PAT1(2.75,2.0)AT(00.0) \$
16 DRILL, 1301/PAT2/DO(2.0)OH(1)OWS
ERROR MINOR SECTION 16 DRILL,1301/PAT2/DQ(2.0)DH(1)OWS
DO SHOULD BE DP
17 PAT3-/PAT1 (5.0,0.0)THEN, PATI( $6,0,0.0$ ) THEN, PATI $7.0,0.0$ ) \$
13 DRILL, 1303/REV, PAT3/DP(2.0)OH(4)THEN, DAE, PAT3, THEN, DAC, PAT3S DH 4 WRONG
9 remark/ reversal of second generation s
o remark/ pattern is mot permissible \$
REMARK/ ERROR DETECTED IN PHASE 2
remark/ the following statement causes
remark/ a hang - up in the gr. §
24 DRILL, 1303/DAC $(-1.0,0.0)(-10.0 .0 .3,-0.5) / D P(0.7) \mathrm{DH}(3) \$$
WOTE - MDICATED ERRORS WHICH CAUSED NO ERROR
MESSAGE ARE DEEECTED IN PHASE 2 OR IN
THE MOST PROCESSOR, OR NOT AT ALL.

Figure 3. General Processor Listing of Sample Processing

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AUTOSPOT PREPROCESSOR DATED $12 / 18 / 63$
REMARK/ RE-RUN of EDITED SOURCE DECK
2 DASHA $3.5,2.75$ ) S

| $P$ |
| :---: |
|  |
| $\mathrm{NO}_{3}$ |

Figure 4. Autospot Preprocessor Output

DASHB =OASHA (0.0,5.25)s
DASHB $=$ DASHA $(0.0,5$
TP
TASHC
No ${ }^{\text {DASHC }}(9.0,7.5) \$$
$\mathrm{CL}(0.3) \mathrm{s}$
CL $(0.3) \$$
DH $1.0,1.0,1.0)$
DH $0.5,3,0,3)$
DH(1.0.0.5,
(1.5)

$\begin{array}{ll}12 & \text { TOOL/DR1L } \\ \text { TOOL } 1303 \text { NO } \\ 13 & \text { STARTS }\end{array}$





O REMARK/ PATTERN IS NOT PERMISSIBLE
REMARK/ ERROR DETECTED IN PHASE 2
REAARK/ THE FOLLOWING STATEMENT CAUSE
22
23 REARK/ THE FOLLOWING STATEMENT CAUSES
R GARK/ A HANG - UP IN THE GP.

25
ENO PREPROCESSOR

Figure 5. Edited Program Deck (Rerun)

## on-lime correction

should have taele positioh

MANAGEMENT INFORMATION

## BY

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## MANAGEMENT INFORMATION

There are different reasons why one may address himself to and accept the challenge of discussing, presenting, or reviewing a given topic. He may be an authority on the subject and discuss it in that capacity, or he may hold a position of responsibility in which the method may be applied and so discuss it from that point of view. When $I$ was invited to present this paper, I was aware that my qualifications are not those of an authority but rather those of a practitioner in the field of Management Information. An interest in the subject and a recognition that there is applicability in present day business management provides motivation for preparing and presenting these remarks.

One way of organizing material for a presentation such as this would have been to search the literature and quote the authorities. I did not do this but rather elected to speak on the subject as I see it in general and somewhat specifically in my company. If a bibliography of writings on this topic were to be assembled, I am sure it would be impressive. I am also sure that the list of articles on the subject will grow at an increasing rate in the years before us and that our present state of knowledge and level of practice will be dwarfed by future developments

My comments will be organized around the following paints:

1. A review of what constitutes information.
2. A definition of terms that are associated with the subject.
3. A brief discussion of the functions that constitute the totality of company activity.
4. The state of the business world with special concern about the need for scientifically developed Management Information.
5. Relationships among Management Information, the computer, and personnel.

## Information

In discussing this topic one must soon come to grips with what is meant by the word "information", and what the connotation must be when used in discussing business problems. A dictionary or academic definition may add a note of scientific precision to this presentation but, in keeping with the intent of the paper, it seems more appropriate to define the word by using it in context for a few paragraphs. It is the intent here to define its meaning as used in the language of business decision making.

Let us first agree that usage of the word suggests the addition of something new to the hearer's store of knowledge. Let us also agree that this information may be used as the basis for making decisions, either in the business world or in private lives; that it will be used as the basis for setting in motion courses of action. We must agree, if the preceding has been accepted, that information must have some value; that is, it must be appropriate, accurate, and it certainly must be timely

We can quite likely agree that information, in part, may consist of reports, lists, graphs, comparisons, counts, or any other statements that something is or is not. In a moment we will be considering that information might be classified as available before an act takes place or after an act takes place, thereby giving it a form of time dimension

A common example of information that is available after an act has taken place is found in performance measurements. These would include data on production to date, sales to date, costs incurred, capacity utilized, asset position, and liability position. Position records such as earning statements and the balance sheet could be looked to as other examples of information made available after an act has taken place. In all of these
follows that the more strategically located and the larger that mirror the better the view will be of where the driver has been.

Information before the act is then likened to the windshield of the automobile. If this is large and clear, the driver is able to see where he is going and can take steps necessary to get him there fast and safely. The relative size of the windshield in comparison to the rear view mirror is important in an automobile and it certainly is important in the operation of a business enterprise.

It must be recognized at this point that these remarks are concerned with degree rather than absolute lack of conformity to the concept being discussed. Historical information has and always will be used for preparing predictions, and anelysts have always contributed toward producing that element within the totality of information upon which decisions can be based. It is argued, however, that considerably more effort should be directed toward using the analytical techniques known to management science personnel, and that this be used to generate decision-making information before it is given to management. The decision maker; that is, the manager, should be in a position to ask the question, "What will happen if I take this or if I take that course of action?" The management scientist, using the analytical tools available to him and working with historical data, is able to add that element which will make it a more reliable basis for planning courses of action within the business enterprise.

## Definition of Terms

It will be convenient, for expository purposes, to define some terms and expressions that are used in discussing the activities in the business world. The definitions =re not intended to be precise in the academic sense but rather as clicifications for the purpose of presenting views in this paper.
A. Business Problems

The activities of a business enterprise constitute a process in which the resources under the control of the business firm are used, in a production phase, to create added value and then to bring into a realization that added value through a distribution and marketing phase. Business problems exist because the total process does not operate without disturbances. Resources, including materials, supplies, facilities, and the skills of employees are limited and imperfect. There is resistance in the market to paying more than necessary for the products of the business enterprise and there is a constant need for attention to the mechanism of the production phase. The existence of these disturbances, as well as the need to plan for the growth of the enterprise, constitute business problems.
B. Sourses of Action

These relate to the steps that are and must be taken by management to correct a business problem. The course of action is therefore simply the doing of something, the execution of the plan that resulted from a management dicision.
C. Dynamic

A moment's reflection on the business problem and its resolution in a business enterprise suggests that many problems occur repeatedly. In fact, it will soon be observed that the majority of the operating problems are recurring. The frequency with which they occur and especially the speed with which they can be resolved play an important role in the competitive position of a business enterprise. These observations partially provide the basis for describing a business, especially as measured by its problems, as dynamic.
D. Information Retrieval

This term relates to a fairly well-defined process of cataloging the content of articles, abstracts, hooks, and the like and for providing a means for locating the document, or a brief statement of its content, in response to the user's need. Management Information, the title of this paper, is not related to Information Retrieval except as the latter may be a part in the process of generating decision-making information for management. An issue is made of this comparison since there is a possibility for confusion, the belief that the ability to rapidly extract data from files will serve the need of management for information.

## Functions of a Company

The totality of activity associated with the operation of a company can be categorized in various ways. To focus attention on a specific function, the generation of information, four categories are formed, which, by definition should include all the activities that can and do take place in a business enterprise. These categories include: 1. Production-Marketing-Distribution. 2. Recording and Control. 3. Decision Making. 4. Information Generation.

Production, marketing and distribution, the operations function in a company, include the obvious activities of utilizing facilities and resources to produce something, to market it, and to move it through the distribution channels into the consumer's hands. In a processing industry such as the canning industry, this will appear as, and in fact is, the dominant function of the enterprise.

The activities of maintaining company operations records, company operating plans, and providing a measure of performance against plans constitute, in part, the function of recording and control. There is
obviously considerably more that could be said about this and about the operations function, but since it is the objective in this paper to discuss Information Generation, further elaboration on these other functions will be omitted.

Decision making is a function that is executed at all levels of company operations. As a first impression it appears that this might be a function reserved for the top executives. This is not true, however, since the worker on the line must, and does, make decisions, or at least apply a measure of judgment, in operating a piece of equipment or using a resource. Top executives make decisions about such matters as finance, plant or production expansion, personnel assignments and the like. The vast majority of the decisions in any business enterprise, however, are made by the operating and management personnel between the line worker and the top executive. In any case, the decisions at all levels must be appropriate and they must be timely. The skill with which this function is executed will be reflected in the effectiveness of the operations function and also in the effectiveness of recording and control.

If it is agreed that setting in motion the appropriate courses of action at the different levels in a company is dependent on the quality and timeliness of decisions, the foregoing statement is obviously supported.

The function to be discussed in greater detail in this paper is that of Information Generation. The importance of this is underscored by recognizing that the function of Decision Making is not exccuted in a vacuum, it is not independent of the other functions. A course of action within the operations function is not put into motion unless there has been a decision to do this and unless there has been a decision to commit certain of the company's resources.

The basis upon which a decision is made, however, is that of the information available to the decision maker. Information about the process
and information developed in the planning sense must be of rered to the manager, the person who will translate it into a decision. It is at this point that the function of Information Generation achieves its significance.

## State of the Business World

Business decisions are not made in a vacuum and business enterprises are not operated independently of the business world environment. One of the characteristics of the business world, it is contended, is that changes are taking place rapidly and that the function of decision making, as a result, is becoming increasingly complex.

If we accept as true that there is, in fact, a rapidly changing climate in the business world, then we must also accept that the advanced techniques for coping with these changes must be developed and applied. It is especially required that support for decision making be made available accurately, adequately, and timely. This constitutes the heart of the total Management Information idea.

Technology in problem solving has changed and has improved very rapidly during recent years. The mathematical methods of linear programming, critical path analysis, inventory control, estimating, forecasting, and many others have been developed, improved, and made available to management. Books, articles, courses, and seminars have been employed during the years since World War II to disseminate the information.

It is of special interest to observe that the mathematical techniques, if considered by themselves, are of limited value. These techniques must be a part of the total rroblem solving system if they are to be of service to a business enterprise. The process of information generation is built around this concept. It is one of the objectives in this paper to demonstrate that information, in addition to being a record or recitation of events that have taken place, also includes those elements of information that will point up the most ideal steps that can be taken in the decision-making process.

Another characteristic of the business world today, in comparison to past years, is the intensification of competition and its attendant problems. New products are coming on the market at a faster pace and the costs of developing them are higher than was true several years ago. The advantage to the company developing a new product, it is contended, is either short lived or the margin of profit is narrow. This is the result of competition not only among manufacturers of the same product, but among all manufacturers competing for the consumer's dollar. This underscores the necessity for having pertinent information available to management, information that can be used as a basis for rapidly formulating decisions and effecting courses of action. The significance of these observations is in the necessity for much faster action than in previous years, and for fewer mistakes in committing companies' resources to an operations course of action.

A single development that has been instrumental in stepping up the pace of business activity, and has also been providing a means for servicing the stepped-up pace, is that of the computer and the technology for programming and operating it. This combination of equipment and technology has made possible the rapid processing of voluminous data, as well as analyzing data complexes such as are common to the management science field. The reduction of voluminous records and the evaluation of complex sets of data provides a source of information that has not been available in the past.

In addition to the data processing equipment, there has been development in communications which makes possible real time or near real time data analysis for decision making. All of this clearly dictates the need to develop a system through which the tools of information generation can be employed most effectively. It must be possible to develop clear and concise elements of information that can be used in the decision-making
process with a minimum of further analysis or data reduction by the user; that is, by the decision maker,

A logical consequence of the foregoing is that management by exception will be and must be practiced. It is not possible and certainly not necessary for a manager to weigh all the facts that can be developed by an information generation system. Rather, he must be given those elements of information to which he can add his skills and thereby reach the decisions that are most beneficial to the company

It is also necessary that the Information-Generating process produce facts that can be translated directly into routine courses of action. A certain percentage, perhaps quite high, of this type of tasks in a company can be reduced to decision rules that can be operatea upon by an electronic computer or, at most, require clerical attention. The net result is that this will leave additional time to the manager to deal with the more complicated decision problems, problems that cannot, or at least not very readily, be reduced to a decision rule.

The intent of these comments has been to demonstrate that the role of the manager, decision maker, is changing rapidly as a result of the technological advances. The business climate within which the decision maker works is being changed by him and in turn requires that he change with it. He is, in a sense, a victim of his profession.

## Relationships Among Management Information, The Computer, and Personnel

The remarks to this point have been intended primarily to set the stage for a detailed review of the Information Generating function, its place in the company, and the impact it may have upon the Decision-Making process. Its impact upon the personnel involved and a review of the current state of the art will be considered briefly. As a point of departure, it will be well to take a look at what is meant by "Information Generation."

It certainly is a function and it has a place among those that define the totality of company activity. Information generation is not new. Rather it has been practiced as long as businesses have been operated. The method for doing it, especially its organization within the company, have changed over the years and the importance it has played and plays now is certainly changing. It shall be the objective in the following sections of this paper to present views as to what constitutes Information Generation, how it has changed over time, and what might be expected in the future.

We may think of this function as an operating process with inputs, service, and output stages. This analogy with the operations functions of a company will provide a convenient medium for presenting some of the basic ideas.

The inputs to the process initiate at various sources. Company accounting records provide data on costs such as those for personnel, power, raw materials, supplies, and others. Operating standards, capacities, and facilities availability data can generally be obtained from company engineering records. Prices of merchandise offered for sale become available from the company's marketing department.

Institutional data constitute another input to the process. These would include such items as taxes, insurance, interest rates, freight rates, economic indicators, and the like. Agency data, such as facts about industry stock position, and industry prices provide a third source of input. A fourth source would need be recognized to include estimates by knowledgeable persons. There are many blanks in the data requirements associated with a given analysis, blanks that must be filled before the analysis can be made. In many cases the best estimates of knowledgeable persons will constitute the total availability of this type of input information.

The input information is directed into the service phase of the information-generating function, an area designed for and increasingly
delegated to the management science personnel. By way of contr»st it might be observed that the service phase could be limited to the organization of data into reports, tabulations, graphs, ratio tables, and the like. This service could be and likely would be provided by the general accounting or by the cost accounting groups of the company. The management science personnel, however, are, or at least should be, qualified to add that element to the information flow which changes it from a presentation of history to a basis for deciding upon a course of action.

The management science contribution at this point should therefore be to work with operating personnel, decision makers, and upon recognition of a business problem, define and formulate it for the analysis phase. After the problem has been defined, it is obviously required that the actual solution be effected and the results prepared in a form that will be most useful to the decision maker.

There is an impressive array of analysis tools available to the management scientist with which he is able to cope with the complexities of the problems to which reference was just made.

It is not the intent in this paper to discuss in detail the analysis tools that are available. It is rather the intent to describe some of the characteristics of the analysis methods and to support a claim that many and powerful tools of this type are available. Some of the characteristics, with which these analysis techniques can cope are:

1. There are involved, inter-relationships among the factors of the problem. These are inter-relationships that cannot be dealt with readily by means other than an appropriate mathematical formula and the necessary computing facilities. An example of such a problem is the one in which shipping schedules are formulated. The factors of this problem are the supply of the homogeneous
product at a number of origin points, the demand for the product at a number of destination points, and the shipping cost per unit for moving a unit of the product from a point of origin to a point of destination. The objective in the solution is to find that combination of routes which, if followed, will transfer the merchandise from the points of origin to the destinations at the lowest possible total freight cost. In working with problems of this type, it is soon found that interaction frequently necessitates the use of the rates, other than the lowest because, if this were not done, another rate of even greater disadvantage would be forced into use. This is all brought about by the complex inter-relationships of the factors in the problem. Solution to a problem of this type is brought about readily with the analytical tool known as the Transportation Model.
2. In these problems there is either a maximum or a minimum that must be found and that serves as a criterion in evaluating the solution. In the Transportation Model, the minimum freight bill is found, whereas in another type of analytical tool a maximum profit might be found.
3. The solutions to problems may lead directly to the application of results in a routine type course of action or they may lead to alternative courses of action in a planning type analysis. In the latter case various conditions might be evaluated through a simulation of the process.

In direct solutions there must have been a prior implementation of the procedure so that the results of a given analysis can be fed directly to it. This is a form of automated decision making.

In another case, the output of the information-generation process, frequently involving simulation, takes the form of a report to management. 217

The manager or decision maker receives this information and adds to it his knowledge of the process. This, then, is the basis upon which decisions about a course of action can be made.

In the discussion of the service phase of this function it was pointed out that direct solutions might be used in implementing courses of action where a procedure has been implemented and where the course of action is routine. In those cases where that is not done, there is management by exception; that is, the manager is concerned with those steps in the operation of a business that cannot be processed or put into force through decision rules programmed into an electronic data processing system,

The output from the service phase of the information-generating process may therefore take two forms. It may be a decision rule that can put into effect routine courses of action through the medium of the data processing system or the intsrvention of a clerk. In the other case, and in a more important sense, the output will be guides for personnel in the decision-making function who will act to initiate those courses of action that are associated with planning and the operations function of the company.

A system does not function without people, and therefore, consideration must be given to the personnel involved in the Information-Generating function. Just as there is no clear distinction between persons involved in the decision making and in the operating functions, there is also no clear distinction among persons involved in information generation and the other functions in the company. It is rather to be found that the persons in the company are or should be aware of this function and become associated with it in whatever position they may hold. They may be involved directly, as suppliers of data, as a user of the output, or in a capacity that is a combination of these.

A logical way to establish who is part of the information-renerating function and what the relationship between those persons and others outside that function is, is to consider this in the light of information flow. A look at the input-service-output analogy discussed in the preceding section will provide some guidance.

The output of the Information-Generating function is the input to the Decision-Making function and takes the form of reports that have been developed from prime data. The prime data is the input to the InformationGenerating system. The personnel involved, therefore, include those responsible for supplying data from prime records, those who analyze the data, and those who deliver the output to the decision-making personnel.

A question that can and must now be considered is concerned with the relationship between accounting and management science personnel. If an integrated and consistent flow of information is to be generated it is not reasonable to expect that some reports into the decision-making process shall originate in the accounting group and others in the management science group. There can be no guarantee that such an arrangement will assure consistent and noncontradictory information. It creates the possibility of sending still picture type of information into the Decision-Making process when the dynamics of the business call for information of the motion picture type. The conclusion that follows from these comments is that the Information-Generating function must be organized and managed in such a way that it will assure the generation of the most valuable information possible and that it will be sent in its most appropriate form into the Decision-Making function.

The comments made in the preceding paragraphs suggest that there might need be a change in the concept of information generation today as compared with that applying in past years. The idea of information generation is not new, but some concepts associated with the total management information
methods has in it aspects to which there must be adjustment by the personnel involved in that function. Some observations about the difference of concept may be itemized as follows:

1. Reports based on individual studies could be, and many times should be, replaced by information logs derived from a series of simulation analyses. This replaces the static snapshot report with the dynamic motion picture type report.
2. Reports of individual projects will be, and certainly can in many places, be replaced by the results of team effort. Team effort has in its favor, many attributes even though it does carry with it the problem of rivalries, and other problems associated with having persons work as a team.
3. A greater reliance will be placed on decision rules programmed into the data processing system. This will be true partly because of the much greater magnitude of data that needs be reviewed and also because of the analytical and data processing techniques that are available for accomplishing this. This will lead to greater emphasis on management by exception.
4. The environment or climate within the company must be created in which the Information-Generating function can be executed effectively. Managers must realize that the working paper study or report cannot and does not give them all the information they need for decision-making responsibilities. The manager must also learn to accept that a large part of the routine decisions for which he may be responsible can be frocessed on electronic equipment. The reluctance to relinquish detailed control over the activities for which he is responsible can prove to be one of the greatest hindrances in establishing a management information system.
5. It must be recognized that the electronic data frosessirs equipment can serve a furfose much greater than that served in billing, processing accounts receivable and accounts payable, recording inventory and the like. The electronic equipment properly managed by technically trained management science personnel can froduce that element in the Information-Generating function that could tip the scale from mediocre to high level and effective decision making.

In summary, let us conclude that management information is the product of our efforts which, when coupled with a well-executed Decision-Making function, puts into effect the correct courses of action with resfect to business problems, end which in turn find exression in profit generation.

## KINGSTON FORTRAN II

FOR THE IBM 1620 DATA PROCESSING SYSTEM

## by :

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We would like to recognize the following people who made particularly useful contributions to the project:

$$
\begin{aligned}
\text { J.W. Holmes }{ }^{1} \text { - } & \text { for his extremely well written arithmetic } \\
& \text { and function subroutines which appear, with } \\
& \text { some modification, in this system. }
\end{aligned}
$$

F.H. Maskiell ${ }^{2}$ - for many helpful suggestions, particularly in the coding and testing of the arithmetic and function subroutines.
C.H. Davidson ${ }^{3}$ - 1620 Users Group representative on the A.S.A. Fortran II subcommittee, for explaining to us the structure of American Standard Fortran II, and for pointing us in the right direction for extending the language.

1. Cooper-Bessemer Corp., Mount Vernon, Ohio.
2. McGraw-Edison Corp., Penn. Trans. Div., Canonsburg, Pa.
3. University of Wisconsin, Madison, Wis.

## HISTORY

The writing of compilers seems to be one of the more popular pursuits of the members of the 1620 Users Group. At least six different FORTRAN compilers for the 1620 have been written by non-IBM personnel, which testifies to the enthusiasm and ability of 1620 users and to their very real desire to build the best possible mousetrap.

All previous user-written compilers have accepted variations of the FORTRAN I language, with the exception of the University of Wisconsin FORGO, a load-and-go compiler for student problems, which accepted a somewhat restricted FORTRAN II. To our knowledge, KINGSTON FORTRAN II is the first user-written FORTRAN II for the 1620. We hope that this initial effort will encourage others to tackle the problem and improve on our system in the same way that improvement followed improvement in the user-written FORTRAN I compilers.

The initial impetus for KINGSTON FORTRAN II came in about August 1963, from those of us living in Kingston, Ontario, when we started to find out how UTO FORTRAN operated, with the intention of providing a suitable FORTRAN for a 40 K 1620. It soon became apparent that many useful features of FORTRAN II could be incorporated at little extra work. Messrs. Lee and Field, authors of UTO FORTRAN, were approached for ideas and suggestions, the outcome of which was a decision to join forces. After some preliminary discussion, it was found that it would be no more work to write a whole new system than to make the desired alterations in UTO FORTRAN.

The basic concepts were conceived in three rather long evening sessions during the October 1963, 1620 Users Group Meeting in Pittsburgh, Pa. By the end of this meeting the source language structure and the organization and general logic of the compiler were developed and agreed upon. The various sections were then allocated to the individuals best qualified to handle them. By the first week in January, the main sections of the compiler had been written and tested and it remained to tie the pieces together in a operating system. This was done in Kingston, Ontario, during late January, when all 5 authors worked for five days on two identical 40K 1620's (Du Pont of Canada and Queen's University).

We hope that Users with 40K 1620's will find the system useful and easy to operate. We have tried to include every useful idea from other people's efforts so that the system would be as speedy and compact as possible.

The work was divided as follows:
J.A. Field - Input/Output statements, DO statements, input/output subroutines, FORMAT statement.
D.A. Jardine - Arithmetic and function subroutines, write-ups and operating manuals.
E.S. Lee - Compilation of arithmetic expressions.
J.A.N. Lee - Compilation of everything not handled by the other authors.
D.G. Robinson - Symbol table organization, including COMMON, DIMENSION, EQUIVALENCE, TYPE.

## KINGSTON FORTRAN II

This write-up describes a FORTRAN system for the IBM 1620 equipped with automatic division, indirect addressing, additional instructions (TNS, TNF, MF), card input-output and minimum 40 K memory. It is assumed that a Model E-8 or larger 407 is available for listing.

The language is that of IBM's FORTRAN II with a few modifications and a number of additions. For the purposes of this write-up it is expected that the reader is at least on speaking terms with the FORTRAN II language.

The compiler for this system batch compiles a source program in one pass, at approximately twice the speed of existing compilers for the 1620. The execution speed of the object program is also approximately twice that of IBM's FORTRAN II. Considerable effort has been made to speed up all important parts of the system; in addition, more core storage is available for the object program than existing FORTRAN II compilers allow.

SOURCE PROGRAM CARDS
These are as required for IBM FORTRAN II. Any number of continuation cards are possible, but the statement may not contain more than 300 characters (blanks not included except in Format statements).

## ARITHMETIC PRECISION

Real numbers: 8 digit mantissa, 2 digit exponent.
Notation is excess 50; (i.e. $1.0 \equiv 5110000000$ )
Integer numbers: 4 digits, modulo 10000

## VARIABLES

These are as in IBM FORTRAN II. 1 to 6
alphabetic or numeric characters, starting with a letter, which, for integer variables, must be one of I, J, K, L, M , N , unless otherwise specified in a TYPE declaration.

## SUBSCRIPTS

A variable with, at the most, two subscripts appended to it can refer to an element of a one-or twodimensional array. Three dimensional subscripting is not permitted. A subscript may be an expression of any
desired complexity, provided only that the result of the evaluation of the expression be an integer quantity. This should be positive if you want to avoid trouble. However, a zero or a negative subscript can be used. To use this effectively, the programmer must know how data areas are laid out in memory. See the operating instructions:

Examples of Subscripts:

$$
\begin{aligned}
& I \\
& 3 \\
& 2+M U \\
& M U+2 \\
& J * 5+M \\
& 5 * J \\
& 6 * J-K+2-10 / L+M \\
& 4 * J(K+2-L+M)+K(M(N+2)) / 3 \\
& F I X F(A * B+3.0 * * S N(X))+L / 2
\end{aligned}
$$

The variable in a subscript may itself be subscripted, and this process of subscripting may be carried on to any desired depth of subscripting. It can, in fact, be carried far beyond the point where the average programmer understands what he is doing.

## SUBSCRIPTED VARIABLES

Only singly or doubly subscripted arrays may be defined. The size of these must be specified in a DIMENSION statement.

EXPRESSIONS
These are defined and organized exactly as in IBM FORTRAN II.

LIBRARY FUNCTIONS
Ten library (closed) functions are included in the KINGSTON FORTRAN II System. These are listed in Table I.

TABLE 1
Closed Subroutines

| Function | Function | No. of | Type | Of |
| :---: | :---: | :---: | :---: | :---: |
| Definition | Name (s) | Arguments | Function | Argument |
| Sine of the argument | SIN | 1 | Real | Real |
| Cosine of the argument | cos | 1 | Real | Real |
| Exponential ( $e^{\mathrm{x}}$ ) of the argument | EXP | 1 | Real | Real |
| Natural logarithm of the argument | LOG | 1 | Real | Real |
| Arctangent of the argument | ATAN | 1 | Real | Real |
| ```Arctangent of (arg1/ arga)``` | ARCTAN | 2 | Real | Real |
| Signum of the argument; $=-1$. for $\mathrm{X}<0 .,=0$. for |  |  |  |  |
| $X, 0 .,=+1$. for $X>0$. | SIGNUM | 1 | Real | Real |
| Absolute value of Arg 1 with the sign of Arg 2 | SIGN | 2 | Real | Real |
| Choosing the larger val of the two arguments | AMAXI | 2 | Real | Real |
| Choosing the smaller value of the two arguments | AMIN1 | 2 | Real | Real |

Table 2 lists the open or built-in functions. These are compiled in-ine every time the function is referred to.

TABLE 2

Function
Definition
Absolute value of the argument ABS ABS I Integer Integer

Table 3 lists closed functions which are permanently stored in the machine, whether or not they are mentioned by name in a FORTRAN source program.

TABLE 3
$\left.\begin{array}{lccccc}\begin{array}{l}\text { Function } \\ \text { Definition }\end{array} & \begin{array}{c}\text { Function } \\ \text { Name }\end{array} & \begin{array}{c}\text { No. of } \\ \text { Arguments }\end{array} & \begin{array}{c}\text { Function }\end{array} & \begin{array}{c}\text { Type }\end{array} \\ \begin{array}{lll}\text { Floating an integer }\end{array} & \text { FLOAT }\end{array}\right)$

## THE ARITHMETIC STATEMENT

The arithmetic statement is the same as in IBM FORTRAN II except for the extensions in complexity of evaluation of subscripts.

CONTROL STATEMENTS
The control statement flexibility in standard FORTRAN's leaves something to be desired, particularly where the program is complex and core storage is at a premium. These conditions, it might be noted, are the normal ones for almost all problems. KINGSTON FORTRAN II attempts to improve this situation by expanding the capabilities of the ASSIGN and assigned GO TO statement and by extending the ASSIGN concept to the other control statements.

ASSIGN STATEMENT
ASSIGN $i$ to $n$
In IBM FORTRAN II, the ASSIGN statement is used only in conjunction with an assigned GO TO statement. For instance,

ASSIGN 3 TO J
GO TO J, $(3,5,9,243)$
will cause a branch to the statement numbered 3 .
The effect of the ASSIGN statement is to "equate" the non-subscripted integer variable $J$ to statement number 3. The subsequent GO TO J, $(3,5,9,243)$ is then interpreted as GO TO 3.

In KINGSTON FORTRAN II, this concept has been modified and expanded considerably. To describe these changes, the following definitions are used:

Statement Label - A statement label is the name attached to the memory location containing the first instruction compiled from the statement identified by the label. There are two kinds of statement labels:

Numeric Statement Label - usually known as a $\bar{s} \bar{t} \bar{a} \neq \overline{m e n} \bar{t} \bar{n} u \bar{m} \bar{b} \bar{e} \bar{r} .-\bar{A} \bar{n}$ unsigned integer number of from one to four digits long.

Alphabetic Statement Label - A variable which may
 by one or more ASSIGN statements has been equated to a numeric statement label (statement number).

It is most important to realize the difference between a statement label and an arithmetic variable. ASSIGN 3 TO J will place in $J$ the address of the first instruction compiled from statement number 3. J $=3$ will cause the number 0003 to be placed in J. The sequence of statements

ASSIGN 3 TO J
GO TO J
will cause a branch to statement numbered 3. However,

$$
\begin{aligned}
& J=3 \\
& \text { GO TO J }
\end{aligned}
$$

will result in disaster. Moreover,
ASSIGN 3 TO J
$J=J+1$
GO TO J
will not transfer control to the statement numbered 4. Arithmetic on assigned variables is not permitted; assigned variables are not in any way the same as arithmetic variables, except that they may be subscripted and stored in an array. They may also appear in COMMON, DIMENSION, and EQUIVALENCE statements.

It is possible in KINGSTON FORTRAN II, to equate two alphabetic statement labels by an ASSIGN statement. If the first statement label in the ASSIGN statement ismalphabetic, it must be enclosed in parentheses.

The following examples illustrate the ASSIGN statement:
ASSIGN 3 TO N (St. label N is equated to St. label 3)
ASSIGN (N) TO J (St. label $J$ is equated to St. label N)
ASSIGN 3 TO I (K) (same as the line above. J must have been defined before this statement and I must be dimensioned).
ASSIGN (I $(K)$ ) TO $L(3+M / 4-M * * 3)$
(same as above. The alphabetic statement labels can be subscripted as desired).

Since the primary definition of a statement identifier is its occurrence as a statement number, it is necessary that any given statement identifier must ultimately be defined (through a series of ASSIGN statements if necessary) in terms of a statement number. Failure to observe this rule will cause trouble. For example,
$3 \quad A=B$
ASSIGN (J) TO K(L)
is not correct, because $J$ has not been associated with any statement identifier when the ASSIGN statement is executed. However,
$3 \quad A=B$
ASSIGN 3 TO J
ASSIGN (J) TO K(L)
is correct.
Alphabetic statement labels may be used in the following control statements:

GO TO (both unconditional and assigned)
IF (SENSE SWITCH 1)
IF (arithmetic expression)
Computed GO TO
Alphabetic statement labels may not be used in a DO statement.
GO TO STATEMENT

GO TO $n$ unconditional GO TO
GO TO $n,\left(n_{1}, n_{2},--n_{m}\right)$ assigned GO TO
where $n$ is a statement label. If $n$ is alphabetic, then it must previously have been defined in an ASSIGN statement. The assigned GO TO statement is treated exactly like the GO TO statement. The comma and parenthesized list are optional and will be accepted but ignored by the compiler.

Computed GO TO Statement
GO TO $\left(n_{1}, n_{2}, n_{3}--n_{m}\right)$,i
where $n_{1}, n_{2}--n_{m}$ are statement labels. If alphabetic they must have been previously defined by ASSIGN statements. $i$ is a fixed point (integer) variable or expression. i may be subscripted as desired.

ARITHMETIC IF STATEMENT
$\operatorname{IF}(\mathrm{a}) \mathrm{n}_{1}, \mathrm{n}_{2}, \mathrm{n}_{3}$
where $a$ is an integer or real (floating point) expression of any complexity, and $\mathrm{n}_{1}, \mathrm{n}_{2}, \mathrm{n}_{3}$ are statement labels. If alphabetic, $n_{1}, n_{2}, n_{3}$ must have been previously defined in ASSIGN statements.

IF (SENSE SWITCH) STATEMENT
IF (SENSE SWITCH i) $\mathrm{n}_{1}, \mathrm{n}_{2}$
where i is a one or two digit unsigned integer number or an integer expression, and $n_{1}, n_{2}$ are statement labels. If $i$ is an integer expression, the low order two digits of the value of the expression are used as the value of i. The two digit numbers resulting from this are the numbers of machine indicators, not just console switches.

THE DO STATEMENT
DO $n i=m_{1}, m_{2}, m_{3}$
where n is a statement number, $i$ is an unsigned integer variable which may be subscripted and $m_{1}, m_{2}, m_{3}$ are integer variables or integer expressions of any dosired complexity, positive or negative. $n$ may not be an alphabetic statement label, and i may not be an expression. There are no particular restrictions on $\mathrm{m}_{1}, \mathrm{~m}_{2}, \mathrm{~m}_{3}$. In particular they may be positive or negative quantities. If $m_{1}=m_{2}$, the DO will be executed once only. $m_{1}, m_{2}, m_{3}$ should be chosen so that the DO loop terminates. See below for an example of a never-ending DO-loop.

Example:

$$
\text { DO } 5 \mathrm{~J}=\mathrm{K}+\mathrm{L}-5, \mathrm{M}-\mathrm{I}(\mathrm{JOB}(\mathrm{KK})),-\mathrm{L}
$$

If $m_{1}, m_{2}, m_{3}$ are expressions, their values are the values of the expressions when the DO statement is encountered at object time, and these values are unaffected by alteration inside the DO of the values of the variables in the expressions $m_{1}, m_{2}, m_{3}$.

As a result of allowing positive or negative values for $m_{1}, m_{2}, m_{3}$, it is legal to have DO loops which count down. For example,

$$
\text { DO } 3 I=10,1,-1
$$

will cause $I$ to run from 10 to 1 in steps of ( -1 ). The following is also permitted.

$$
\text { DO } 10 \mathrm{~J}=-10,5,2
$$

which will cause $J$ to assume successively the values $-10,-8$, $-6,-4,-2,0,2,4$. If the DO variable assumes zero or negative values, it may be used, with caution, as a subscript. Intelligent use of negative or zero subscripts demands knowledge of the layout of data areas in memory, as described in the operating instructions.

Care should be taken to see that the DO index terminates properly. For instance,

$$
\text { DO } 20 \mathrm{~K}=-10,-1,-2
$$

will increment nearly 5000 times before termination. The same is true of

$$
\text { DO } 40 \mathrm{~K}=10,1,2
$$

Termination in both cases occurs because integer arithmetic is performed modulo 10000.

All the restrictions on DO statements currently imposed by IBM FORTRAN II are also in force in KINGSTON FORTRAN, except as already mentioned.

CONTINUE STATEMENT
Same as IBM FORTRAN II.

## PAUSE STATEMENT

PAUSE
PAUSE $n$, where $n$ is a fixed point constant, variable or expression.

The typewriter types PAUSE n, together with error messages (see operating instructions) and the machine halts. If $n$ is a variable or expression, its current value is typed. PAUSE (without $n$ ) generates an in-line halt command; there is no typing. In either case, depression START will cause resumption of program.

## STOP STATEMENT

STOP
STOP n, where $n$ is a fixed point constant, variable or expression.

The typewriter will type STOP, followed by the current value of $n$. If $n$ is not specified, STOP 0000 will be typed. CALL EXIT is then executed (see operating instructions).

END STATEMENT
END is an instruction to the compiler that the program is complete. An END statement must be physically the last card of the main line program and of each subprogram which is associated with the job. The END statement results in CALL EXIT except in a sub-program, where it is interpreted as a RETURN statement.

FUNCTION AND SUBPROGRAM STATEMENTS
FUNCTION and SUBPROGRAM statements are the same in KINGSTON FORTRAN as in IBM 1620 FORTRAN II, and the same restrictions apply.

Because the compiler is one-pass, the subprograms are not compiled separately from the main program. See the operating instructions for further details.

## INPUT/OUTPUT STATEMENTS

The INPUT/OUTPUT statements in KINGSTON FORTRAN II are similar to those of IBM FORTRAN II, except that expressions are permitted, as well as simple variables, in certain places in INPUT/OUTPUT lists. Indexed lists, array names (to handle a whole array) and all other standard FORTRAN II features are allowed. It is not necessary to specify a FORMAT statement number in an I/O statement. If no FORMAT statement number is given, the system will supply FORMAT (5N). See the description of FORMAT for an explanation of FORMAT (5N).

The permitted INPUT/OUTPUT statements are:
READ (card input), ACCEPT TAPE, ACCEPT (input on console typewriter), REREAD (re-reads last input record), PUNCH, PUNCH TAPE, TYPE (console typewriter), PRINT (on-line printer).

Indexed I/O Lists
As in IBM FORTRAN II, the statement

$$
\operatorname{READ} 10,((A(I, J), I=1,10), J=1,10)
$$

will cause 100 numbers $(A(1,1)$ to $A(10,10)$ to be read into array A. Similarly,

$$
\operatorname{READ} 10,((A(I, J), \quad I=K, L), \quad J=M, N)
$$

will cause various elements of $A$ to be read in under the control of the indices $I$ and $J$.

In KINGSTON FORTRAN II, the limits on the implied DO's ( $I=K, L ; J=M, N$ ) may be expressions. Furthermore, the names of the input variables may be subscripted to any desired depth (not exceeding 40). For example:

READ 10, ( $(A(I(K I), J(M I), K I=K-J O B * 2, I+5-J 6), M 1=M * 8-M M 9, N-3 * N 18)$
will be executed as

$$
\begin{aligned}
& \text { DO } \quad 100 \mathrm{MI}=\mathrm{M} * 8-\mathrm{MM} 9, \mathrm{~N}-3 * \mathrm{~N} 18 \\
& \text { DO } \quad 100 \mathrm{KI}=\mathrm{K}-\mathrm{J} 0 B^{*} 2, \mathrm{~L}+5-\mathrm{J} 6
\end{aligned}
$$

$100 \operatorname{READ} 10, \mathrm{~A}(\mathrm{I}(\mathrm{KI}), \mathrm{J}(\mathrm{MI}))$
where $I$ and $J$ are names of one-dimensional arrays which must previously have been defined.

KINGSTON FORTRAN II permits the same kinds of expressions in indexing as are permitted in standard DO statements. The implied DO in and I/O list may run forward or backward, and may have integer expressions of any desired complexity.

INPUT LISTS
In an input list, the variables may be only simple variables or indexed variables. Input of expressions is meaningless, and not permitted. For example:

READ 10, $M, \mathrm{Q}, \mathrm{A}\left(\mathrm{I}\left(\mathrm{K}+\mathrm{H}^{*} \mathrm{~L}\right), \mathrm{M}\left(\mathrm{N}-5^{*} \mathrm{~L}+4\right)\right), \mathrm{B}$ is permitted, provided $I, K, L, N$ and $M$ are previously defined. READ 10, $A+B-C(K)$ is not permitted.

## OUTPUT LISTS

Output lists may be fully indexed lists, as described above. In addition, expressions may appear in the list as output quantities. For example:

PUNCH 20, C*D/(LOGF (X-Y*Z)+10.3, Y, D
will cause

$$
\mathrm{C} * \mathrm{D} / \mathrm{LOGF}(\mathrm{X}-\mathrm{Y} * \mathrm{Z})+10.3
$$

to be calculated at the time the punch statement is encountered and its value to be punched, together with the values of $Y$ and D, on a card, according to Format statement 20. The value of the expression in an output list is lost when it is output, and is not available for further calculation. The expression in an I/O list may be of any desired complexity, and may be indexed as required, either by DO statements, or by implied DO statements in the list itself. For example:

PUNCH 20, (( (C*SQRTF (A (I,J))-M(I)),I=1,L+4,3),J=I+1,K-10,5)
will cause values of $C * \operatorname{SQRTF}(A(I, J))-M(I)$
to be punched out for values of J from $\mathrm{I}+1$ to $\mathrm{K}-10$ in steps of 5 and values of $I$ from 1 to $L+4$ in steps of 3 .

## ASSIGNED FORMAT NUMBERS

Format statement numbers may be assigned by ASSIGN statements in the same way any other statement number can. Hence, input/output statements may use alphabetic statement labels in place of Format statement numbers. For example, the following program is permitted:

|  | FORMAT (5 (I3,Flo.5) |
| :---: | :---: |
| 4 | FORMAT (5I5) |
| 5 | FORMAT (5I7) |
|  | ASSIGN 3 TO J |
|  | ASSIGN 4 TO K(1) |
|  | ASSIGN 5 TO K(2) |
|  | READ J, (M ( I ), $\mathrm{A}(\mathrm{I}), \mathrm{I}=1,5$ ) |
|  | DO $10 \mathrm{~L}=1,2$ |
| 10 | READ K(L), (M4 (I), $\mathrm{I}=1,5$ ) |

Note that the first statement will be executed according to Format statement 3, while the second READ statement will be executed according to Format Statement 4 when $L=1$, and according to Format Statement 5 when $\mathrm{L}=2$.

The subscripted variables in all the above examples must previously have been mentioned in a DIMENSION statement.

## ARRAY NAMES IN I/O LIST

As in IBM FORTRAN II, array names without subscripts may appear in I/O lists. Mention of an array name will cause the entire array, as specified in the DIMENSION statement to be input or output. Two dimensional arrays are handled column-wise -

$$
\begin{aligned}
& \text { DIMENSION A }(10,10) \\
& \text { READ, A }
\end{aligned}
$$

will cause the entire 100 elements of $A$ to be read in, in 5 N notation. The elements of $A$ must be in order $A(1,1), A(2,1)$, $A(3,1), A(4,1), A(5,1), A(6,1)$, etc.

## FORMAT STATEMENTS

Format statements are, in general, equivalent to Format statements allowed in 7090/94 FORTRAN II. E, F, I and A conversion are permitted. Repetition of field format is allowed before E, F,I or A. Thus FORMAT (I2,3E12.4) is equivalent to

FORMAT (I2,E12.4,E12.4,E12.4)
Parenthetical expression is permitted in order to enable repetition of data fields according to certain Format specifications within a longer FORMAT statement. The number of repetitions is limited to 99. Thus,

FORMAT (2 (F10.6,E10.2),I4)
The level of parenthesizing can be extended to a second level, thus:

FORMAT $(2(\mathrm{I} 4,2(\mathrm{~F} 6.2, \mathrm{~F} 8.3)))$ is equivalent to
FORMAT (I4,F6.2,F8.3,F6.2,F8.3,I4,F6.2,F8.3,F6.2,F8.3)
The depth of such nesting of parentheses must not exceed 5, which appears to be more than would ever be necessary.

## N-Format

Rigid format on input data is not always desirable, and in many cases makes key-punching more difficult. KINGSTON FORTRAN allows so-called "free form" input, as well as the more familiar fixed or rigid format. If the FORMAT statement specifies $I$, $E$ or $F$ format on input, then the input data record must conform to the normal rules for such format as specified in IBM manuals. However, if $N$ format (denoting "free form") is used, the data numbers may appear anywhere on the card, and input is controlled by the input list.
$N$ format is used like $E, F$ or $I$ format except that no width or decimal point location digits are required or permitted. For example,

> READ 10, I, J, A, C, Z
> 10 FORMAT $(5 \mathrm{~N})$
will cause the program to read in a record of 2 integer numbers followed by 3 floating-point numbers. In $N$ format, a number is defined as: any number of leading blanks, followed by a meaningful collection of digits, followed by $l$ trailing blank. Note that the blank column immediately following the right-most digit or character of the number is considered part of the number, and serves to delineate the right-hand end of the number.

In the case of E numbers handled with N -format, blanks after the letter E are ignored, and the machine uses the next set of digits as the exponent. For example:

$$
\text { bl . } 2345678 \mathrm{E}-05 \mathrm{~b}
$$

will be interpreted as .000012345678.
The number bl. $2345678 \mathrm{Ebbbbb}-05 \mathrm{~b}$
will be interpreted in the same way.
b1.2345678Ebbbbl03
will result in an error condition (see operating instructions).
b1. 2345678 E bb 00005
will be interpreted as 123456.78. Leading zeros before either the mantissa or exponent are ignored.

An E- type number handled by N-format ends with the blank after the exponent digits.

A FORMAT statement may specify N, E, F, I or A format as required, thus allowing both free and rigid format on the same card. Note that, in $N$ format, if a floating point number does not have a decimal point, it is assumed to be after the low-order digit of the number.

Some examples may help:
READ 10, I, J, A, C, Z
10 FORMAT (5N)
The card might look like:
bbl23bbbbbb12bbb16.3bbbbbl.2E6b123000bbb etc.
N Format requires only that at least 1 blank column follow the number. In this case, I, J, A, C, Z would be stored as 123, 12, 16.3, 1.2E06, 123000. resp.

READ 11, I, J, A, C, Z
11 FORMAT (I3, I6, N, FlO.3, N)
The Format requires that I, J, C follow rigid format. The card might look like:
bl2bbbl2bbbbbb120.bbbb1234567bbb16.8bbb etc.
This would give the following results:
Variable Value

| I | 12 |
| :--- | :--- |
| J | 120 |
| A | 120. |
| C | 1234.567 |
| Z | 16.8 |

Note that the F-specification for C starts on the first column after the blank following 120., (see the position of the arrow) since this blank is considered part of the value of an N-Format number.

An output, N format is equivalent to $1 \mathrm{PE} 14.7,1 \mathrm{X}$ for floating point numbers, and I5,lX for integer numbers.

N Format allows repeated format and parenthesizing, and follows the usual rules for them.

If a number is positive, the output under E, F, I or $N$ Format will not contain a leading plus sign. On I Format, no space is left for it, so that it is possible to construct a fully packed output record provided all numbers are positive. N Format generates a space for a + sign and a space following the number.

If a floating point number is output under Iw Format, the integer part of the floating point number is convered to Iw Format. Thus 128342.56 output with IlO Format would appear as bbbbl28342.

## SCALE FACTORS

To permit more general use of $E$ and $F$ conversion, a scale factor followed by the letter $P$ may precede the specification. The scale factor is defined such that

Output number $=$ internal number $\times 10^{\text {scale }}$ factor
Internal number $=$ input number $\times 10^{\text {-scale factor }}$ This operates exactly the same as in IBM FORTRAN II for the larger machines. For example

FORMAT (2PF10.4)
used on output will multiply the number by 100 before output. On input, it will divide the external number by 100 before storing it in the machine.

On E-Format output, the effect of P-scaling is to shift the decimal point in the mantissa and to adjust the exponent by the amount of the shift.

Thus, if FORMAT(E15.8), used for output, produced the number . $12345678 \mathrm{E}-04$, then FORMAT ( 3 PE15.5) would produce $123.45678 \mathrm{E}-07$ for the same number. Note that for E-Format output, P-scaling does not change the magnitude of the number. It shifts the decimal point, and makes a compensating change in the exponent. For F-Format, P-scaling alters the magnitude of the number on input/output.

## VARIABLE FORMAT

KINGSTON FORTRAN II allows variable Format. That is, Format specifications may be read in at object time. In this way, data may be read in under control of a Format Statement which itself has been read in. Variable Format statements must be read under A-Format into an array by means of a normal Read statement.

For example:
DIMENSION FMT (15)
READ 10, ( $\operatorname{FMT}(I), I=1,14)$
10 FORMAT (15A5)
will cause 70 characters of input record (i.e. the Format Statement being read in) to be stored in array FMT. It is then possible to write:

READ FMT, A, B, X, Z, (A(J), J=1,10)
where the input variables will be read in according to the Format Statement stored in array FMT.

It is also possible to alter array FMT by programming. This should be done with some care, otherwise the Format Statement stored in array FMT may become completely unintelligible.

The name of the variable Format specification must appear in a DIMENSION Statement, even if the Array size is only 1.

The Format read in at object time must take the same form as a source program Format Statement except that the word Format is omitted, i.e. the variable Format begins with a left parenthesis.

## SPECIFICATION STATEMENTS

## COMMON

Variables, including array names, appearing in COMMON statements will be assigned core storage locations beginning at the high end of memory, and will be stored at object time in descending sequence, 10 digits per variable, or per item of a dimensioned variable, as they are encountered in the COMMON statement. If a variable is a dimensioned variable, the size of the dimensioned array must appear in the COMMON statement, and the variable must not again be dimensioned in a DIMENSION statement. The COMMON statement must precede EQUIVALENCE or DIMENSION statements (if any) and must precede the first statement of the source program. For example:

COMMON $A, B, I, J, X(10,3), Y(5)$
(Inclusion of dimensioning information in COMMON statements is allowed in FORTRAN IV).

## DIMENSION

The DIMENSION statement is the same as IBM FORTRAN II except that variables already mentioned in COMMON may not again be dimensioned and that only 2 subscripts are allowed.

> DIMENSION $\mathrm{Z}(10,5), \mathrm{V}(400)$ is permitted
> DIMENSION $\mathrm{X}(10,5,10)$ is not permitted

EQUIVALENCE
EQUIVALENCE ( $\mathrm{a}, \mathrm{b}, \mathrm{c},---$ ), ( $\mathrm{d}, \mathrm{e}, \mathrm{f},--$ ),---
where $a, b, c, d, e, f$, are variable names. KINGSTON FORTRAN imposes some restrictions on EQUIVALENCE statements which are not present in IBM FORTRAN II. These are noted below:

1. Single variables may be equivalenced only to single variables.
2. Arrays may be equivalenced to other arrays, of the same size only.
3. Single variables may not be equivalenced to individual items of arrays, nor may single items of two arrays be equivalenced. In general, no subscripts may appear in an Equivalence statement.
4. Because the compiler is single pass, it is crucial that the order in the source deck be:

COMMON (if any), DIMENSION (if any), EQUIVALENCE (if any).
They must precede the first executable statement of the program.
5. If arrays are to be equivalenced, the first item only
in the list must have been defined previously in a
COMMON, or DIMENSION declarāion, and the remaining items in the list must not have been so defined. The Equivalence statement itself defines these remaining items. If single variables are to be equivalenced, and any item in the Equivalence list has been defined in a previous COMMON or TYPE statement, it must be first in the Equivalence list, and the other items must not have been defined in a COMMON or TYPE statement. For example,

$$
\begin{aligned}
& \text { COMMON A, B }(10,3), C \\
& \text { DIMENSION D }(50) \\
& \text { EQUIVALENCE }(\mathrm{A}, \mathrm{~F}, \mathrm{G}),(\mathrm{D}, \mathrm{X})
\end{aligned}
$$

This puts A, array B, and C in common storage; defines array $D$; defines $F$ and $G$ as single variables in the same memory location as $A$; and defines $X$ as a 50-item vector in the same location as D. The following are errors: (in the example above).

| EQUIVALENCE | $(D, A)$ |
| :--- | :--- |
| EQUIVALENCE | $(B,(1,1), G)$ |
| (para.1,2) | (para. 3$)$ |
| EQUIVALENCE $(X, D)$ | (para.5, X not defined) |
| EQUIVALENCE $(G, A, F)$ | (para.5, G not defined, |
|  | A defined) |
| EQUIVALENCE $(D(50), X(50))$ (para.3) |  |

6. To preserve compatibility with other FORTRAN systems, which require DIMENSION statements for all array variables in an Equivalence list, KINGSTON FORTRAN allows extra DIMENSION statements after the Equivalence statements. Such DIMENSION statements may be used to mention the equivalenced variables, but since they have already been defined in the Equivalence Statement, the compiler will ignore them. It will not, however, call them errors. For example:

DIMENSION X(10), $\mathrm{Y}(20)$
EQUIVALENCE (X,A,B), (Y,C,G)
DIMENSION $A(10), B(10), C(20), G(20)$
is permitted. The variables $A, B, C, G$ in the second DIMENSION statement are ignored by the compiler, because they have already been defined in the preceding EQUIVALENCE Statement.
7. It is possible to equivalence items not of the same type or mode: e.g. EQUIVALENCE (A,I) - where A is real and I is integer.

## TYPE

Two TYPE declarations are permitted. These statements determine the type of variable associated with each variable name appearing in the statement. This TYPE declaration is in effect throughout the program. The two declarations are

INTEGER $a, b, c, \ldots$
REAL $a, b, c, \ldots$
where $a, b, c$, are variable names appearing within the program. Function names may not appear in TYPE declarations.

## Rules:-

(1) A variable defined to be of a given type remains of that type throughout the program.
(2) INTEGER indicates that the variables listed are integer, and over-rides the alphabetic naming convention.
(3) REAL indicates that the variables listed are floating point, and over-rides the alphabetic naming convention.

The TYPE declaration must occur before the first executable statement of the program. If any of the variables mentioned in a TYPE declaration are mentioned in a COMMON or DIMENSION statement, the TYPE declaration must follow such mention.

If a TYPE declaration precedes an EQUIVALENCE statement, then it defines a variable in the sense required by the EQUIVALENCE statement, and all variables equivalenced to the one declared in the TYPE statement will be of the same type.

If a TYPE declaration follows an EQUIVALENCE statement, then only the specific variable names mentioned in the declaration will be affected.

Examples,

1. INTEGER A EQUIVALENCE (A,B,C)
2. EQUIVALENCE (A,B,C) INTEGER A
3. EQUIVALENCE (A , B , C) INTEGER A,B,C
4. INTEGER A,B,C EQUIVALENCE (A,B,C)

Examples 1 and 3 cause $A, B, C$, to be integer variables and occupy the same memory location.

Example 2 causes $A$ to be integer, $B, C$ to be real, and $A, B, C$ to occupy the same memory location.

Example 4 is an error in KINGSTON FORTRAN (see para. 5 under EQUIVALENCE).


[^0]:    

[^1]:    TYPE IN VIFF
    $(-0+-(R+(-0+P))) /--(-R .(Q . F))$
    $(-\mathrm{Q}+-(\mathrm{R}+(-\mathrm{Q}+\mathrm{P}))) /-(-\mathrm{R} \cdot(\mathrm{Q} . \mathrm{F}))$
    TEST ON C1 - WIFF WITHOUT STACKEC NEGATIVES
    $(-\mathrm{Q}+-(\mathrm{R}+(-\mathrm{Q}+\mathrm{P}))) /(-\mathrm{R} \cdot(\mathrm{Q} \cdot \mathrm{P}))$
    TEST ON C2 - WFF AS TWO VARIAELE LIST
    WFF $S / V$
    $S=-0+-T$
    $S=-Q+-T$
    $T=R+U$
    $U=-0+P$
    $V=-Q+P$
    $V=-R . W$
    WO THEOREM

[^2]:    * Speaker (to whom enquiries concerning this programe should be sent.)

